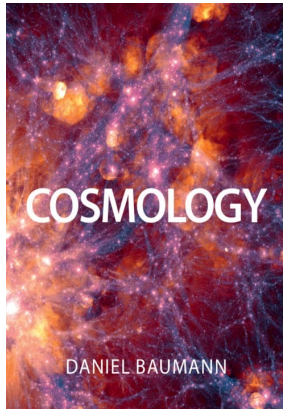# Universo Primitivo
2025-2026 (1º Semestre)

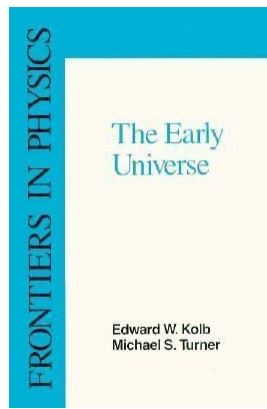**Mestrado em Física - Astronomia**

Chapter 6

6   Big Bang Nucleosynthesis

- Initial Conditions;

- Nuclear statistical equilibrium;

- Neutron abundance;
- Helium abundance ;
- Comparison with observations
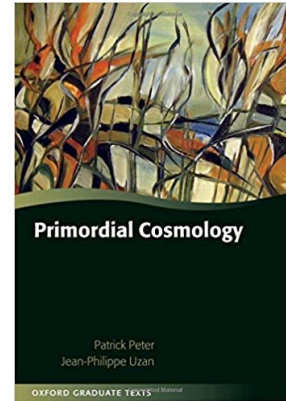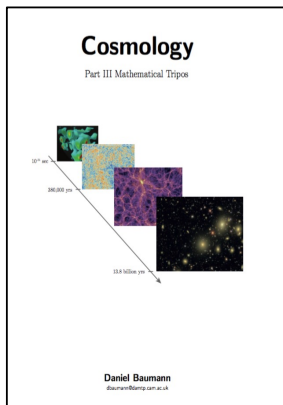- BBN as a probe of cosmology and fundamental physics
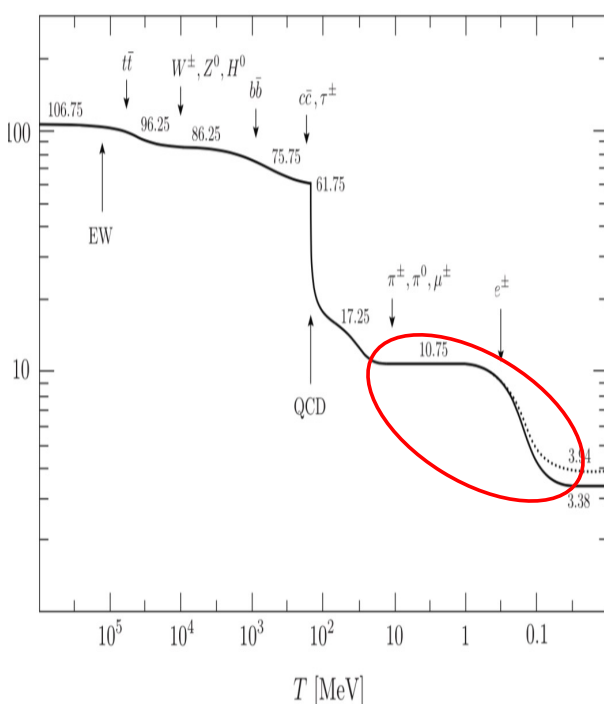
References

Ch. 3.2.4

Ch. 4

Ch. 4.3

Ch. 3.3

Big-Bang Nucleosynthesis

Initial conditions

After QCD phase transition and $T \gtrsim 1$ MeV protons and neutrons…

* remain in equilibrium with the fluid mostly due to weak interactions involving neutrinos.
* First atomic nuclei may form in equilibrium via 2-body nuclear reactions between protons + neutrons
* The proton to neutron ratio is $n/p = n^{eq}/p^{eq}$

By $T \sim 1 - 0.7$ MeV,
* weak interactions can no longer keep protons and neutrons in equilibrium
* <u>Free neutrons tend to decay into protons</u> by $T/MeV \sim 0.8$, while atomic nuclei remain in equilibrium (due to the electromagnetic interaction)
* Neutrinos also decouple; n/p starts to deviate from the equilibrium value, $n/p \neq n^{eq}/p^{eq}$
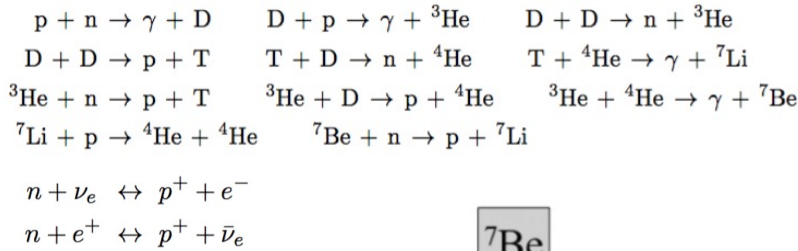
By $T \sim 0.7 - 0.5$ MeV,
* The production of deuterium, $n + p \rightarrow D + \gamma$, ceases when the number of neutrons decrease.
* Light atomic nuclei are then consistently formed by 2-body reaction involving deuterium nuclei (3 body reactions are very unlikely).
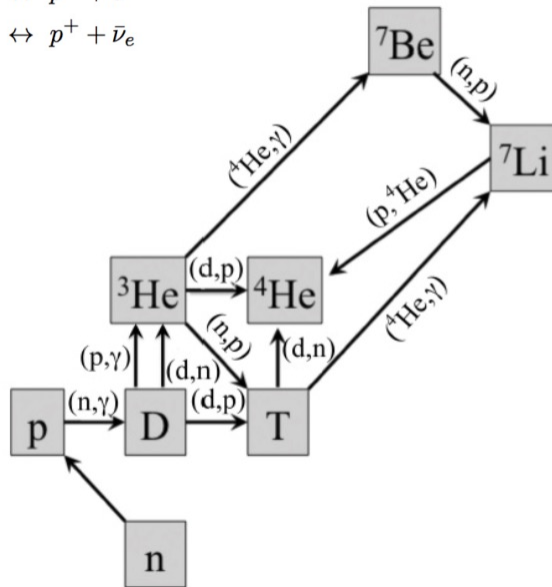
Big-Bang Nucleosynthesis

Initial conditions

$$p + n \rightarrow \gamma + D \qquad D + p \rightarrow \gamma + {}^3He \qquad D + D \rightarrow n + {}^3He$$
$$D + D \rightarrow p + T \qquad T + D \rightarrow n + {}^4He \qquad T + {}^4He \rightarrow \gamma + {}^7Li$$
$${}^3He + n \rightarrow p + T \qquad {}^3He + D \rightarrow p + {}^4He \qquad {}^3He + {}^4He \rightarrow \gamma + {}^7Be$$
$${}^7Li + p \rightarrow {}^4He + {}^4He \qquad {}^7Be + n \rightarrow p + {}^7Li$$

$$n + \nu_e \leftrightarrow p^+ + e^-$$
$$n + e^+ \leftrightarrow p^+ + \bar{\nu}_e$$

Main nuclear reactions that can be establish during this phase

Big-Bang Nucleosynthesis (BBN) is able to predict the observed abundances of light elements!

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

Let us assume a given atomic nucleus $A = n + p$ nucleons (A is the **nuclear mass number**, n is the number of neutrons, and p is the number of protons of the nucleus. The nuclear charge is given by the **atomic number** $Z = p$.

The number density of this **nuclear species** at equilibrium is given by the non-relativistic expression derived in Series 2 (exercise 5.1):

$$n_A = g_A \left(\frac{m_A T}{2\pi} \right)^{3/2} \exp\left(\frac{\mu_A - m_A}{T} \right)$$

where the chemical potential needs to account for the number of protons and neutrons that make up the nucleus

$$\mu_A = Z\mu_p + (A - Z)\mu_n$$

We can also write similar equations to the free (non-relativistic) protons and neutrons, noticing that both these particles have 2 degrees of freedom (spin).

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

i.e., **neutrons and protons have also non-relativistic equilibrium densities** given by the previous expression ($A = 1$, $g_A = 2$) :

$$n_n = 2\left(\frac{m_n T}{2\pi}\right)^{3/2} e^{-(m_n - \mu_n)/T}$$

$$n_p = 2\left(\frac{m_p T}{2\pi}\right)^{3/2} e^{-(m_p - \mu_p)/T}.$$

The **nuclear binding energy**, B_A, of a nucleus with atomic mass, A, is defined as the difference between the total mass of free nucleons and the mass of the nucleus:

$$B_A = Z m_p + (A - Z) m_n - m_A$$

$$m_A = Z m_p + (A - Z) m_n - B_A.$$

Using these expressions in n_A (the previous slide) and approximating $m_A = A m_B$ inside the (), with $m_B \simeq m_p \simeq m_n$, one obtains (Ex. Sheet 4's exercise):

$$n_A = \frac{g_A}{2^A} A^{3/2} \left(\frac{m_B T}{2\pi}\right)^{3(1-A)/2} n_p^Z n_n^{A-Z} e^{B_A/T}$$

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

This shows that **abundance of a nuclear species**, critically depends on :

- the abundance of protons and neutrons at a given T ;
- the binding energy to temperature ratio, B_A/T

It is useful to write the nuclear abundances in terms of **mass fraction abundances**, X_A, defined as:

$$X_A \equiv \frac{n_A A}{n_B}$$

where

$$n_B = n_p + n_n + \sum_A A n_A$$

This definition allows on to write the following conservation equation of nuclear abundances

$$\sum_A X_A = 1$$

Using $n_A = X_A n_B / A$ in the expression of n_A in the previous slide, one has:

$$X_A = \frac{g_A}{2^A} A^{5/2} \left(\frac{m_B T}{2\pi}\right)^{3(1-A)/2} \frac{n_p^Z n_n^{A-Z}}{n_B} e^{B_A/T}$$

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

The density ratio in the previous expression can be written as:

$$\frac{n_p^Z n_n^{A-Z}}{n_B} = \frac{n_p^Z}{n_B^Z} \frac{n_n^{A-Z}}{n_B^{A-Z}} n_B^{A-1} = X_p^Z X_n^{A-Z} n_B^{A-1} = X_p^Z X_n^{A-Z} n_\gamma^{A-1} \eta^{A-1}$$

where we write $n_B = n_\gamma \, \eta$ and define the **baryon to photon ratio** as:

$$\boxed{\eta \equiv n_B/n_\gamma} \qquad \text{where,} \qquad n_\gamma = \frac{2}{\pi^2}\zeta(3)T^3$$

η **is a central quantity in BBN**. It can be calculated at present ($T_0 = 2.7525$):

$$\eta = 2.74 \times 10^{-8} h^2 \Omega_B$$

Using these expressions in X_A (of the previous slide) one has (check all the steps!):

$$X_A = \frac{g_A}{2^A} A^{5/2} \left(\frac{m_B T}{2\pi}\right)^{3(1-A)/2} X_p^Z X_n^{A-Z} \left(\frac{2}{\pi^2}\zeta(3)T^3\right)^{A-1} \eta^{A-1} e^{B_A/T}$$

$$= g_A A^{5/2} 2^{-A+A-1-3(1-A)/2} \pi^{-2A+2-3(1-A)/2} \zeta(3)^{A-1} T^{(1-A)(-3+3/2)} m_B^{3(1-A)/2} \eta^{A-1} X_p^Z X_n^{A-Z} e^{B_A/T}$$

$$= g_A \zeta(3)^{A-1} 2^{-5/2+3/2A} \pi^{-1/2-1/2A} A^{5/2} T^{-3(1-A)/2} m_B^{3(1-A)/2} \eta^{A-1} X_p^Z X_n^{A-Z} e^{B_A/T},$$

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

Which can be written in a nicer way...

$$\boxed{X_A = F(A)\left(\frac{T}{m_B}\right)^{3(A-1)/2} \eta^{A-1} X_P^Z X_n^{A-Z} e^{B_A/T}}$$

where

$$F(A) = g_A A^{5/2} \zeta(3)^{A-1} \pi^{(1-A)/2} 2^{(3A-5)/2}$$

This expression allows one to explicitly compute the mass fraction abundances of any nuclear species **assuming nuclear statistical equilibrium**. In particular one has:

$$
\begin{aligned}
\text{D}: \quad & X_2 = 16.3\left(\frac{T}{m_B}\right)^{3/2} \eta \, e^{B_2/T} X_n X_p, & B_2 = 2.22 \text{ MeV} \\[2mm]
{}^3\text{He}: \quad & X_3 = 57.4\left(\frac{T}{m_B}\right)^{3} \eta^2 e^{B_3/T} X_n X_p^2, & B_3 = 7.72 \text{ MeV}(^3\text{He}) \\[2mm]
{}^3\text{H}: \quad & & B_3 = 6.92 \text{ MeV}(^3\text{H}) \\[2mm]
{}^4\text{He}: \quad & X_4 = 113\left(\frac{T}{m_B}\right)^{9/2} \eta^3 e^{B_4/T} X_n^2 X_p^2, & B_4 = 28.3 \text{ MeV} \\[2mm]
{}^{12}\text{C}: \quad & X_{12} = 3.22 \times 10^5 \left(\frac{T}{m_B}\right)^{33/2} \eta^{11} e^{B_{12}/T} X_n^6 X_p^6, & B_{12} = 92.2 \text{ MeV}
\end{aligned}
$$

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

These abundances are constrained by the conservation equation which, if one neglects other elements, reads:

$$X_n + X_p + X_2 + X_3 + X_4 + X_{12} = 1$$

The neutron and proton fractions are related. Their mass fractions in equilibrium can be easily obtained. We know that

$$\left(\frac{n_n}{n_p}\right)_{eq} = \left(\frac{m_n}{m_p}\right)^{3/2} e^{-(m_n - m_p)/T}$$

Dividing the numerator and the denominator on left hand side of this equation by n_b one obtains:

$$\left(\frac{n_n}{n_p}\right)_{eq} = \left(\frac{X_n}{X_p}\right)_{eq} \simeq e^{-Q/T} \qquad (Q = m_n - m_p)$$

Note that expressions for X_n derived in the previous slides assume the approximation $m_B = m_p = m_n$. If this approximation is taken rigorously then $X_n/X_p = 1$. However, the mass difference ($Q = m_n - m_p$) in the exponential should not be ignored whereas it is smaller impact on the ratio of masses of the right-hand side of n_n/n_p .

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

Also note that, since the mass fraction abundances add up to one, e.g.,

$$X_n + X_p + X_2 + X_3 + X_4 + X_{12} = 1$$

and **nuclear synthesis occurs via 2-body reactions** (such as those in slide 5):

- Heavier **nuclear species are only effectively produced after the lighter ones are produced**. This is the case of Helium-4 which is only produced via 2-body reaction involving Deuterium or Hydrogen-3

- If the abundance fraction of a given nuclear species increases, this happens at the expenses of some other species (which has its fraction reduced)

So, one can define an **estimate of the temperature at which a given nuclear species is effectively produced by setting $X_A \sim 1$**. this can only happen for $T \ll B_A$ so that the exponential term in X_n compensates η (the baryon to photon ratio) term, which is small.

$$X_A = F(A)\left(\frac{T}{m_B}\right)^{3(A-1)/2} \eta^{A-1} X_P^Z X_n^{A-Z} e^{B_A/T} \quad \sim 1$$

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

From this previous expression on can derive **an approximate equation to compute the temperature of effective production** of a given nuclear species, T_A. Setting $X_A \sim X_n \sim X_p \sim 1$, taking the logarithm of X_A and droping $\ln F(A)$, which is also $F_A \sim 1$, gives:

$$0 = \frac{3}{2}(A-1)\ln\left(\frac{T_A}{m_B}\right) + (A-1)\ln\eta + \frac{B_A}{T_A}$$

This can be used with iterative numerical methods to estimate T_A,

$$T_A \approx -\frac{B_A}{\frac{3}{2}(A-1)\ln\left(\frac{T_A}{m_B}\right) + (A-1)\ln\eta}$$

$$= \frac{B_A}{A-1}\frac{1}{\ln\eta^{-1} + \frac{3}{2}\ln\left(\frac{m_B}{T_A}\right)}.$$

For example, using this expression for Deuterium, one obtains:

$$T_D = \frac{2.22}{1}\frac{1}{\ln(2\times10^{-8}\Omega_B h^2)^{-1} + \frac{3}{2}\ln\left(\frac{1\,\text{GeV}}{T_D}\right)}$$

Similar equations can be derived for other nuclear species.

Big-Bang Nucleosynthesis

Nuclear Statistical equilibrium

Solving these type of equations, one obtains the following effective temperatures of production (in equilibrium) of the Deuterium, Tritium, and Helium-4:

$$T_D \approx 0.07\text{MeV} \; ; \quad T_{^3\text{H}} \approx 0.11\text{ MeV} \; ; \quad T_{^4\text{He}} \approx 0.28\text{ MeV}.$$

These temperatures can be converted to time using the Friedmann equation expressed in terms of temperature of the effective degrees of freedom in energy

$$\frac{\dot{a}}{a} = H = \sqrt{\frac{\hbar c}{3M_{pl}^2}\frac{\pi^2}{30}g_* T^4} = \frac{\pi}{3}\left(\frac{g_*}{10}\right)^{1/2}\frac{T^2}{M_{pl}}$$

where we assume radition domination.
Taking $g_* = 3.38$ one can derive the following expression for the beginning of the nucleosynthesis,

$$t_{\text{nuc}} = 132\text{ s}\left(\frac{0.1\text{ MeV}}{T_{\text{nuc}}}\right)^2.$$

Big-Bang Nucleosynthesis

Neutron's abundance

The production of nuclear elements within the mechanism of Big-Bang nucleosynthesis is directly related with the abundance of free neutrons, and the evolution of n_B or the baryon to photon ratio. One can tell the story of neutrons in a few steps:
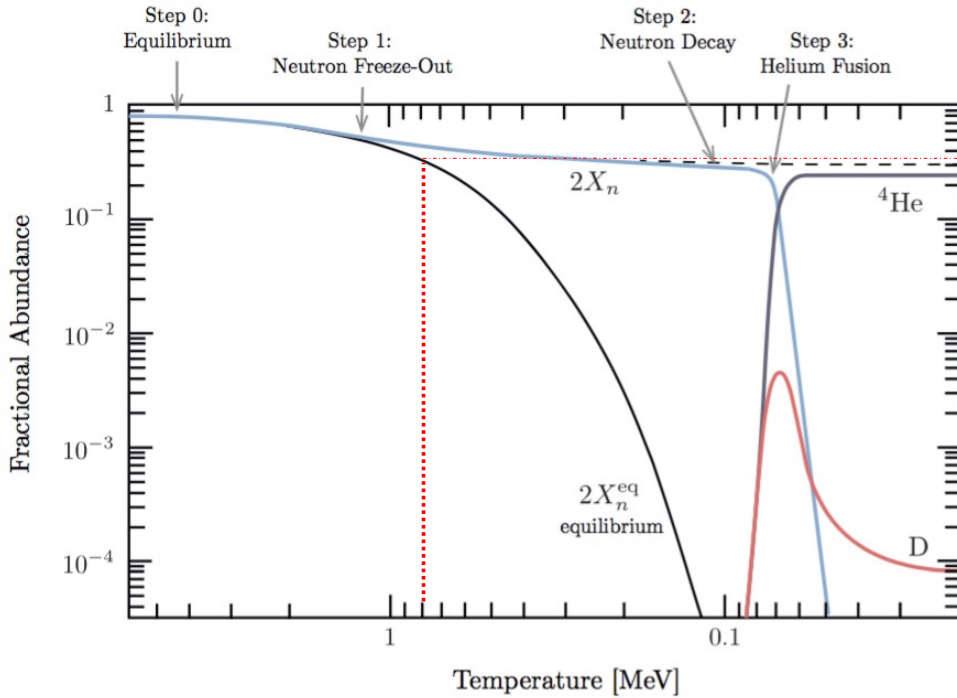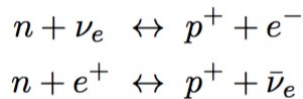

Neutrons decouple from the fluid and abandon equilibrium. They also decay into Protons.

Big-Bang Nucleosynthesis

Neutron's abundance

Step 0 (Equilibrium): Above $T \sim 1$ MeV protons and neutrons are in equilibrium via the nuclear reactions

$$n + \nu_e \ \leftrightarrow \ p^+ + e^-$$
$$n + e^+ \ \leftrightarrow \ p^+ + \bar{\nu}_e$$

The relative abundance of neutrinos to protons is then given by the equilibrium prediction (neglecting the chemical potential of the leptons, $\mu_n \sim \mu_p$):

$$\left(\frac{n_n}{n_p} \right)_{\mathrm{eq}} = \left(\frac{m_n}{m_p} \right)^{3/2} e^{-(m_n - m_p)/T}$$

where $m_n - m_p = Q = 1.293$ MeV is the mass difference between neutrons and protons. So, the fraction of neutrons at equilibrium can be approximated by:

$$X_n^{\mathrm{eq}} \simeq \frac{n_n^{\mathrm{eq}}}{n_p^{\mathrm{eq}} + n_n^{\mathrm{eq}}} = \frac{n_n^{\mathrm{eq}}/n_p^{\mathrm{eq}}}{1 + n_n^{\mathrm{eq}}/n_p^{\mathrm{eq}}} \simeq \frac{e^{-Q/T}}{1 + e^{-Q/T}}$$

where $n_B \simeq n_n + n_p$ is used in the first equality and $m_n / m_p \simeq 1$ is used in the last equality. At $T = 0.8$ MeV this gives,

$$X_n^{\mathrm{eq}}(0.8\,\mathrm{MeV}) = 0.17 \ \sim 1/6$$

Big-Bang Nucleosynthesis

Neutron's abundance

Step 1 (Decoupling): As neutrinos decouple and positron-electron annihilation occurs, neutrons are forced to also decouple from the fluid. From the figure in a previous slide one expects that the **freeze out abundance of neutrons** should be close to:

$$X_n^\infty \sim X_n^{\text{eq}}(0.8\,\text{MeV}) \sim \frac{1}{6}$$

To confirm this expectation, one needs to integrate the Boltzmann equation for the interactions that keep neutrons and protons in contact with the plasma. As seen in Chapter 4, the **Boltzmann equation** for the 2-body interaction $1 + 2 \rightleftarrows 3 + 4$ is:

$$\frac{1}{a^3}\frac{d(n_1 a^3)}{dt} = -\langle\sigma v\rangle\left[n_1 n_2 - \left(\frac{n_1 n_2}{n_3 n_4}\right)_{\text{eq}} n_3 n_4\right]$$

For interactions of the form $n + l_1 \leftrightarrows p^+ + l_2$, where l_i is a lepton **tightly bound to the plasma** one obtains:

$$\frac{1}{a^3}\frac{d(n_n a^3)}{dt} = -\Gamma_n\left[n_n - \left(\frac{n_n}{n_p}\right)_{\text{eq}} n_p\right]$$

Since leptons are tightly bound to the fluid one has: $n_{l_i} = n_{l_i}^{eq}$, and $\Gamma_n = <n_{l_1}\sigma v>$.

Big-Bang Nucleosynthesis

Neutron's abundance

Step 1 (Decoupling): The solution of the Boltzmann equation is numerical. To compute the free neutron's fraction, X_n, one needs to use its definition (in slide 8) and compute the densities of all baryon species in the fluid at a given time.

However, one can simplify the calculation of X_n using the following approximations:

- before neutron decoupling $n_b \simeq n_n + n_p \Leftrightarrow 1 \simeq X_n + X_p$
- the total number of baryons is conserved, i.e., $n_b a^3 = constant$.

Using these assumptions the Boltzmann equation can be written as (see Black Board):

$$\frac{1}{a^3}\frac{d(n_n a^3)}{dt}\frac{1}{(n_B a^3)} = -\frac{\Gamma_n}{(n_B a^3)}\left[n_n - \left(\frac{n_n}{n_p}\right)_{\text{eq}} n_p\right] \Leftrightarrow$$

$$\Leftrightarrow \frac{d}{dt}\left(\frac{n_n a^3}{n_B a^3}\right) = -\Gamma_n\left[\frac{n_n}{n_B} - \left(\frac{n_n}{n_p}\right)_{\text{eq}}\frac{n_p}{n_B}\right] \Leftrightarrow$$

$$\Leftrightarrow \frac{dX_n}{dt} = -\Gamma_n\left[X_n - \left(\frac{n_n}{n_p}\right)_{\text{eq}} X_p\right] \Leftrightarrow \boxed{\frac{dX_n}{dt} = -\Gamma_n\left[X_n - (1 - X_n)\,e^{-Q/T}\right]}$$

where we used $X_p \simeq 1 - X_n$ and the fact that ($Q = m_n - m_p$):

$$\left(\frac{n_n}{n_p}\right)_{\text{eq}} = \left(\frac{m_n}{m_p}\right)^{3/2} e^{-(m_n - m_p)/T} \simeq e^{-Q/T}$$

Big-Bang Nucleosynthesis

Neutron's abundance

Step 1 (Decoupling):

To integrate this Boltzmann equation,

$$\frac{dX_n}{dt} = -\Gamma_n \left[X_n - (1 - X_n)e^{-Q/T} \right]$$

it is useful to make a change of variable $x = Q/T$,

$$\frac{dX_n}{dt} = \frac{dX_n}{dx}\frac{dx}{dt} = \frac{dX_n}{dx}\frac{d(Q\,T^{-1})}{dt} = \frac{dX_n}{dx}\left(-\frac{Q}{T^2}\frac{dT}{dt}\right) = -\frac{dX_n}{dx}\frac{x}{T}\frac{dT}{dt} \simeq \frac{dX_n}{dx}\,x\,H$$

Where the last approximation comes from $T = A_i\,g_{*S}^{-1/3}(T)\,a(t)^{-1}$ assuming $g_{*S} = $ constant (see Riccati equation in Chap 5). This expression is therefore valid away from mass thresholds. Using this in the Boltzmann equation and writing

$$H = \sqrt{\frac{\rho}{3M_{\rm pl}^2}} = \underbrace{\frac{\pi}{3}\sqrt{\frac{g_\star}{10}}\frac{Q^2}{M_{\rm pl}}}_{\equiv H_1 \approx 1.13\,s^{-1}}\frac{1}{x^2}\,, \qquad \text{with} \quad g_\star = 10.75\,.$$

where H_1 is the $x-$independent part of the Hubble function written as a function of x the Boltzmann equation reads:

$$\frac{dX_n}{dx} = \frac{\Gamma_n}{H_1}\,x\left[e^{-x} - X_n(1 + e^{-x})\right]$$
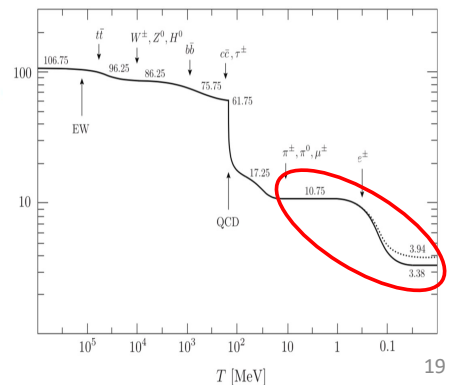
Big-Bang Nucleosynthesis

Neutron's abundance

Step 1 (Decoupling):

The exact form of Γ_n depends on the lepton particles being considered. Its calculation can be done in Quantum Field Theory. It can be, generically, approximated by:

$$\Gamma_n(x) = \frac{255}{\tau_n} \cdot \frac{12 + 6x + x^2}{x^5}$$

where $\tau_n = 886.7$ s is the neutron half-time decaying period.

With these expressions the **numerical integration of the Boltzmann** equation (blue curve) would give:

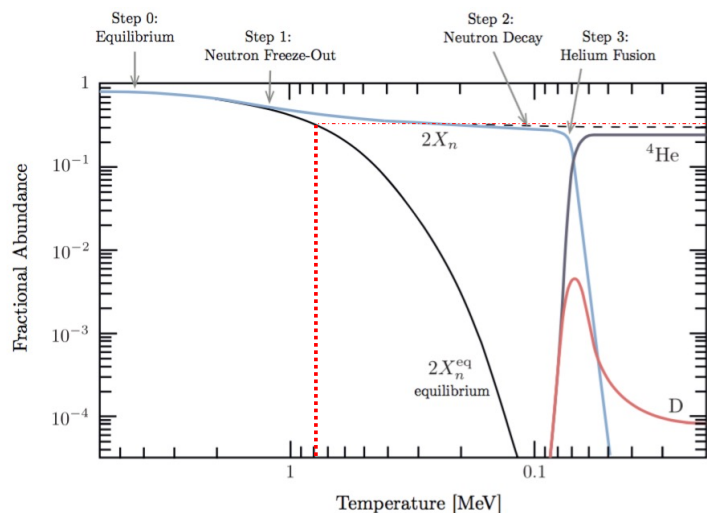$$X_n^\infty \equiv X_n(x = \infty) = 0.15$$

only if neutrons don't decay! (Step 2) This is like the result in slide 17.

So just **before Neutron decay** one has:

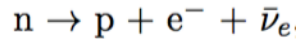$$n_B \simeq n_p + n_n \iff 1 \simeq X_p + X_n$$

and

$$\boxed{X_p \simeq 1 - X_n = 0.85 \quad ; \quad X_n/X_p \simeq 0.17}$$

Big-Bang Nucleosynthesis

Neutron's abundance

Step 2 (Neutron decay): The decoupled neutrons also decay into protons via the process:

$$n \rightarrow p + e^- + \bar{\nu}_e$$

which has a half-time decaying period of $\tau_n = 886.7 \pm 0.8 \text{ sec}$. **This decay can only become relevant when the universe is old enough (as old as the τ_n decaying period)**.
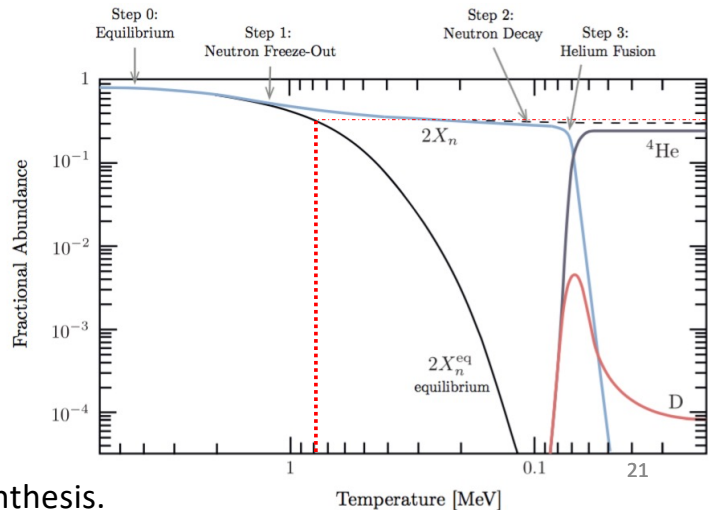
To include neutron decay into the calculation, we simply multiply the neutron abundance by an exponential term characteristic of nuclear decaying processes:

$$X_n(t) = X_n^{\text{no-decay}} e^{-t/\tau_n}$$
$$\simeq \frac{1}{6} e^{-t/\tau_n}$$

Where t is (radiation domination):

$$t = 132 \text{ s} \left(\frac{0.1 \text{ MeV}}{T}\right)^2.$$

This decaying mechanism has strong implications for the nuclear species synthesis.

Big-Bang Nucleosynthesis

Neutron's abundance

Step 2 (Neutron decay)

Using these assumption one can, for example, compute mass fraction abundances by $t = t(T \sim 0.07 \, MeV) = 269.4 \, s$
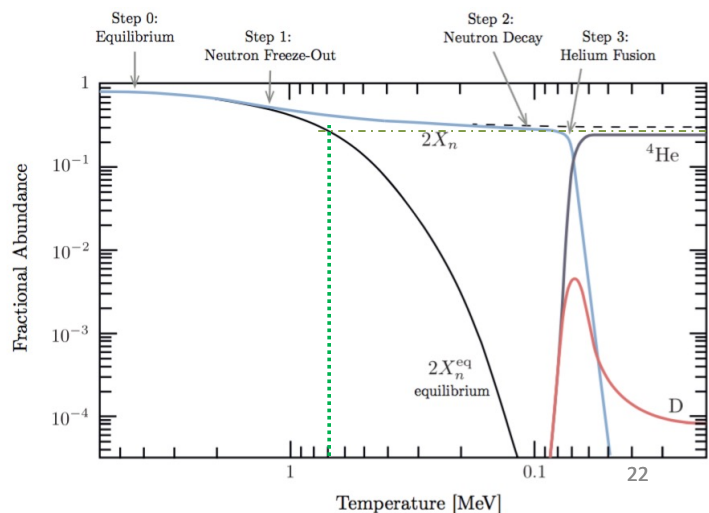
$$X_n(0.07 \, MeV) = \frac{1}{6} \exp\left(-\frac{260.4 \, s}{886.7 \, s}\right) = 0.123$$

$$X_p(0.07 \, MeV) = 1 - X_n = 0.877$$

and therefore:

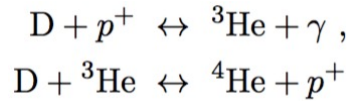$$\frac{X_n(0.07 \, MeV)}{X_p(0.07 \, MeV)} = 0.140 \sim \frac{1}{7}$$

this is just before Hellium-4 starts to be produced in an efficient way.

Big-Bang Nucleosynthesis

Helium abundance

Step 3 (Helium fusion): Helium is produced via the reactions:

$$D + p^+ \leftrightarrow {}^3\text{He} + \gamma \,,$$
$$D + {}^3\text{He} \leftrightarrow {}^4\text{He} + p^+$$

that **require the existence of Deuterium**, which is produced via: $n + p^+ \leftrightarrow D + \gamma$
So, helium cannot be produced before enough deuterium is formed.

The **helium fraction abundance by the end of BBN** can be **estimated** as follows:

- Until before neutron decay ($T \sim 0.07$) all baryons are in the form of free protons and neutrons: $\boxed{n_B^i \simeq n_p^i + n_n^i}$

- By the end of BBN **hydrogen** (p) and **helium-4** nuclei are the 1$^{\text{st}}$ and 2$^{\text{nd}}$ most abundant elements (other nuclei are residual). So, baryon conservation allows to write: $\boxed{n_p^f + 4n_{^4\text{He}}^f = n_p^i + n_n^i}$

- By the end of BBN **about half of the initial neutrons are inside helium nuclei** (because each nucleus of helium contains 2 neutrons): $\boxed{n_{^4\text{He}}^f = n_n^i/2}$

Under these approximations, the **Helium mass fraction abundance** becomes:

$$X_{^4\text{He}} = \frac{4n_{^4\text{He}}^f}{n_p^f + 4n_{^4\text{He}}^f} = \frac{4n_n^i/2}{n_p^i + n_n^i} = \frac{2n_n^i}{n_p^i + n_n^i} = \frac{2n_n^i/n_p^i}{1 + n_n^i/n_p^i} = \frac{2X_n^i/X_p^i}{1 + X_n^i/X_p^i} \simeq \frac{2/7}{1 + 1/7} \simeq \frac{1}{4}$$

Big-Bang Nucleosynthesis

Numerical evolution of mass fraction abundances of light elements:

24
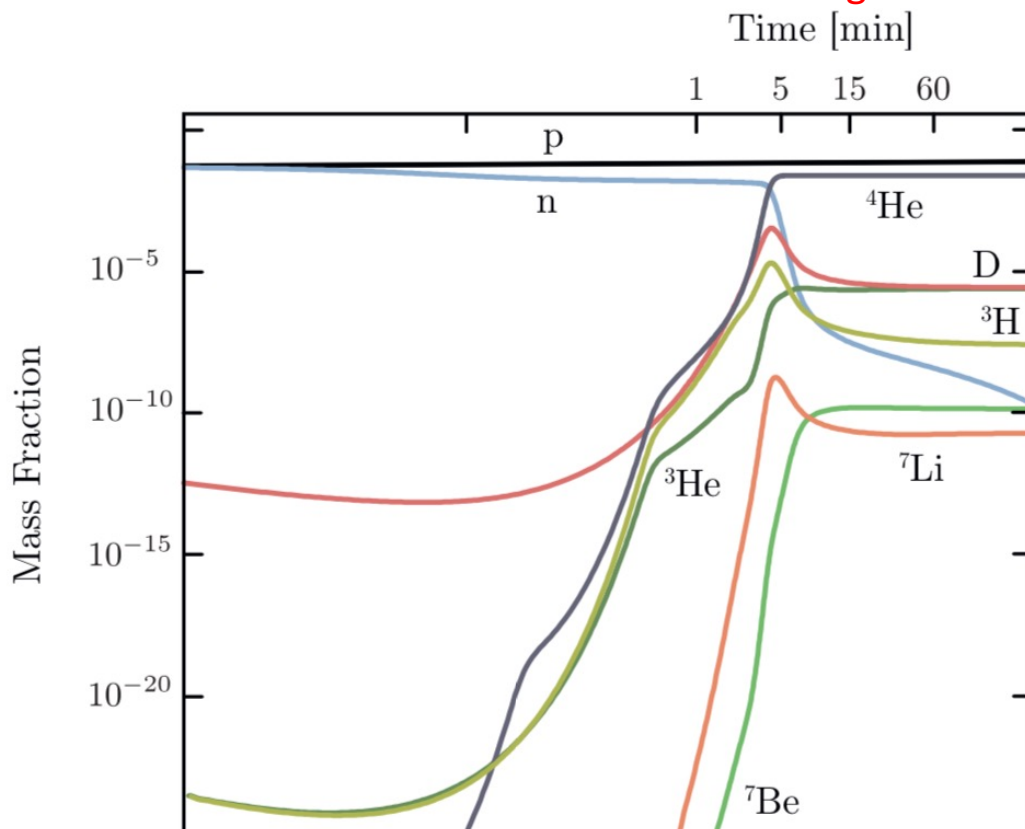
Big-Bang Nucleosynthesis

Comparison with observations:

Helium 4: constraints from ionized gas (metal poor) clouds

Deuterium: constraints from metal poor quasar absorption systems

Helium 3: is hard to constraint. Limits estimated from solar system and HII (metal abundant) regions in our galaxy

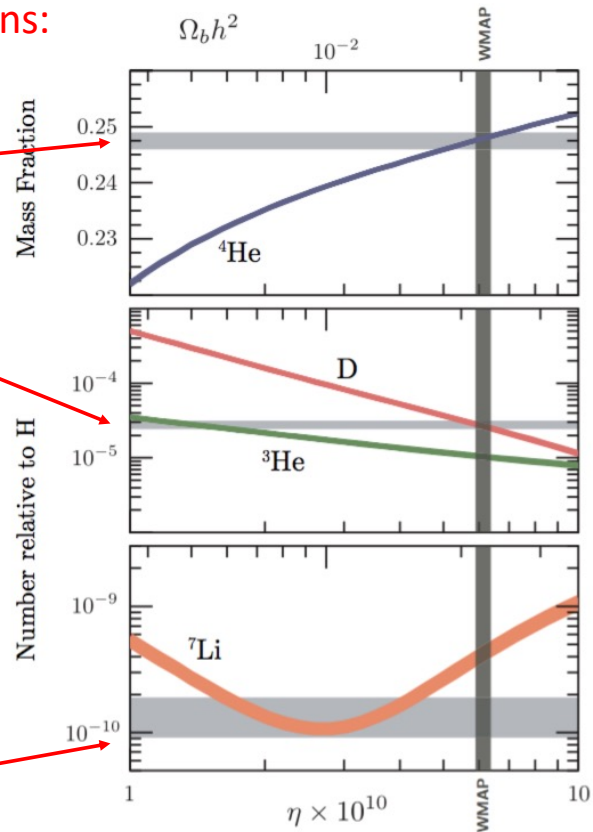Lithium 7: constraints from low metallicity population II stars in our galaxy.

$\Omega_b h^2$

Figure 3.10: *Theoretical predictions (colored bands) and observational constraints (grey bands).*