

# Ciências ULisboa

Faculdade  
de Ciências  
da Universidade  
de Lisboa

# **DISCIPLINA LEEA**

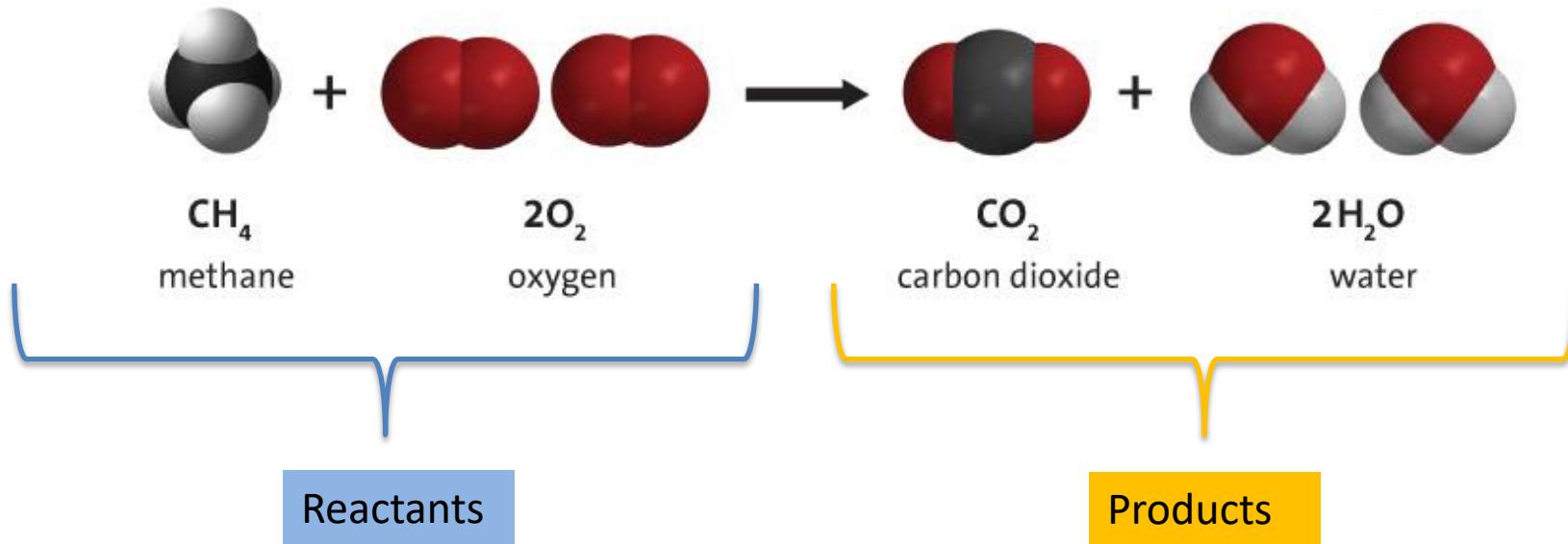


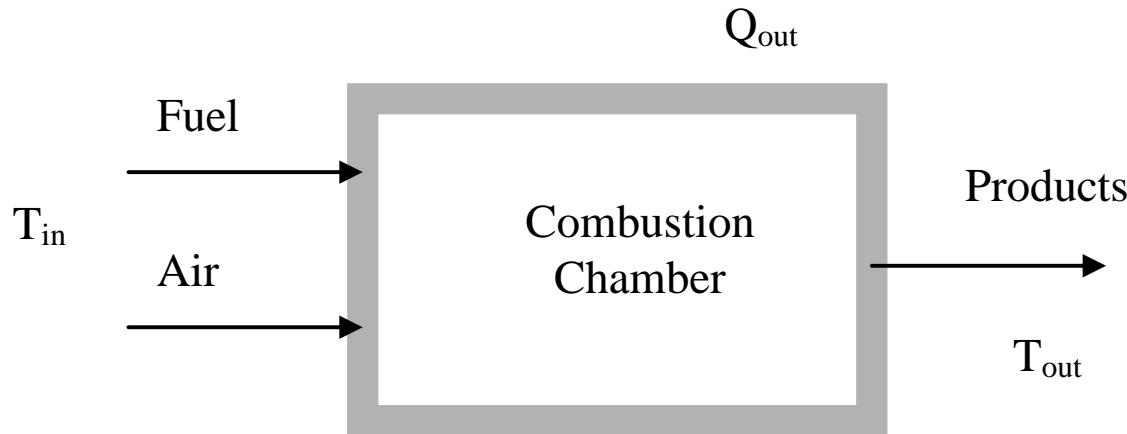
# **Technologies of combustion**

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## Corpo docente

**Carla Silva (Teóricas e práticas) /Theory and practice**  
[camsilva@ciencias.ulisboa.pt](mailto:camsilva@ciencias.ulisboa.pt)



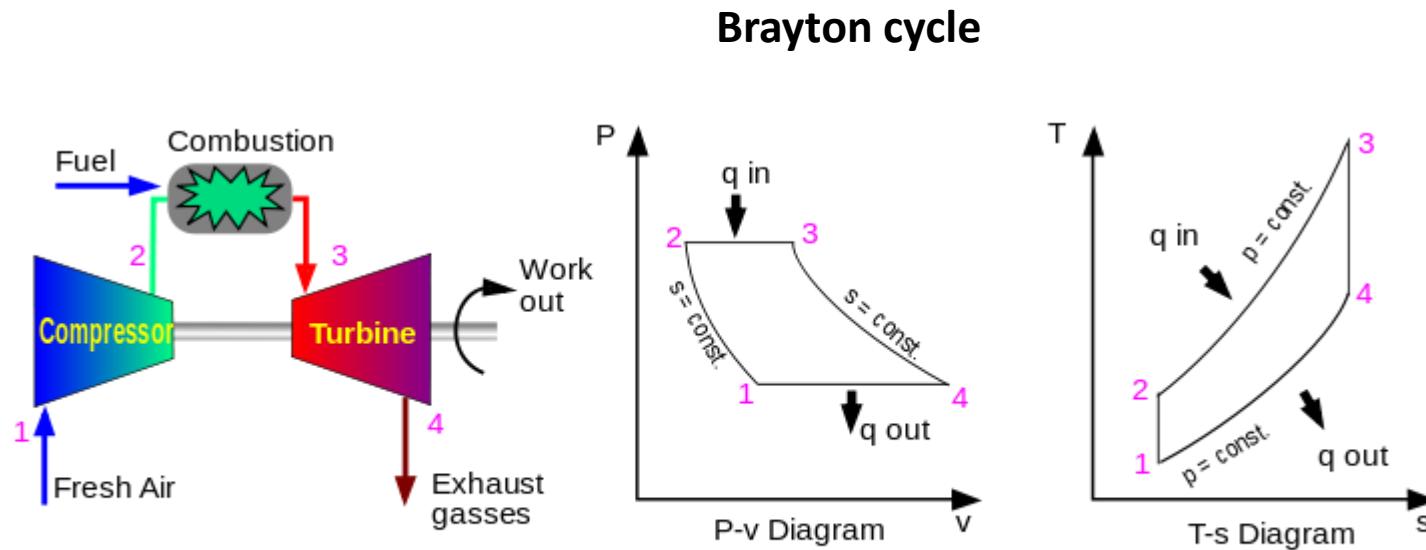


- Maximum heat release,  $\max Q_{out}$ :  $T_{out} = T_{in}$
- Maximum flame temperature,  $T_{ad}$ :

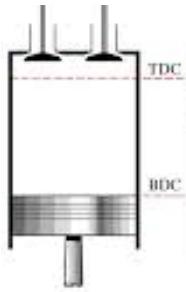
$H_{reag}(T_{in}) = H_{prod}(T_{ad})$  (constant pressure, e.g. Diesel engine, gas turbine, furnace)

$H_{reag}(T_{in}) = H_{prod}(T_{ad}) - R(n_{prod}T_{ad} - n_{reag}T_{in})$  (constant volume, e.g. gasoline engine)

$H_{\text{reag}}(T_{\text{in}}) = H_{\text{prod}}(T_{\text{ad}})$  (constant pressure, e.g. Diesel engine, **gas turbine**, furnace)

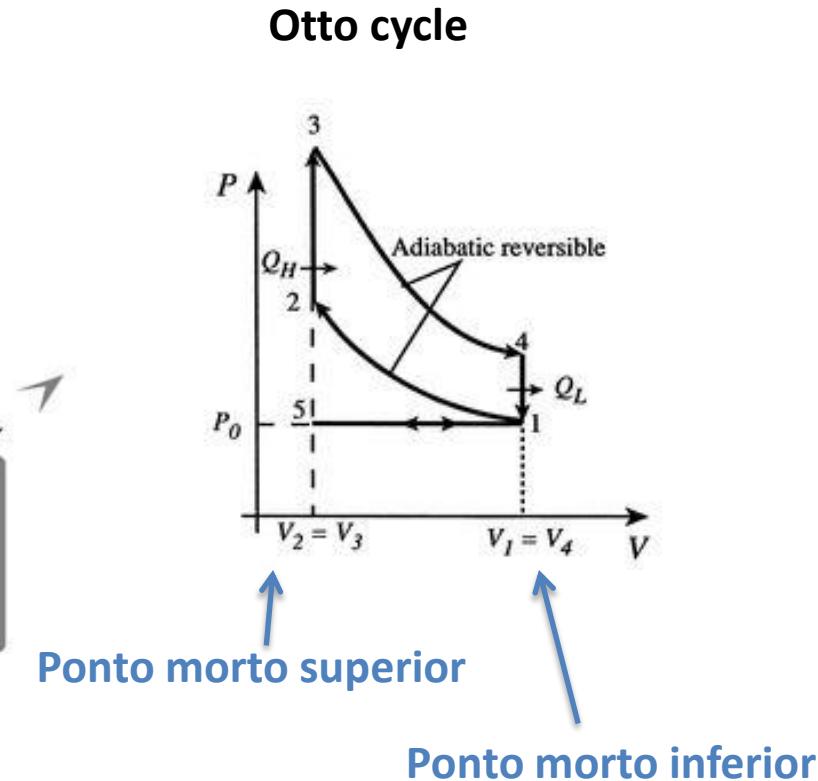
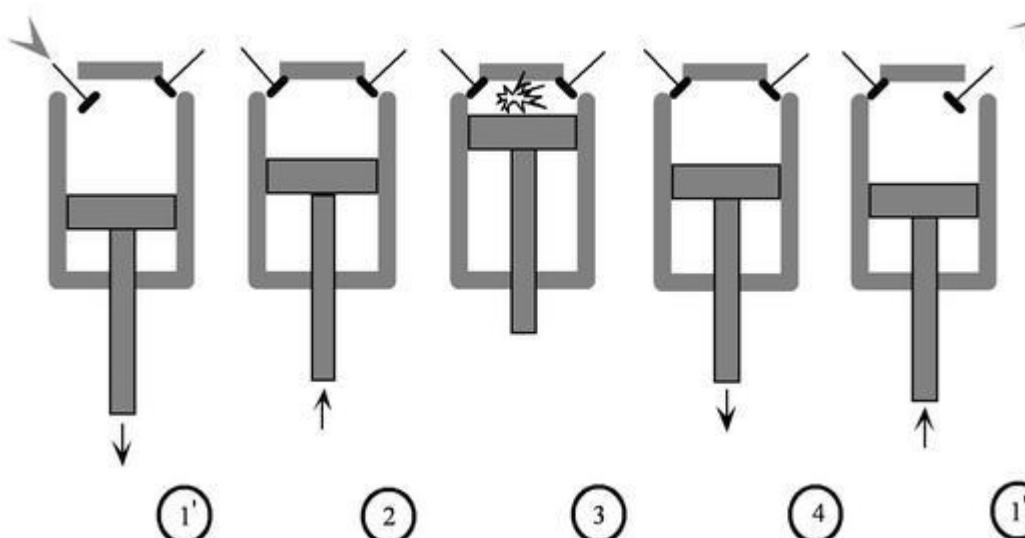


$$H_{\text{reag}}(T_{\text{in}}) = H_{\text{prod}}(T_{\text{ad}}) - R(n_{\text{prod}} T_{\text{ad}} - n_{\text{reag}} T_{\text{in}}) \quad (\text{constant volume, e.g. gasoline engine})$$

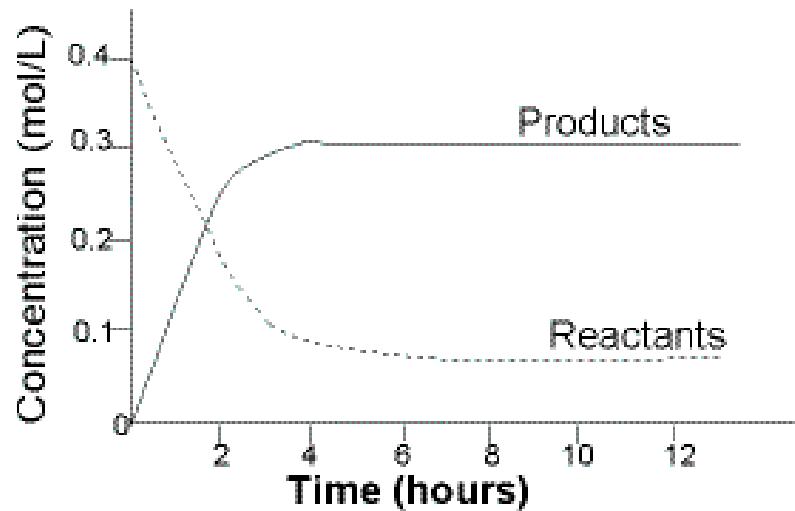


*Top Dead Centre*  
*- Ponto morto superior*

*Bottom Dead Centre*  
*- Ponto morto inferior*

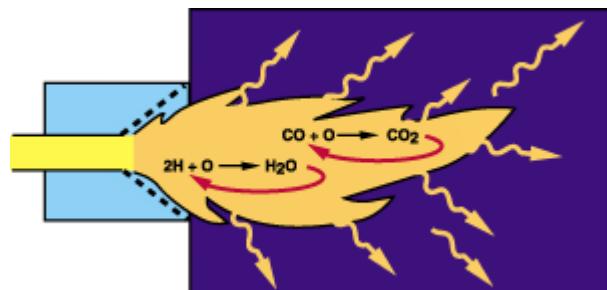


## Chemical equilibrium

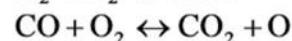
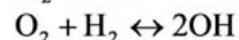
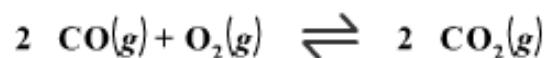
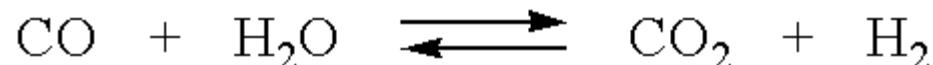
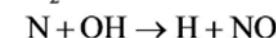
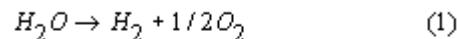


**Chemical equilibrium** is the state reached when the concentrations of the products and reactants **remain constant over time**. The mixture of reactants and products in the equilibrium state is the **equilibrium mixture**.

Usually temperatures are higher than 1250 K.....other species form through dissociation reactions

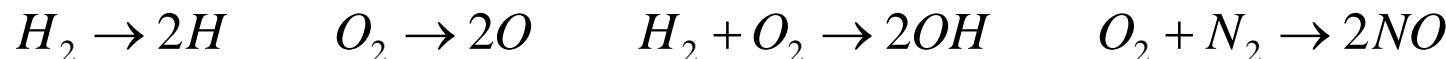


### Chemical Reactions



# Chemical Equilibrium

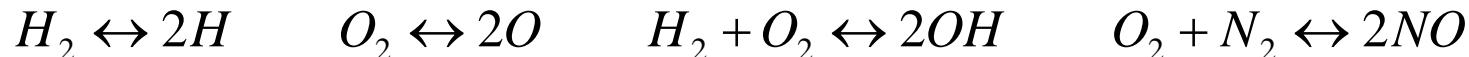
- In general the combustion products consist of more than just  $\text{CO}_2$ ,  $\text{H}_2\text{O}$  and  $\text{N}_2$
- For rich mixtures CO also exists in the products and at high temperatures the molecules dissociate to form H, O, OH, NO via the following reactions:



- The opposite direction reactions are also possible



- At **equilibrium** the rate of the forward reaction equals the rate of the backward reaction.



# Chemical equilibrium and 2<sup>nd</sup> law thermodynamics

$$\Delta S = \oint \frac{\partial Q}{T} + \sigma$$

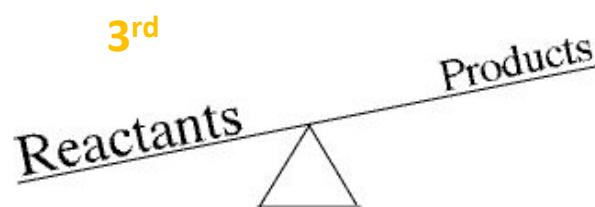
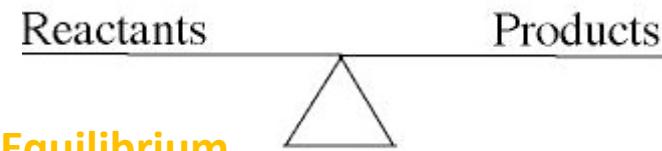
# $\sigma \geq 0$ entropy generation

T=control volume

# temperature

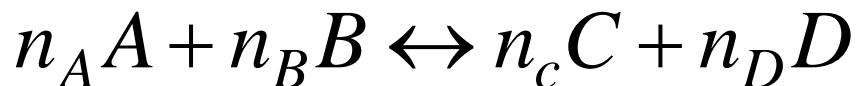
# G=H-TS Free Gibbs Energy

# Le chatelier



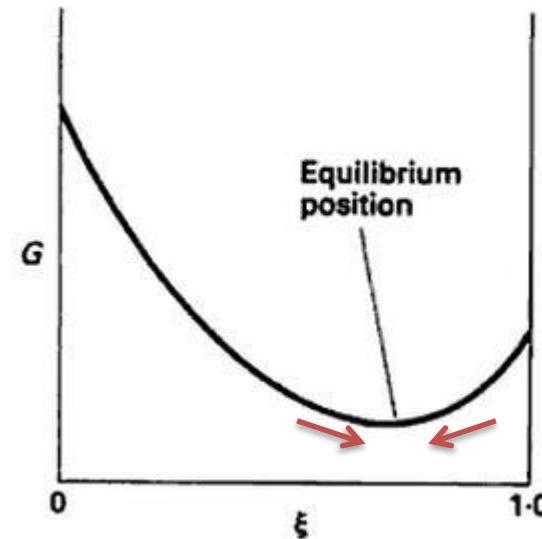
# Chemical Equilibrium

G=H-TS Free Gibbs Energy



@equilibrium, dG=0

$$K = \exp \left[ -\frac{\Delta G^0(T)}{RT} \right] = \frac{p_C^{nC} \cdot p_D^{nD}}{p_A^{nA} \cdot p_B^{nB}}$$



Le chatelier

- At equilibrium the relative proportion of the species mole fraction is fixed
- For the general equilibrium reaction



- The forward (f) reaction for species A, B TO TRANSFORM IN C, D and REVERSE (r) ratio is given by:

$$K_p \quad \frac{k_f}{k_r} = \exp \left[ -\frac{\Delta G^0(T)}{RT} \right] = \frac{p_C^{nC} \cdot p_D^{nD}}{p_A^{nA} \cdot p_B^{nB}}$$

**$K$  is the equilibrium constant**

**Kc**

$$kf(T) / kr(T) = \frac{X_C^{n_C} \cdot X_D^{n_D}}{X_A^{n_A} \cdot X_B^{n_B}}$$

Forward reaction

Reverse reaction

Note  $X_A = \frac{n_A}{n_A + n_B + n_C + n_D} = \text{concentration}$

$K$  is the **equilibrium constant**

$$K_p = K_c^* \left( \frac{RT}{P_{ref}} \right)^{n_{prod} - n_{reag}}$$

$$kf(T) / kr(T) = K_p(T) = \frac{X_C^{n_C} \cdot X_D^{n_D}}{X_A^{n_A} \cdot X_B^{n_B}} \left( \frac{P}{P_{ref}} \right)^{n_C + n_D - n_A - n_B}$$



  
 Forward reaction      Reverse reaction

Note  $X_A = \frac{n_A}{n_A + n_B + n_C + n_D} * p / RT = \text{concentration}$

mol/m<sup>3</sup>

**$K$  is the equilibrium constant**

**$Kn$**



Forward reaction

$$kf(T) / kr(T) = Kn(T) = \frac{n_C^{n_C} \cdot n_D^{n_D}}{n_A^{n_A} \cdot n_B^{n_B}}$$



Reverse reaction

$$K_p = K_c * \left( \frac{RT}{P_{ref}} \right)^{n_{prod} - n_{reag}} = K_n * \left( \frac{P}{n_{Total} P_{ref}} \right)^{n_{prod} - n_{reag}}$$

$K$  is the **equilibrium constant**

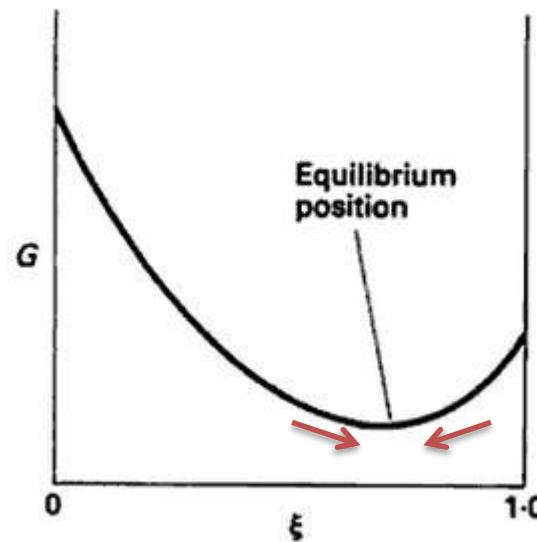
$$K_p = K_c * \left( \frac{RT}{P_{ref}} \right)^{n_{prod} - n_{reag}} = K_n * \left( \frac{P}{n_{Total} P_{ref}} \right)^{n_{prod} - n_{reag}}$$

P em bar

$G = H - TS$  Free Gibbs Energy

@equilibrium,  $dG = 0$

$$K = \exp \left[ -\frac{\Delta G^0(T)}{RT} \right] = \frac{p_A^{nA} \cdot p_B^{nB}}{p_C^{nC} \cdot p_D^{nD}}$$



Le chatelier

$K$  is tabulated as a function of temperature for different equilibrium reactions

## APÊNDICE 4 CONSTÂNTES DE EQUILÍBRIO

T (K)	$\log_{10} K_p$ com as pressões parciais em atmosferas							
	$\frac{P_{H_2O}}{P_{H_2} \sqrt{P_{O_2}}}$	$\frac{P_{CO_2}}{P_{CO} \sqrt{P_{O_2}}}$	$\frac{(P_{H_2O})(P_{CO})}{(P_{H_2})(P_{CO_2})}$	$\frac{P_{H_2O}}{P_{OH} \sqrt{P_{H_2}}}$	$\frac{P_{NO}}{\sqrt{P_{O_2} \sqrt{P_{N_2}}}}$	$\frac{P_{H_2}}{(P_H)^2}$	$\frac{P_{O_2}}{(P_O)^2}$	$\frac{P_{N_2}}{(P_N)^2}$
298	40,048	45,066	-5,018	46,181	-15,171	71,232	81,202	159,600
300	39,786	44,760	-4,974	45,876	-15,073	70,762	80,664	158,578
400	29,240	32,431	-3,191	33,600	-11,142	51,758	58,944	117,408
600	18,633	20,087	-1,454	21,264	-7,210	32,676	37,146	76,162
800	13,289	13,916	-0,627	15,060	-5,243	23,082	26,202	55,488
1000	10,062	10,221	-0,159	11,322	-4,062	17,294	19,612	43,056
1200	7,899	7,764	0,135	8,822	-3,275	13,416	15,208	34,754
1400	6,347	6,014	0,333	7,030	-2,712	10,632	12,054	28,812
1600	5,180	4,706	0,474	5,686	-2,290	8,534	9,684	24,350
1800	4,270	3,693	0,577	4,638	-1,962	6,896	7,836	20,874
2000	3,540	2,884	0,656	3,799	-1,699	5,582	6,356	18,092
2200	2,942	2,226	0,716	3,113	-1,484	4,504	5,142	15,810
2400	2,443	1,679	0,764	2,541	-1,305	3,602	4,130	13,908

Tabela A4.1

Constantes de equilíbrio. (Dados extraídos de Rogers e Mayhew, 1994.) (continua)

## Chemical equilibrium

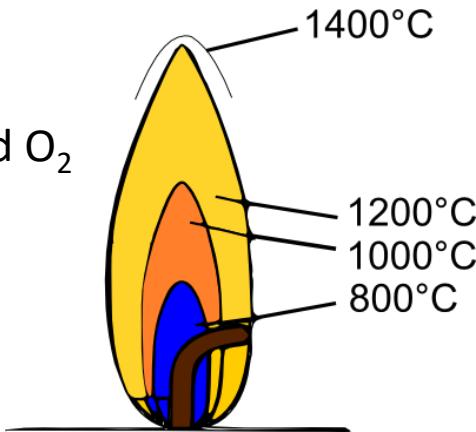
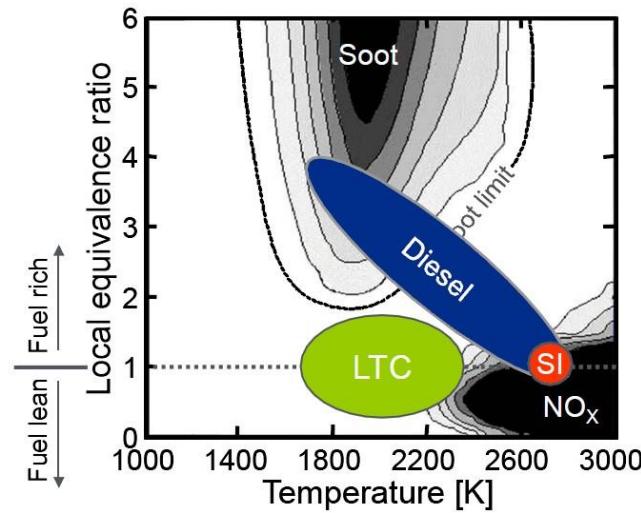
$T < 1250\text{ K}$

$\lambda >= 1$   
(stoichiometric/poor)

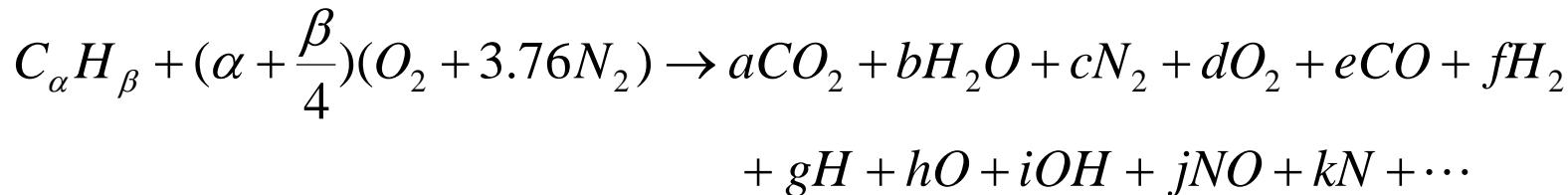
$\Rightarrow$  Complete combustion

Stable chemical species:  $\text{CO}_2$ ,  $\text{H}_2\text{O}$ ,  $\text{N}_2$  and  $\text{O}_2$

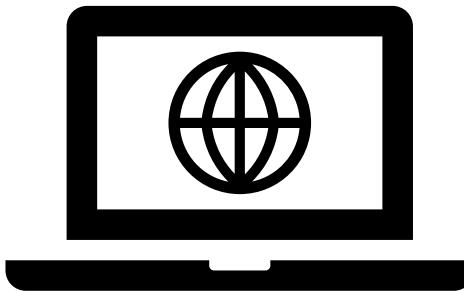
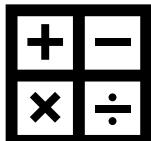
Usually temperatures are higher than 1250 K.....e.g.



- If the products are at high temperature (>2000 K) minor species will be present due to the dissociation of the major species CO<sub>2</sub>, H<sub>2</sub>O, N<sub>2</sub> and O<sub>2</sub>.



- Hand calculations are not practical when many species are considered, one uses a computer program to calculate product equilibrium composition.





**TITLE AND SUBTITLE:**

Computer Program for Calculation of Complex Chemical Equilibrium Compositions and Applications II. User's Manual and Program Description

**AUTHOR(S):**

Bonnie J. McBride and Sanford Gordon

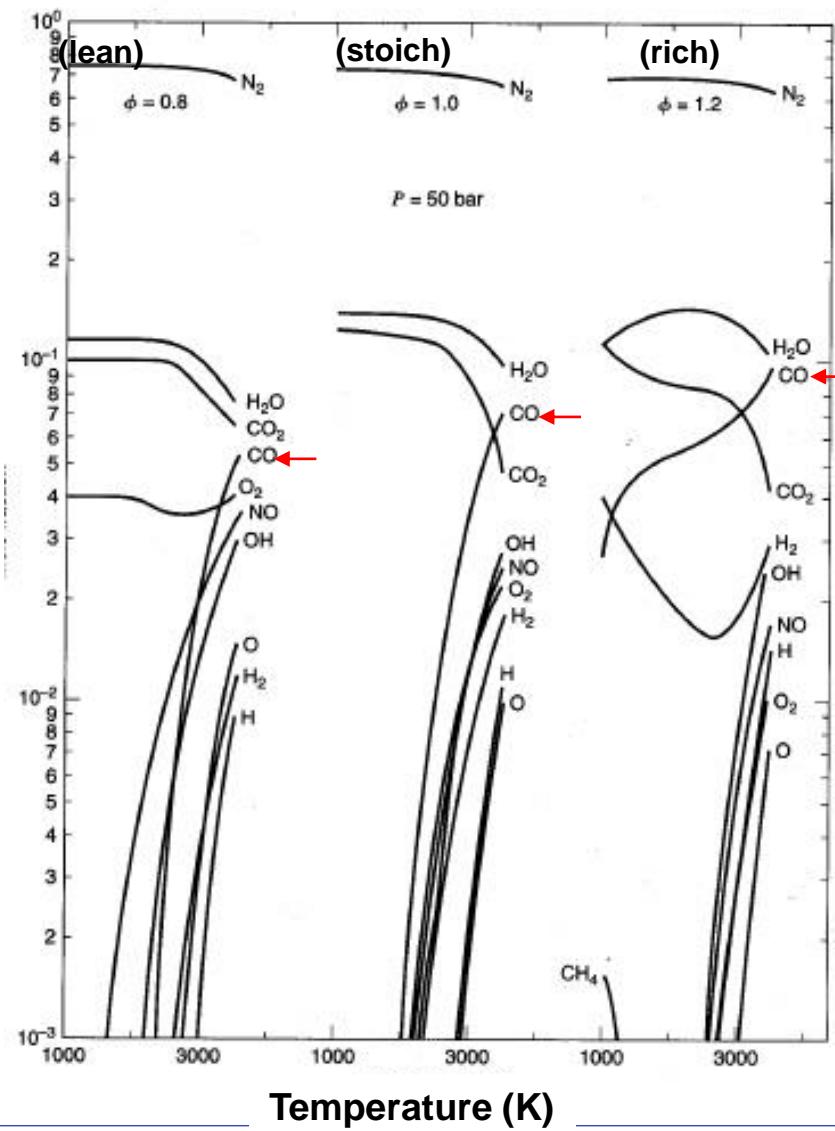
**REPORT DATE:**

June 1996

# Composition of Octane-air Mixtures at Equilibrium

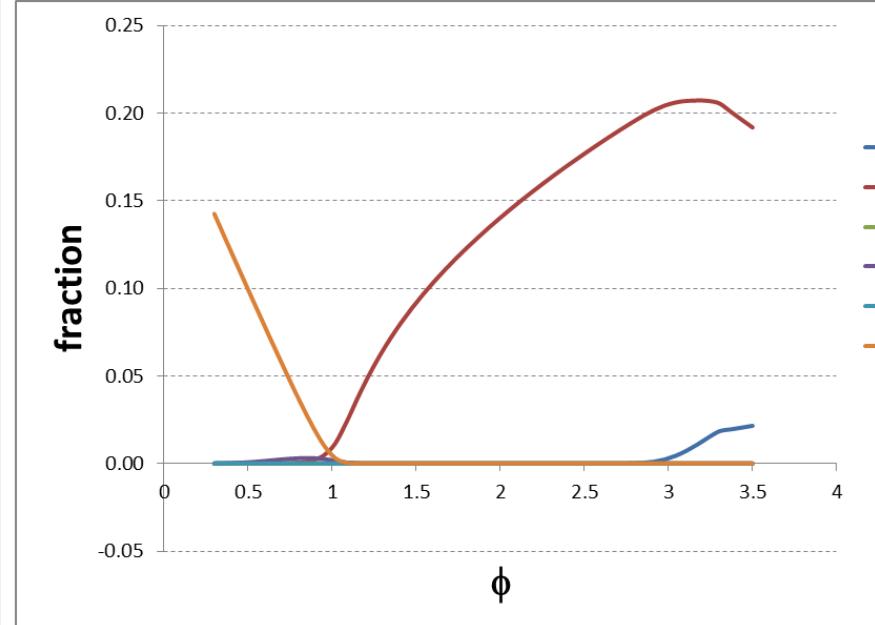
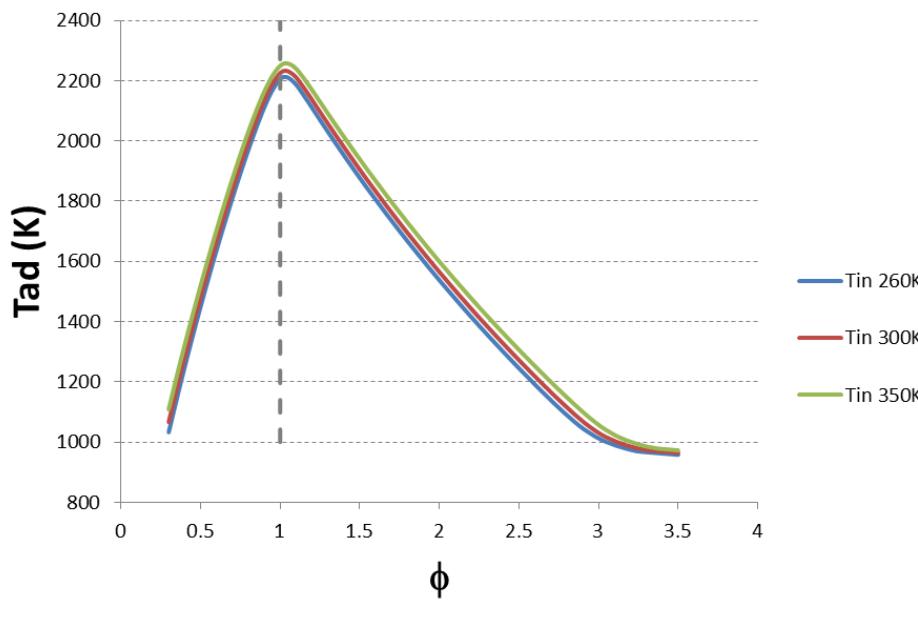
C8H18

Mole fraction of each species

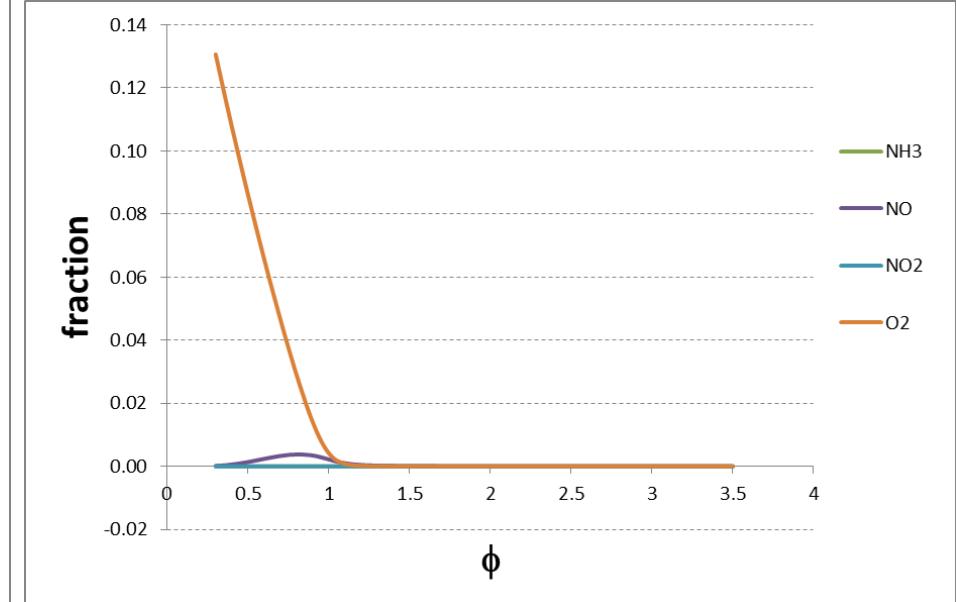
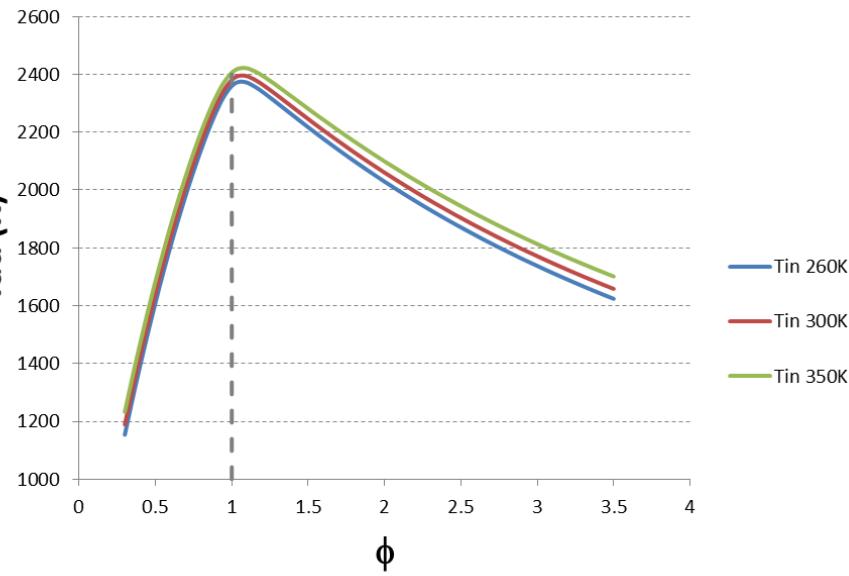




[http://www.cantera.org/docs/sphinx/html/cython/examples/multiphase\\_adiabatic.html](http://www.cantera.org/docs/sphinx/html/cython/examples/multiphase_adiabatic.html)



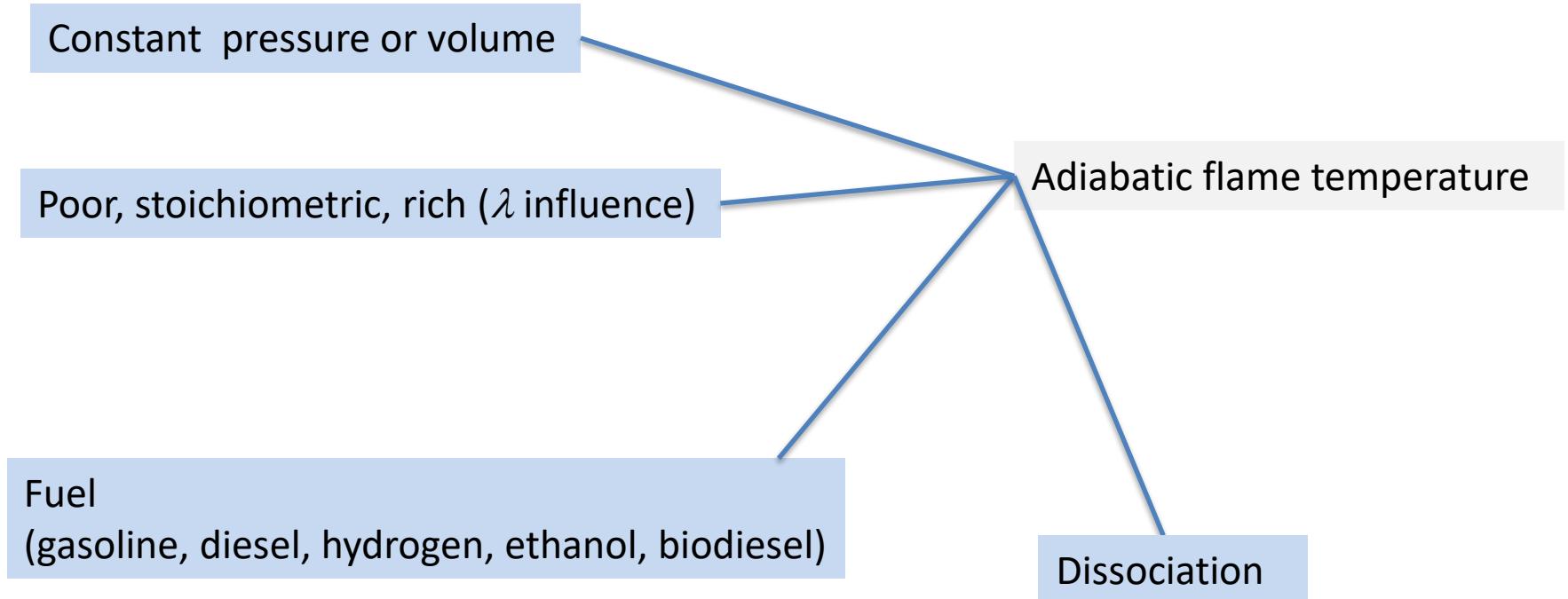
[http://www.cantera.org/docs/sphinx/html/cython/examples/multiphase\\_adiabatic.html](http://www.cantera.org/docs/sphinx/html/cython/examples/multiphase_adiabatic.html)



[http://www.cantera.org/docs/sphinx/html/cython/examples/multiphase\\_adiabatic.html](http://www.cantera.org/docs/sphinx/html/cython/examples/multiphase_adiabatic.html)

P#8 Consider the stoichiometric combustion of methane ( $\text{CH}_4$ ) at standard conditions with dissociation. Assume the following species in equilibrium  $\text{CO}_2$ ,  $\text{H}_2\text{O}$ ,  $\text{O}_2$ ,  $\text{CO}$ ,  $\text{H}_2$  e  $\text{N}_2$

- Compute the chemical equilibrium concentrations at 2000 K.
- Compute the adiabatic flame temperature and compare with the adiabatic flame temperature without dissociation.



# Adiabatic???

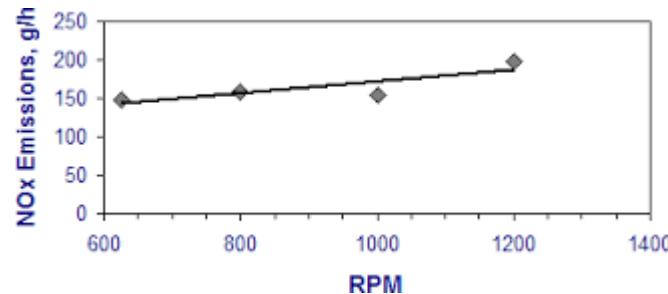
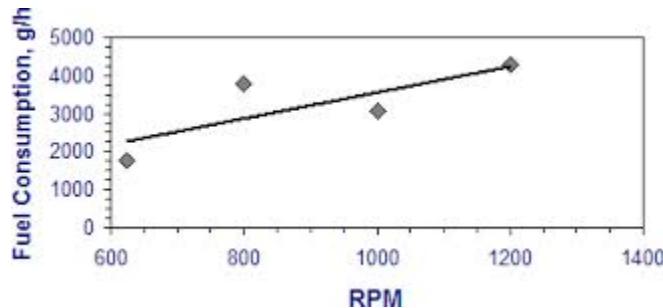
Combustion reactions generally occur very fast ~ 1ms



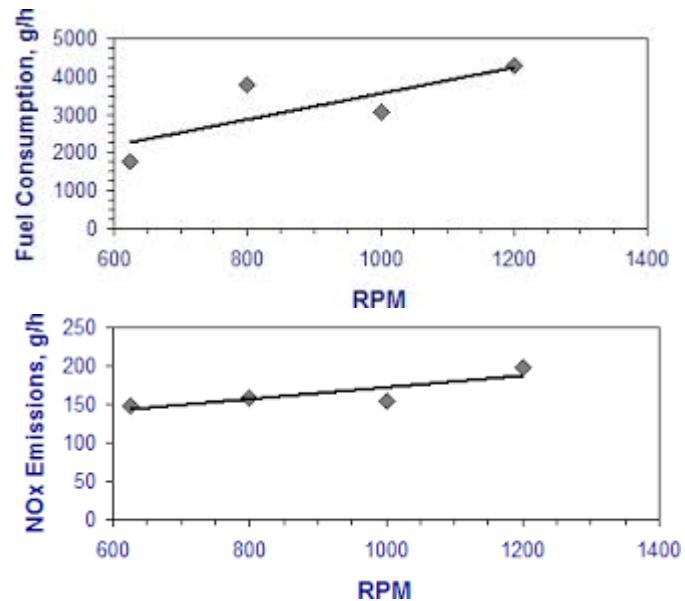
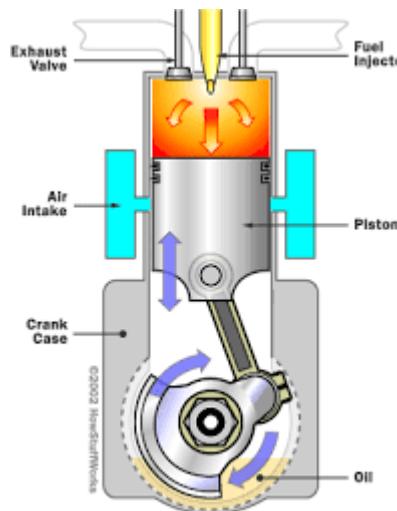
Little heat or work transfer takes place



Maximum temperature achieved is often near  $T_{ad}$



# Adiabatic???

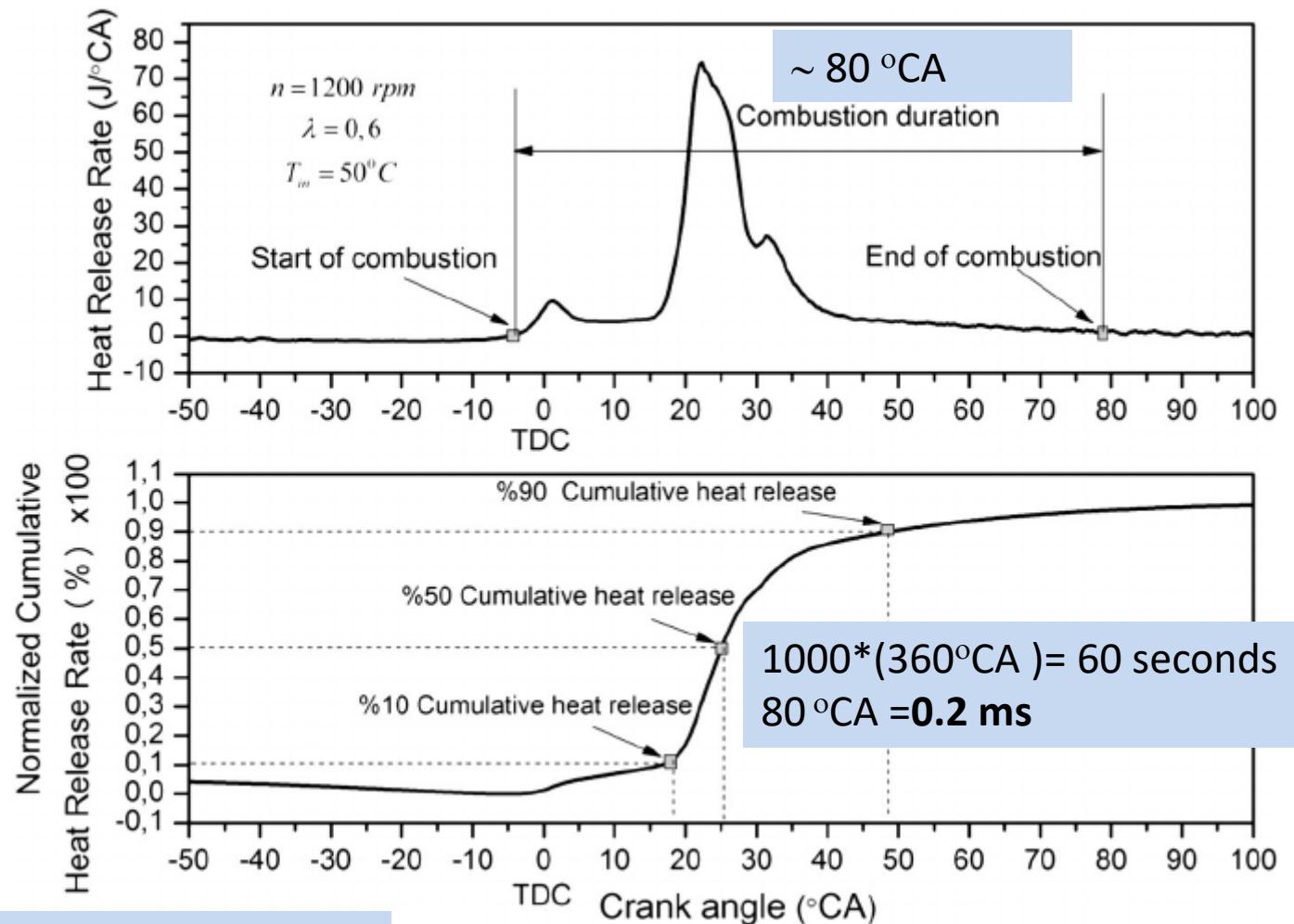
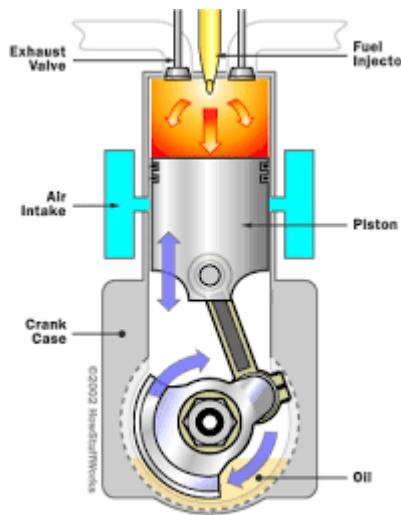


1000 rpm = 1000 revolutions per minute

1 revolution is  $360^\circ\text{CA}$  (Crank angle)

$1000 * (360^\circ\text{CA}) = 60 \text{ seconds}$

# Adiabatic???



**More rpm, less combustion time!!!**

NO<sub>x</sub> means the sum of NO and NO<sub>2</sub> contents in flue gas recalculated on NO<sub>2</sub>

NO<sub>x</sub> = NO + NO<sub>2</sub> (expressed in NO<sub>2</sub>)

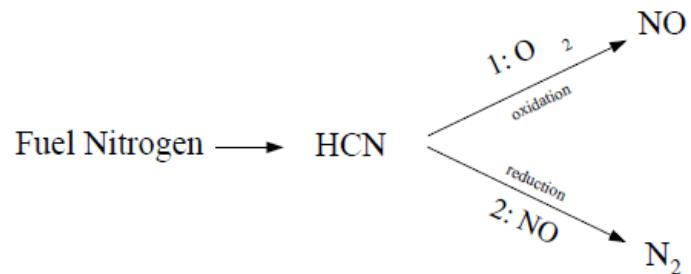
$$\text{NO}_x \text{ [ppm]} = \text{NO} \text{ [ppm]} + \text{NO}_2 \text{ [ppm]}$$

The NOx content in the combustion gases from conventional power plant boilers and many industrial heating process contains some **90 % NO** with the remainder NO<sub>2</sub>

- **THERMAL NITRIC OXIDE MECHANISM is usually the most important**
- **Fuel NOx**
- **Prompt NOx**

- Prompt NOx
- Fuel NOx
- **THERMAL NITRIC OXIDE MECHANISM is usually the most important**

**Prompt NOx:** Formed in the flame zone through intermediate formation of hydrogen cyanide (HCN) followed by a subsequent oxidation of HCN to NO



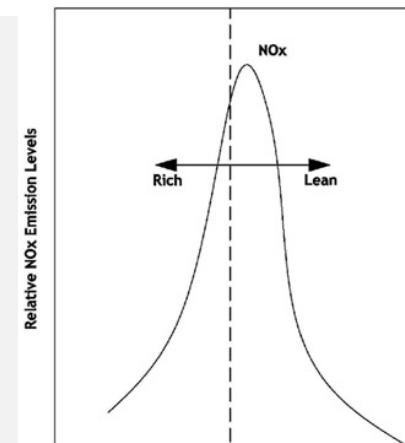
**Fuel NOx:** Nitrogen accounts for about 1.5 wt% of most coals.

	Low Rank		High Rank	
<b>Rank:</b>	Lignite	Subbituminous	Bituminous	Anthracite
<b>Age:</b>			increases	
<b>% Carbon:</b>	65-72	72-76	76-90	90-95
<b>% Hydrogen:</b>	~5		decreases	~2
<b>% Nitrogen:</b>	<~1	~1-2		
<b>% Oxygen:</b>	~30		decreases	~1
<b>% Sulfur:</b>	~0	increases	~4	decreases ~0
<b>% Water:</b>	70-30	30-10	10-5	~5
<b>Heating value (BTU/lb):</b>	~7000	~10,000	12,000-15,000	~15,000

FIGURE 7-3. Variation of selected coal properties with coal rank.

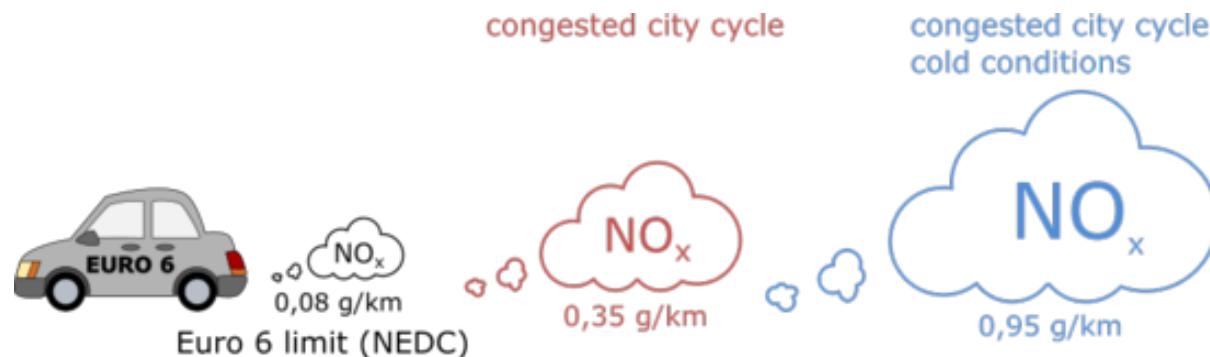
@<http://www.ems.psu.edu/~radovic/Chapter7.pdf>

Impact of Pulverizer Performance on Nitrous Oxide Emissions

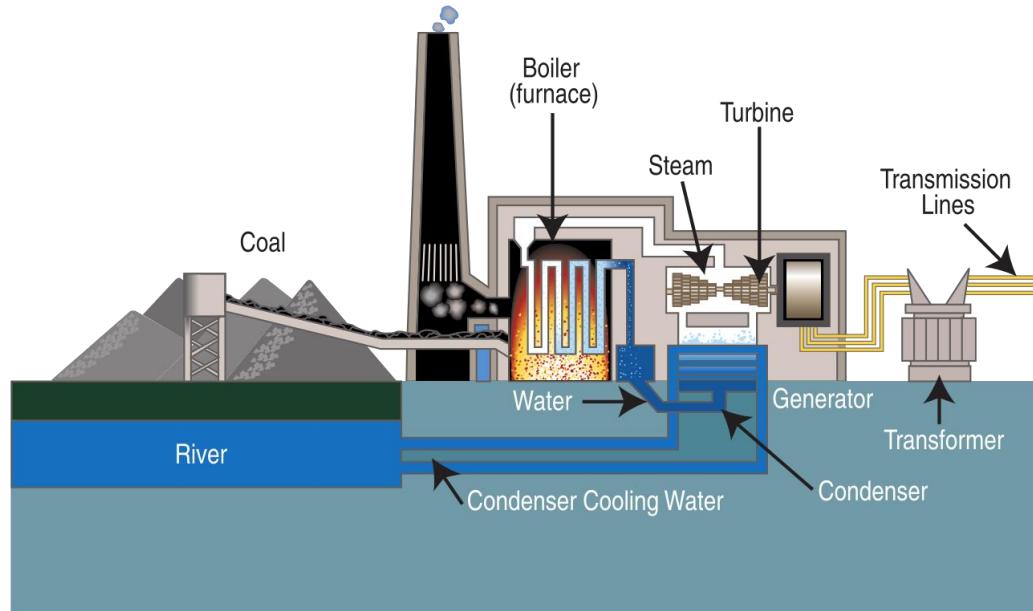
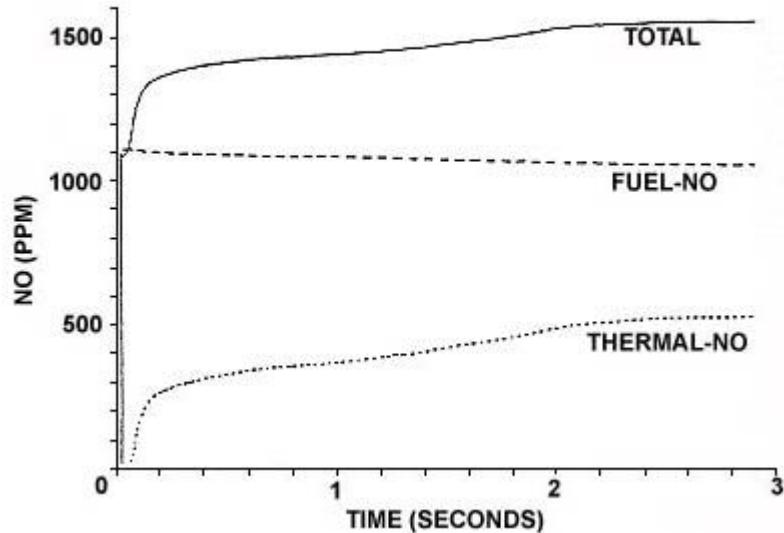


*The conversion of fuel N is weakly temperature dependent but depends strongly upon local burner stoichiometry.*

**Thermal NO<sub>x</sub>:** The three principal reactions (the extended Zeldovich mechanism) producing thermal NO<sub>x</sub> are:



## NO<sub>x</sub> formation in a coal-fired boiler



ppm ☺ !!!!

# EGR influence Emissions

## Exhaust gas recirculation and aftertreatment (lean combustion)

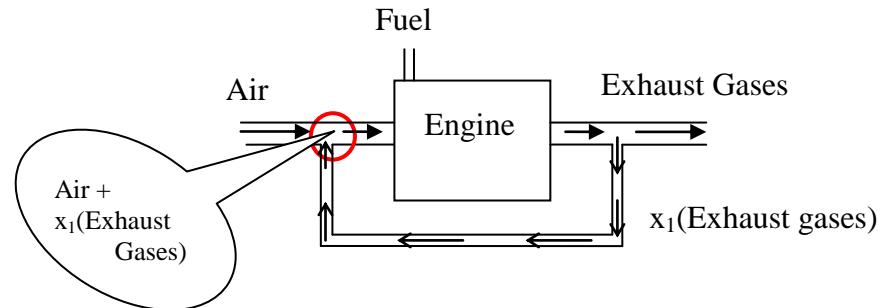
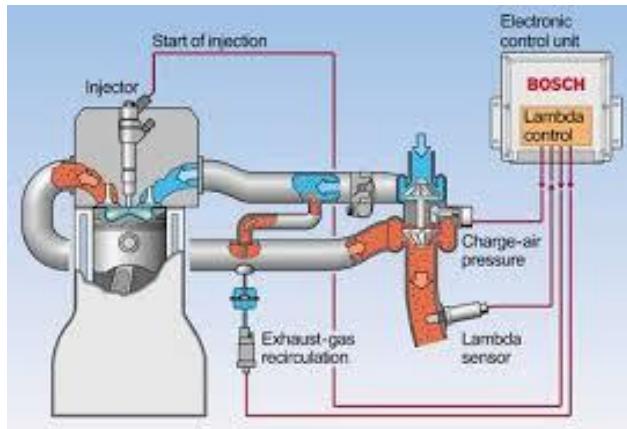
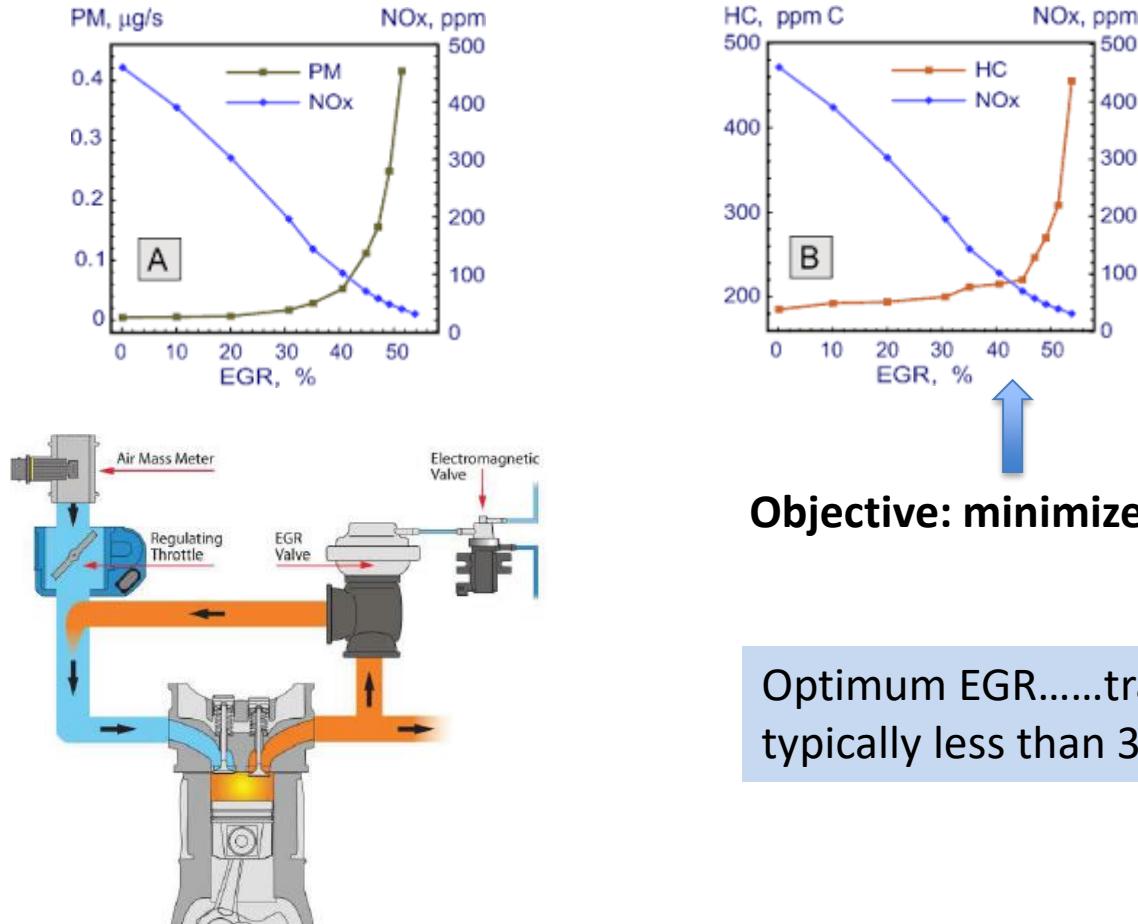


Figure 2: Exhaust Gas Re-circulation

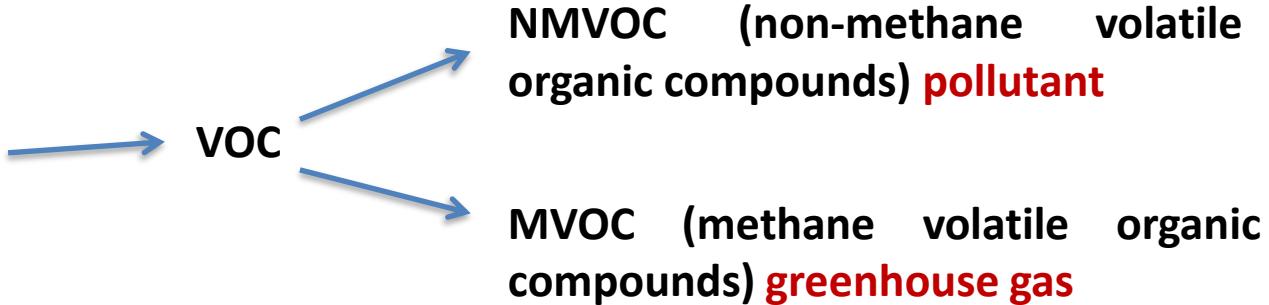


# EGR influence Emissions

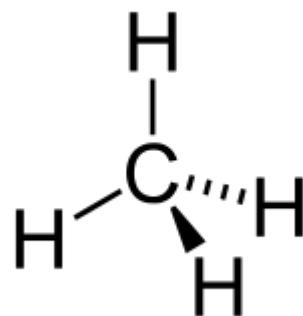
## Exhaust gas recirculation and aftertreatment



Unburned hydrocarbons included in



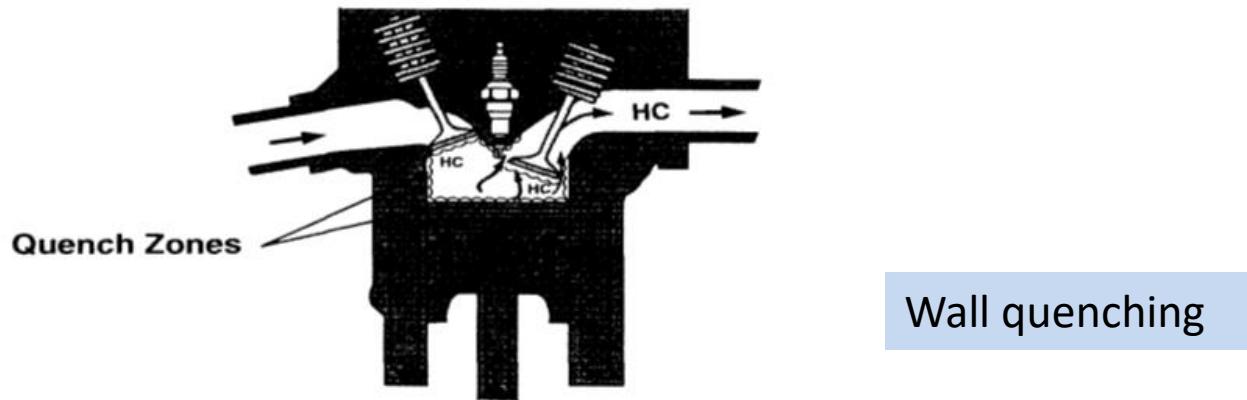
Organic compounds are a class of complex molecules that are characterized by their use of carbon as a molecular backbone



## Unburned hydrocarbons

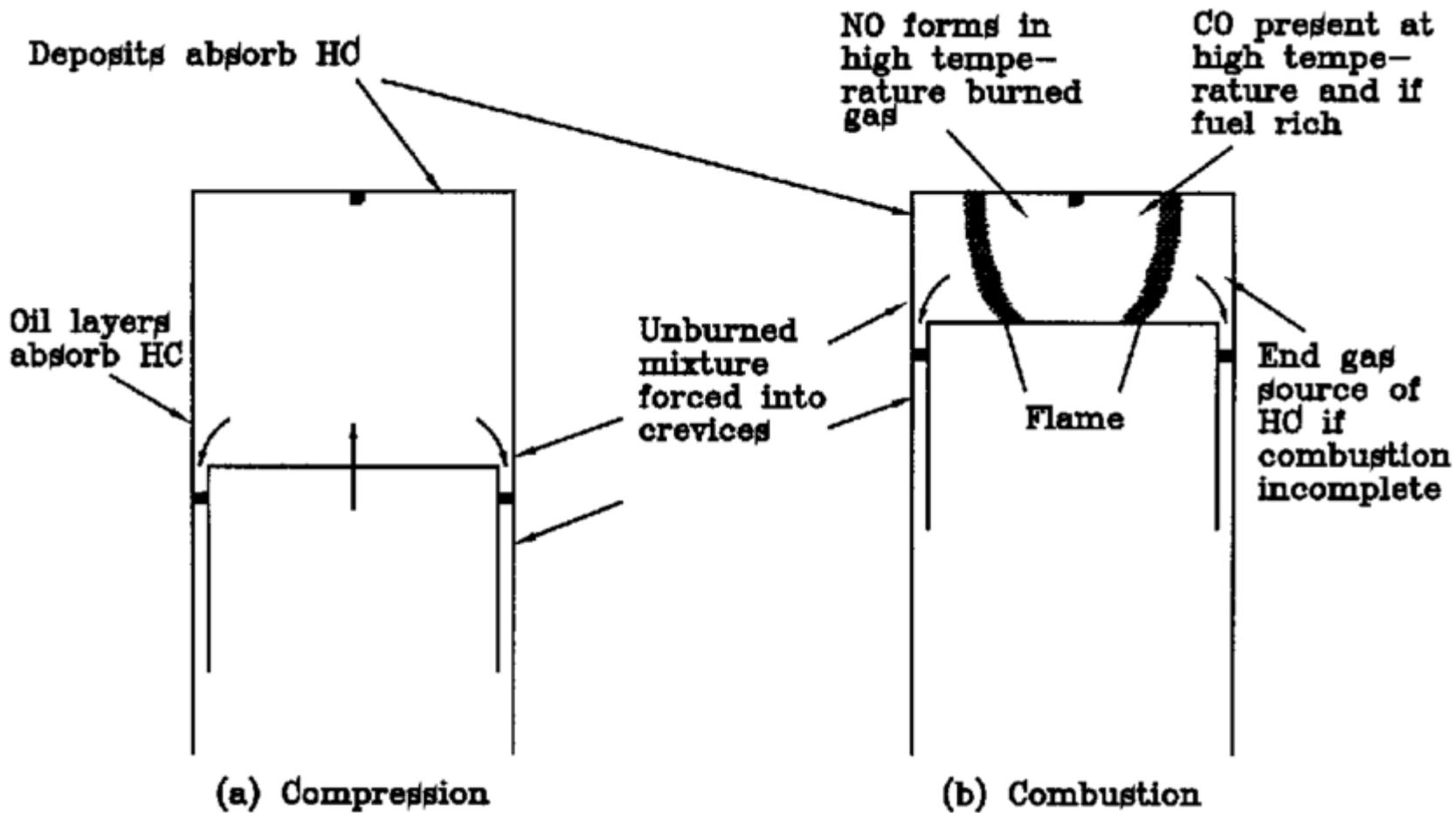
### **"Quenching"**

Quenching occurs when the combustion flame-front is extinguished before all the fuel is burned.

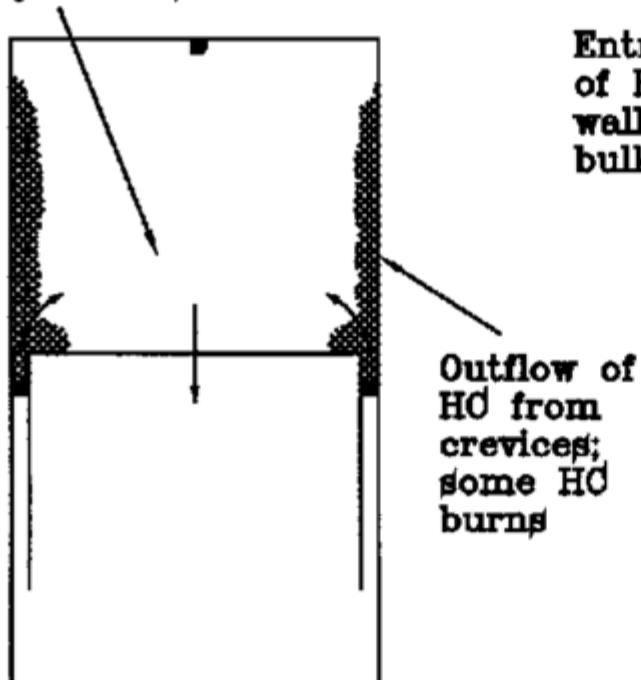


Wall quenching

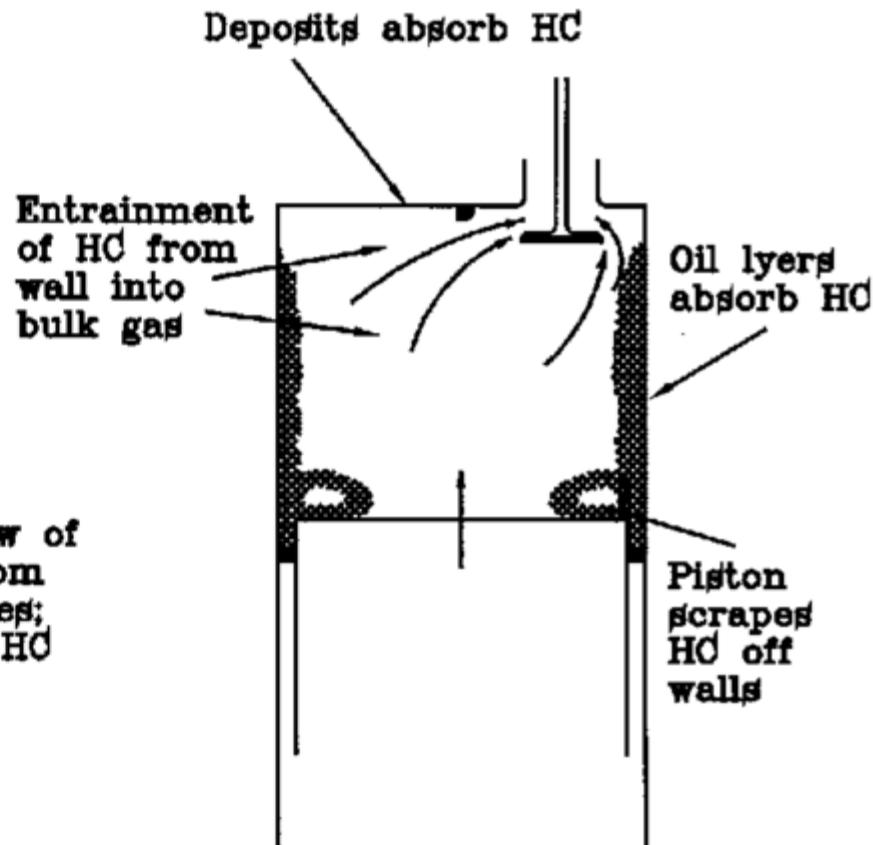
# HC Emissions



As burned gases cool,  
first NO chemistry, then  
CO chemistry freezes



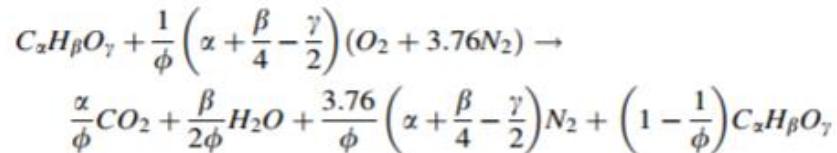
(c) Expansion



(d) Exhaust

# Emissions

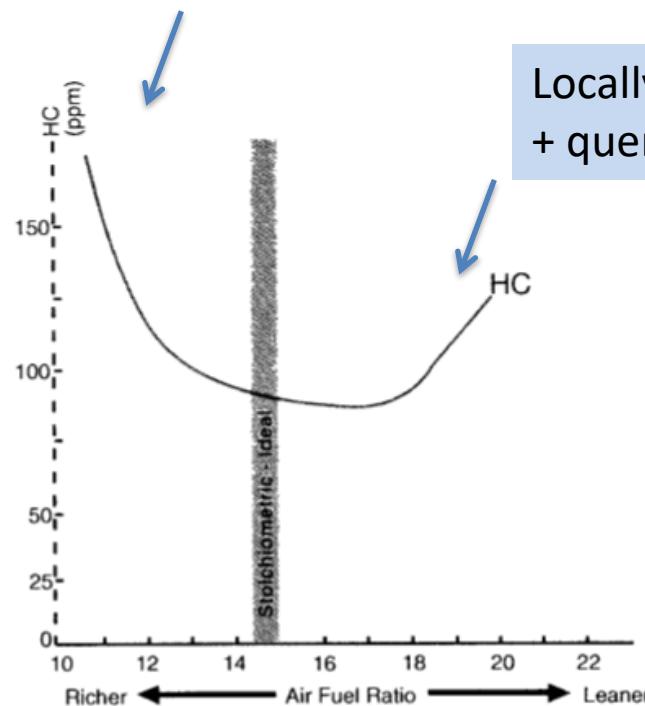
No air enough  
+quenching



**Effects of A/F Ratio  
on Exhaust HC**

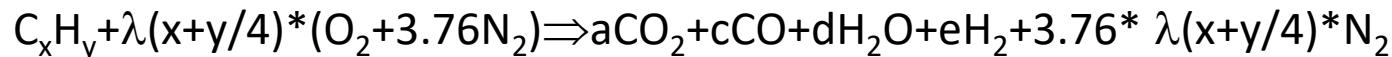
As shown, exhaust HC production is lowest when A/F ratio is slightly leaner than "ideal"; however, HC's increases dramatically when the mixture becomes too rich or too lean to the point of misfire.

Locally no air enough  
+ quenching



## CO emissions – carbon monoxide

$\lambda < 1$ , rich conditions possible equation

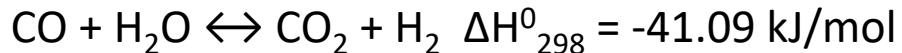


How many unknowns: **4**

From mass balance: **3 equations**

Use equilibrium reaction: water-gas shift equation and then **4 equations 4 unknowns**

Water-gas shift reaction (WGS)



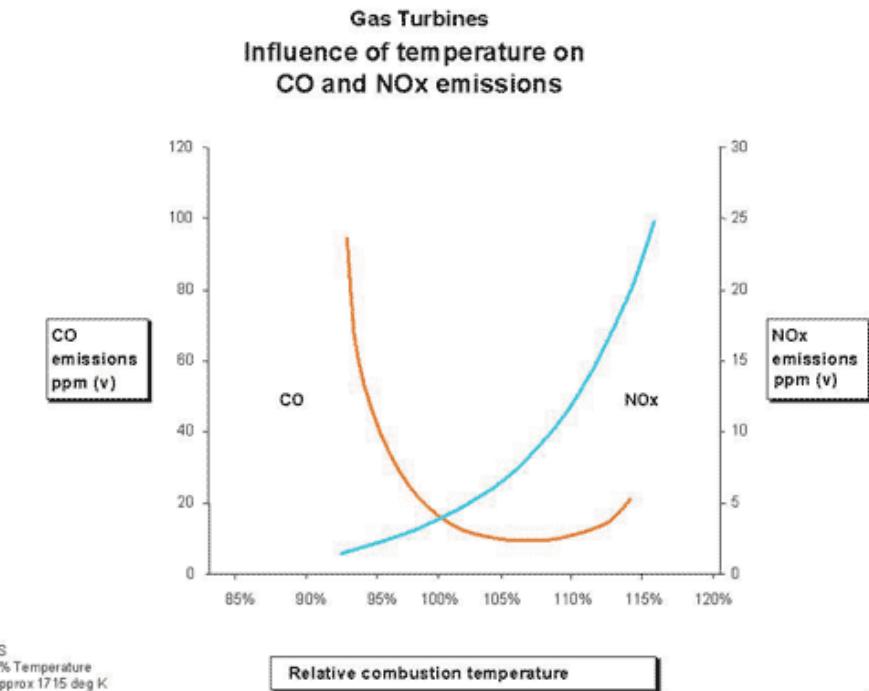
Low temperatures favours forward reaction



High temperatures favours reverse reaction

## Le Chatelier

$K_{\text{eq}} = k_f/k_r < 1$  the system tends to increase forward reaction

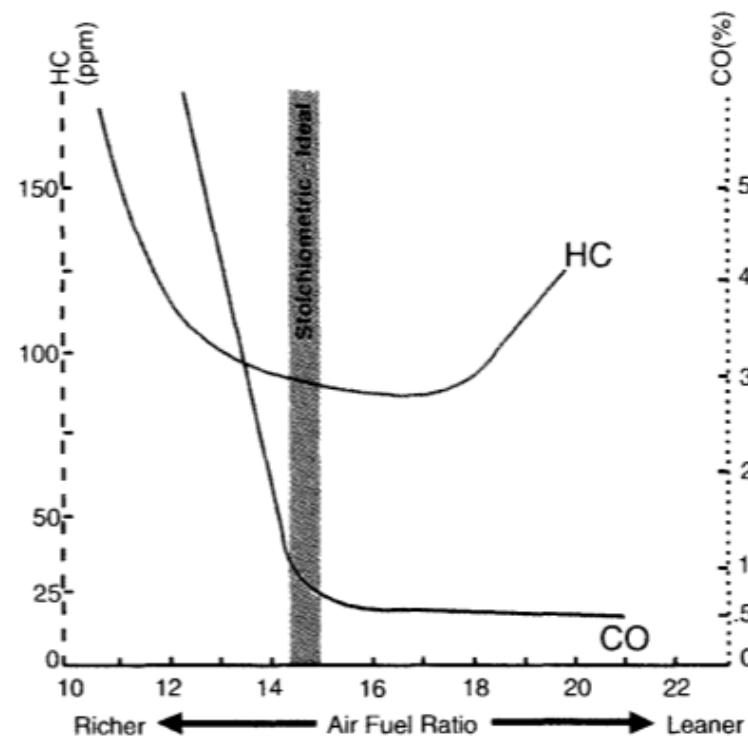


## CO emissions – carbon monoxide

$\lambda \ll 1$ , rich conditions e.g. quenching

### **Effects of A/F Ratio on Exhaust CO**

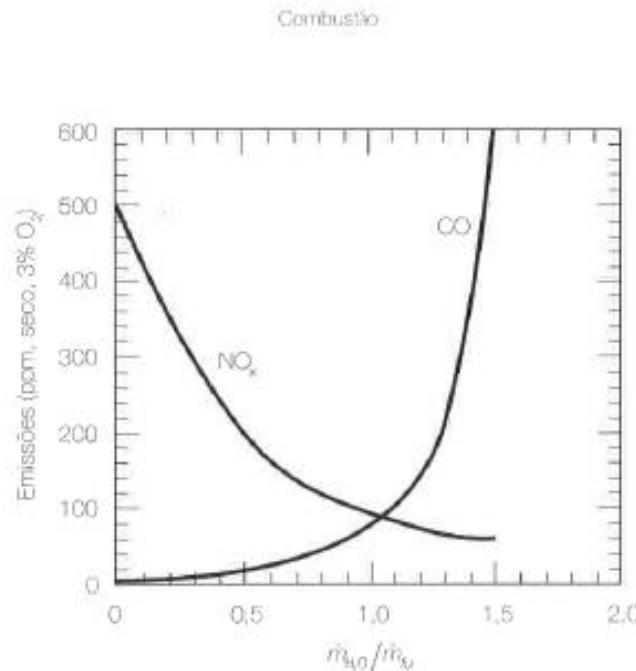
Exhaust CO is lowest when A/F ratio is leaner than "ideal"; however, CO increases dramatically with richer mixtures.



## Trade-off NOx / CO

CAPÍTULO 12

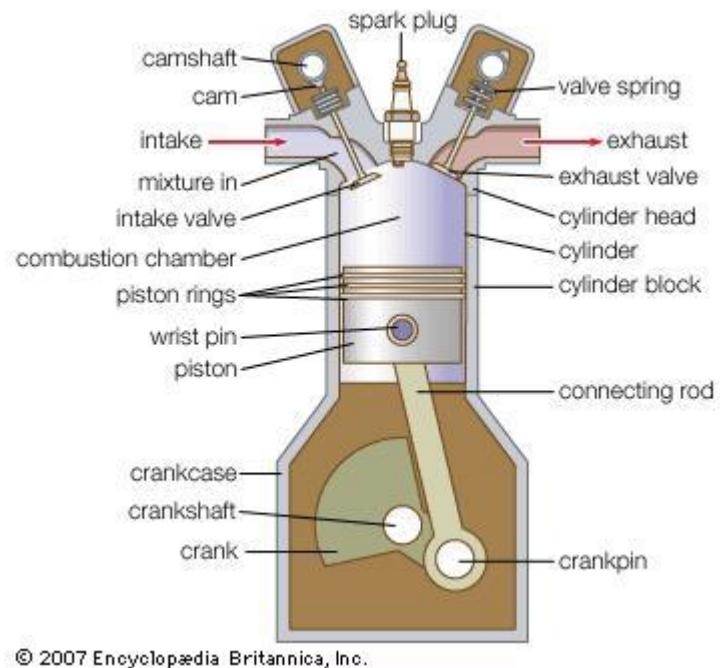
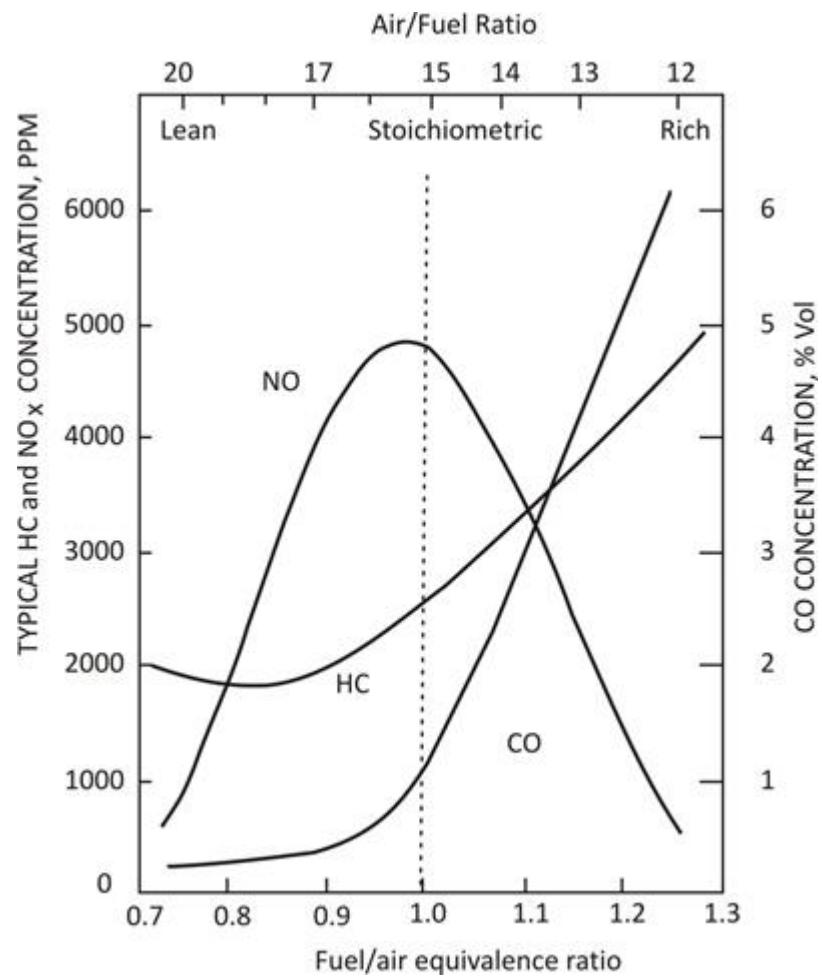
**Figura 12.8**  
Efeito da injeção de água nas emissões de NO<sub>x</sub> e CO de turbinas a gás industriais. (Extraído de Bowman, 1992.)



Effect of water injection industrial turbines

Typically lowering NOx imply increase other emissions

# NO<sub>x</sub>, HC and CO

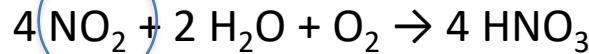
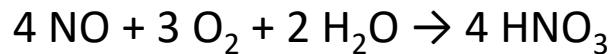


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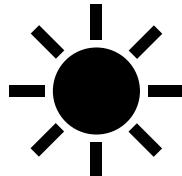
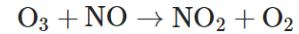
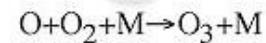
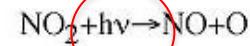
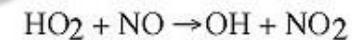
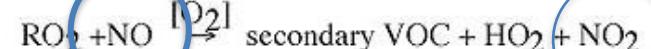
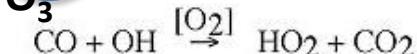
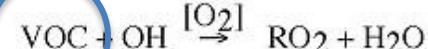
$$\phi = \frac{1}{\lambda}$$

## Problem: acid rain or smog (smoke+fog) problems

Nitric acid  $\text{HNO}_3$



Tropospheric ozone  $\text{O}_3$



## Problem: smog (smoke+fog) Shenzhen, China



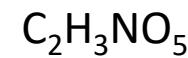
Aldehydes

Nitrogen oxides particularly nitric oxide and nitrogen oxide

Peroxyacetyl nitrate (PAN)

Tropospheric ozone

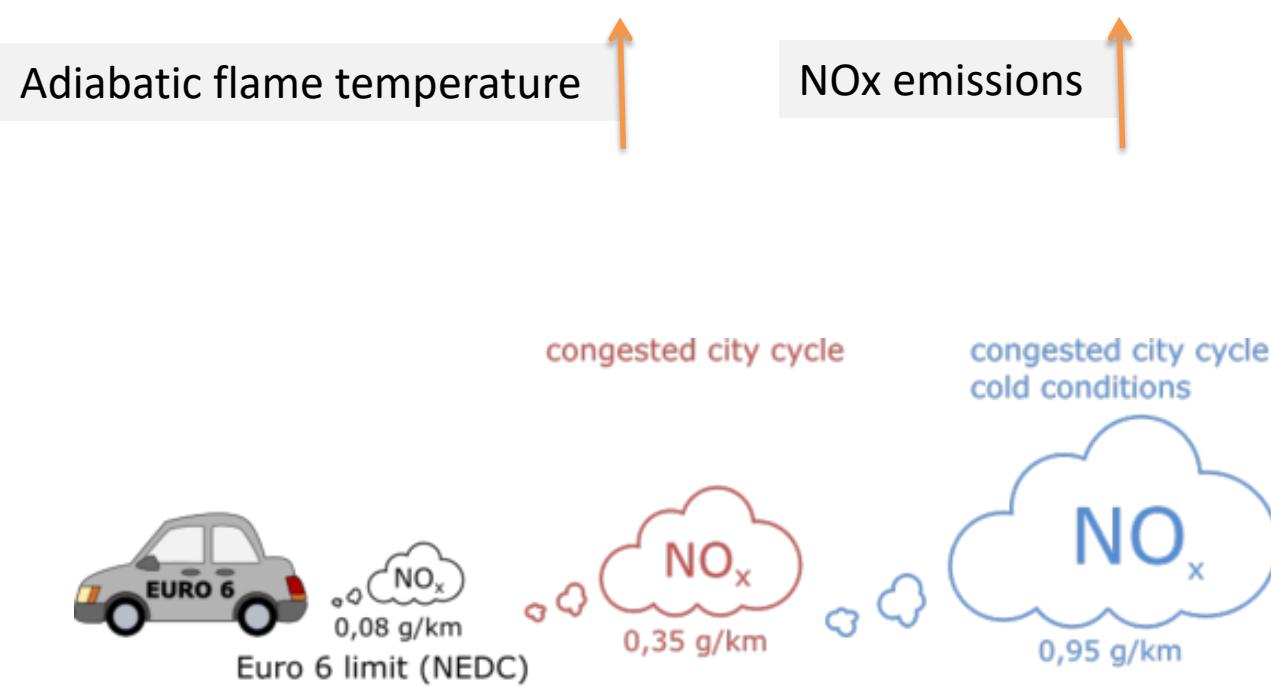
Volatile organic compound



(PAN)

$\text{O}_3$  (Main)

VOC



P#9 Consider the combustion of C<sub>7</sub>H<sub>14</sub> (~diesel). Determine the emission concentration of CO (ppm) in both cases.

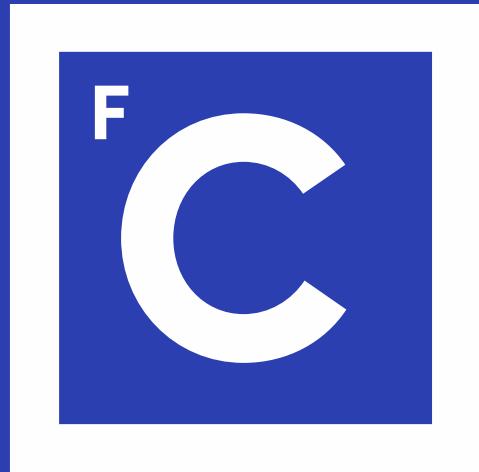
- a) At 1200 K and 10 atm with A/F=40;
- b) At 2400 K, 40% of theoretical stoichiometric air.

P#10 Following table list the results of an experiment of boiler that is used to produce superheated vapour. The boiler is feed by natural gas trough a conventional burner.

- a) The air/fuel ratio
- b) The higher heating value of the fuel
- c) Heat transfer to water, assuming that heat loss trough boiler walls are 3% of the lower heating value.

Fuel rate	150 m <sup>3</sup> /h
Reactants temperature@ entrance	25°C
Products temperature @exit	227°C
Fuel composition by volume(%)	CH <sub>4</sub> : 88 H <sub>2</sub> : 2 CO <sub>2</sub> : 3 N <sub>2</sub> : 7
Dry analysis combustion products (%)	O <sub>2</sub> : 1.1 CO <sub>2</sub> : 10.8 N <sub>2</sub> : 88.1

Obrigado



# Ciências ULisboa

Faculdade  
de Ciências  
da Universidade  
de Lisboa