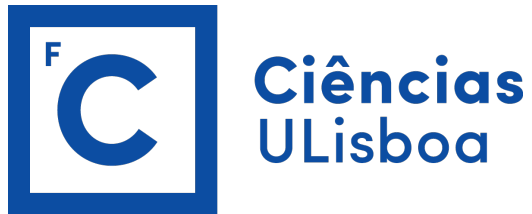


# Cosmologia Física

Ismael Tereno (IA)



2025

# Introduction

**The course: a physical model for the Universe**

## Practical information

Thursday 11h30-12h30 (T) C8.2.04

Thursday 12h30-13h30 (TP) C8.2.04

Friday 14h30-15h30 (T) C8.2.04

### **Communication: Fénix page and email**

Links to lecture notes, homework, and other courses material are given in this page:

<https://fenix.ciencias.ulisboa.pt/courses/cfis-2254879305243175/lecture-notes>

### **Contact**

email: [tereno@fc.ul.pt](mailto:tereno@fc.ul.pt)

office: C8.1.42

### **Evaluation**

Homework: series of exercises

Presentation: of a topic chosen from a list to be given (for example to go in greater depth into a topic from the course). In principle no written report will be required.

# Physical Cosmology

describing the physical model of the Universe

## Everything

The universe is all of space and time and their contents.

It comprises all fundamental interactions, physical processes and physical constants, and therefore all forms of energy and matter, and the structures they form.

→ two fundamental constraints in the study of the Universe:

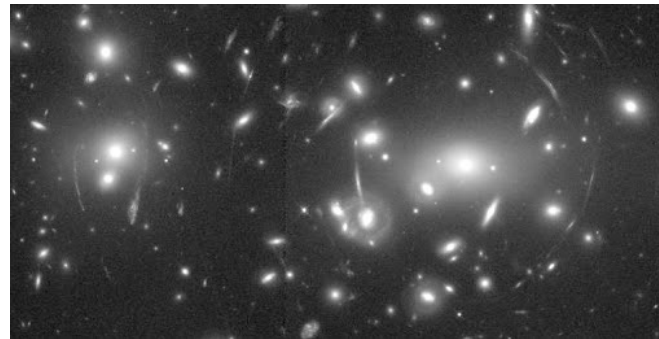
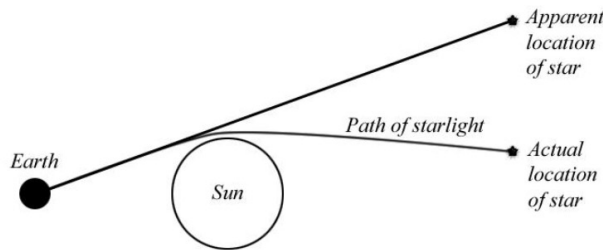
→ finite speed of information propagation → we have only access to part of the Universe - our **lightcone**.

→ we only observe one Universe → we cannot make laboratory experiments, test results in different conditions, or get statistics (possible only under an approximation, the **ergodic hypothesis**) → fundamental limitation – **cosmic variance**.

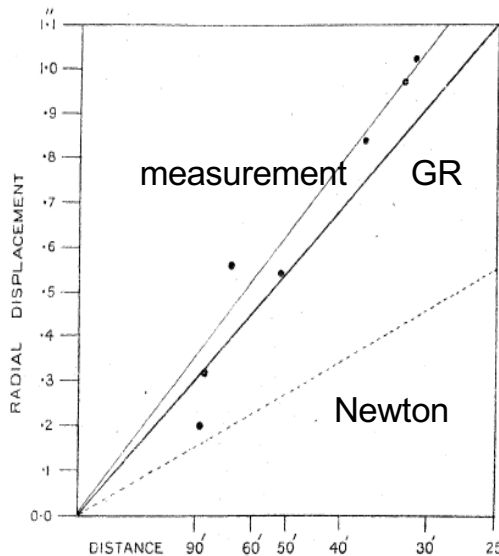
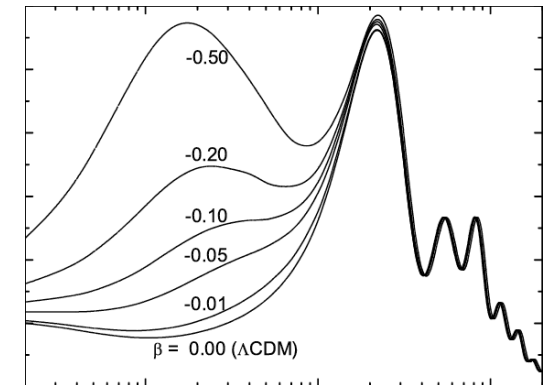
# + Gravity

is the force that drives the cosmological evolution and describes large-scale interactions, because among the 4 fundamental forces strong and weak forces have short range and the Universe is neutral.

It is tested on various scales:



1987 - today



1919

(Eddington)

Gravity is described by **General Relativity**

→ **metric**

→ Einstein equations

Awarded to **Albert Einstein** "for his services to Theoretical Physics, (and especially for his discovery of the law of the photoelectric effect)." (1/1)



1921

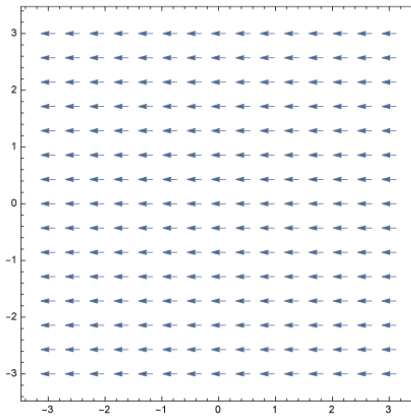
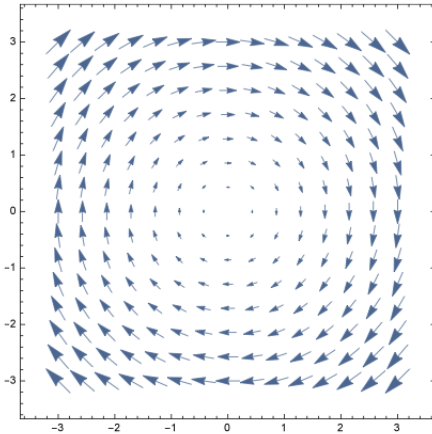
## + Cosmological principle

Isotropy :

the Universe observed in any direction looks the same → rotational invariance

Homogeneity:

the Universe is identical in all points, at each instant → translational invariance

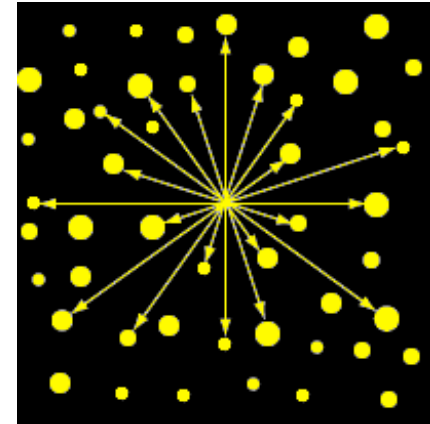


→ metric is Robertson-Walker, **spherically symmetric** with two degrees of freedom:  $a$ ,  $K$  → and two related cosmological parameters:  $H_0$ ,  $\Omega_K$

## + Olbers paradox

→ universal loss of luminosity → **redshift**

→ scale factor “a” must **evolve**



## + Observations of the recession of galaxies

→ Expansion **Big Bang theory**

→ Thermal history

→ Nucleosynthesis

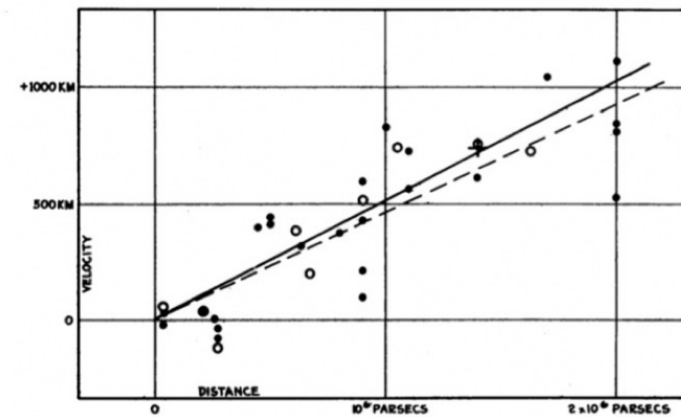


FIGURE 1  
Velocity-Distance Relation among Extra-Galactic Nebulae.

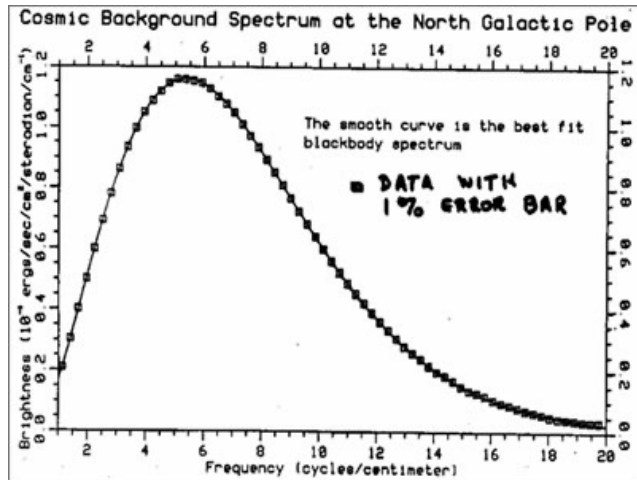
(Hubble)

1929

→ Existence of a universal background radiation:

the **cosmic background radiation, CMB** [ $z \sim 1100$ ]

1965 - 1990



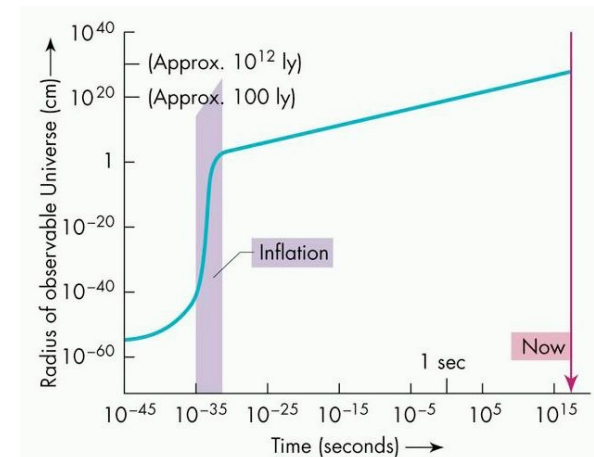
(COBE, 1990)

Awarded to **Arno A. Penzias and Robert W. Wilson** "for their discovery of cosmic microwave background radiation." (1/4 + 1/4)



→ Horizon, flatness and coincidence problems

Solved by **Inflation**





## + Observation of anisotropies in the CMB

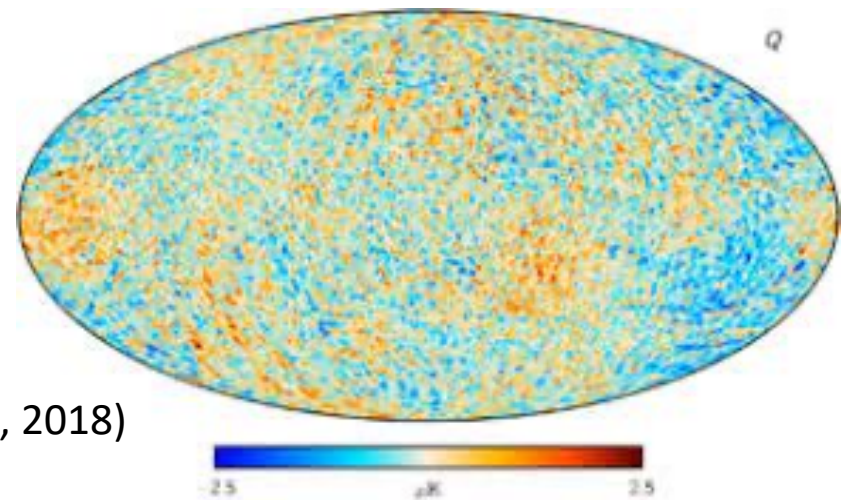
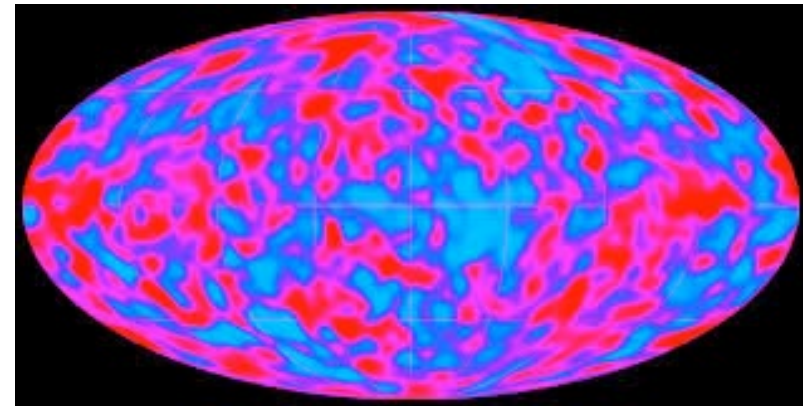
1992 - 2018

(COBE, 1992)

→ Existence of perturbations to the cosmological principle → found the **seeds of structure!**

→ Problem of the origin of the seeds of structure

Solved by the mechanism of **quantum fluctuations** + inflation + **gravitational interaction**



(Planck, 2018)

Awarded to **John C. Mather** and **George F. Smoot** "for their discovery of the blackbody form and anisotropy of the cosmic microwave background radiation." (1/2 + 1/2)

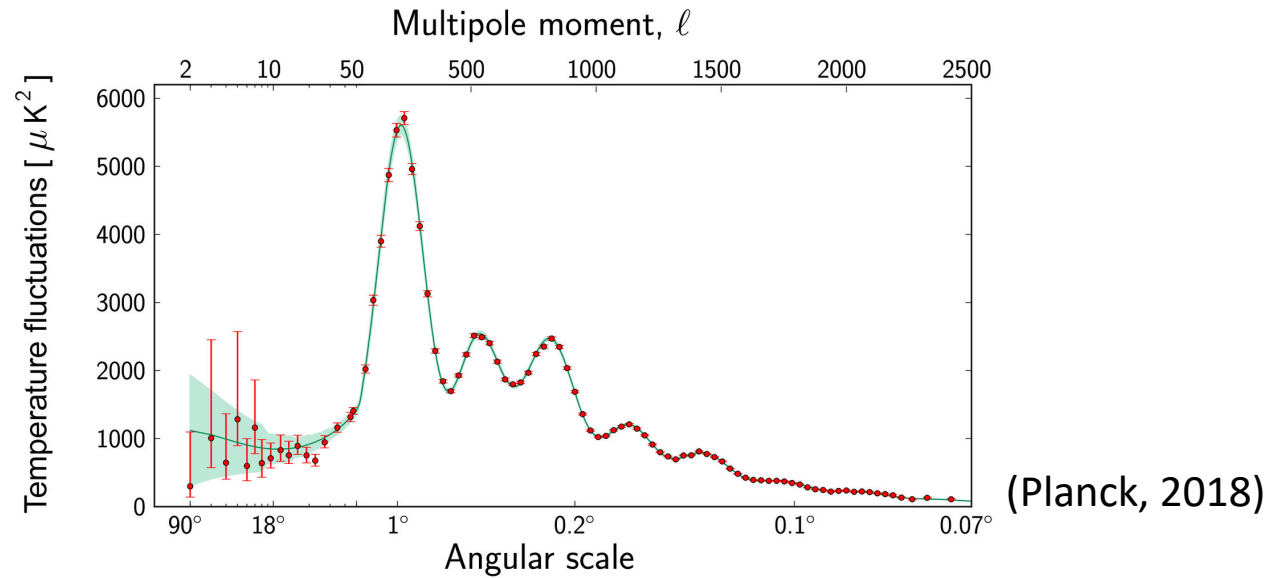


2006

## + Measurement of the anisotropies in the CMB

1992 - 2018

Their amplitude is very small  $\delta_T \sim 10^{-5}$



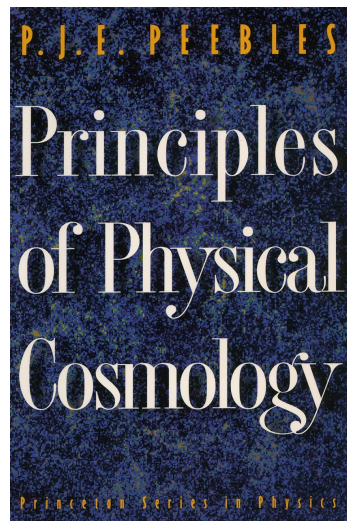
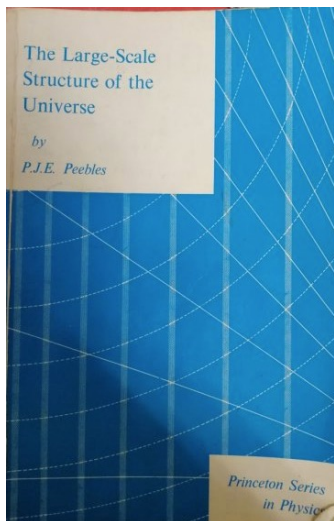
→ **Isotropy** confirmed (wide angular bins, i.e., on large angular scales)

→ indicates very small clustering at  $z=1100 \rightarrow \delta_b(z=1100) \sim 10^{-5}$

- + Gravitational collapse is slow ( $\delta_b$  grows only a factor  $\sim 10^3$  until  $z=0$ )
- + Today there are structures with large density contrast  $\delta$  (large clustering at  $z=0$ )

→ Problem of the mechanism of **structure formation**

Solved by the hypothesis of the existence of an extra component in the cosmological fluid - **Dark matter** → **CDM model**



Awarded to **P. James. E. Peebles** "for theoretical discoveries in physical cosmology" (1/2)



## + Structure formation

### Linear (gravitational clustering)

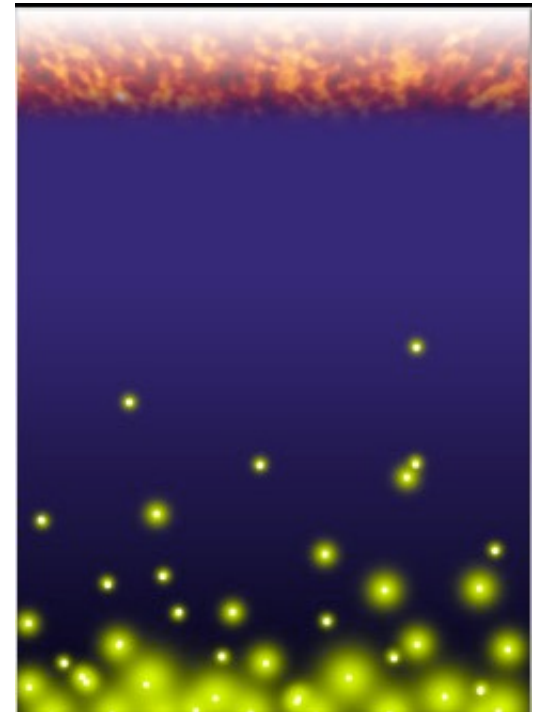
→ There is a very long process of **linear** clustering, during the **dark ages** and beyond. In some points, local gravitational fields start to become strong.

### Non-linear (collapse)

→ Formation of **dark matter halos**

**Non-linear** collapse of baryonic matter on those halos → neutral Hydrogen HI clouds condense and form the **first stars**, ending the dark ages → **Cosmic Dawn** [ $z \sim 20$ ]

Meanwhile, in some parts (or scales) of the Universe linear structure formation continues its slow process.



## + Galaxy formation

→ The gravitational collapse does not describe all aspects of structure formation.

Non-gravitational effects associated to the baryonic matter start to be important at this stage:

**Cooling** - the gas has to cool-down to condense. By losing pressure it falls into the center of the halo where it can form stars. Angular momentum conservation during the fall produces a disk → spiral galaxies

**Feedback** - the quantity of cold gas available decreases by influence of the environment

**Mergers** - frequent interactions between halos may form elliptical galaxies from primitive spiral galaxies.



The first galaxies [ $z \sim 15?$ ] led to the **Reionization** era [ $z \sim 10$ ]

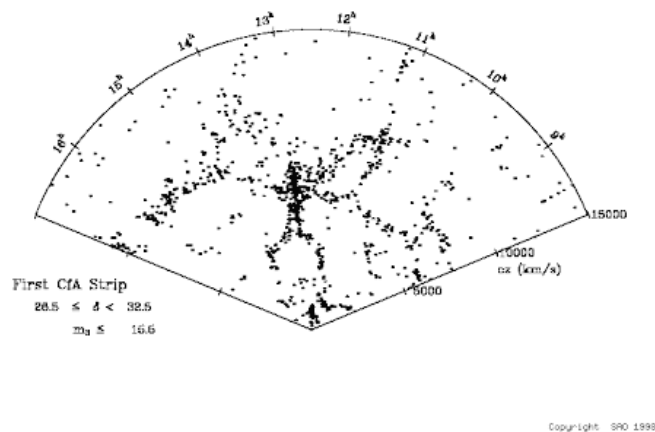
→ New radiation ionizes the HI clouds, forming ionized Hydrogen regions HII - the **reionization** of the Universe

## + Observation of the LSS of luminous matter in 2D and 3D

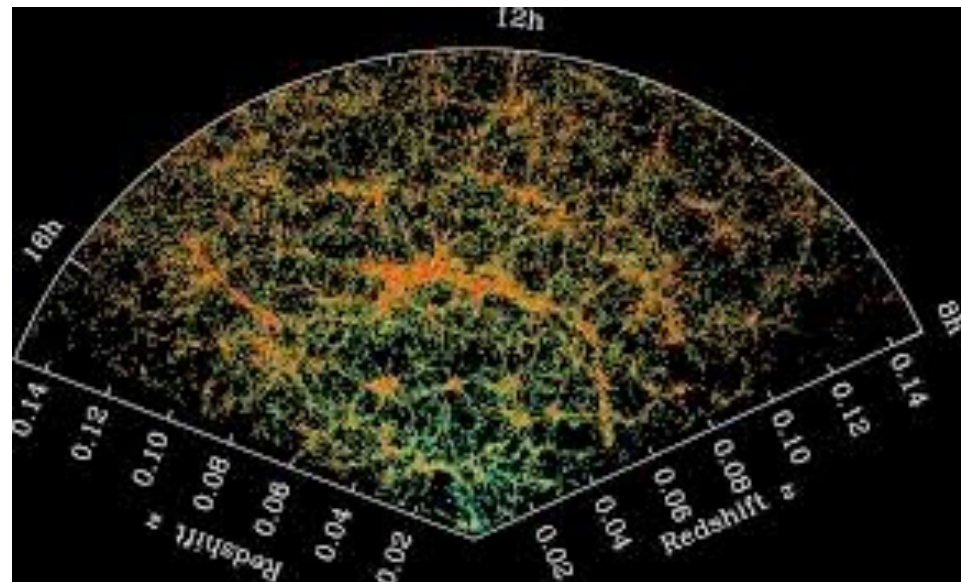
Since the epoch of reionization, galaxies have been forming and evolving, with an intense period of star formation occurring at the **Cosmic Noon** [ $z \sim 2-3$ ]

Mapping the galaxies positions gives (biased) information on the **cosmic web** - the DM **large-scale structure** of the Universe - by using **galaxy clustering** methods and **redshift space distortions** → find out the details of structure formation

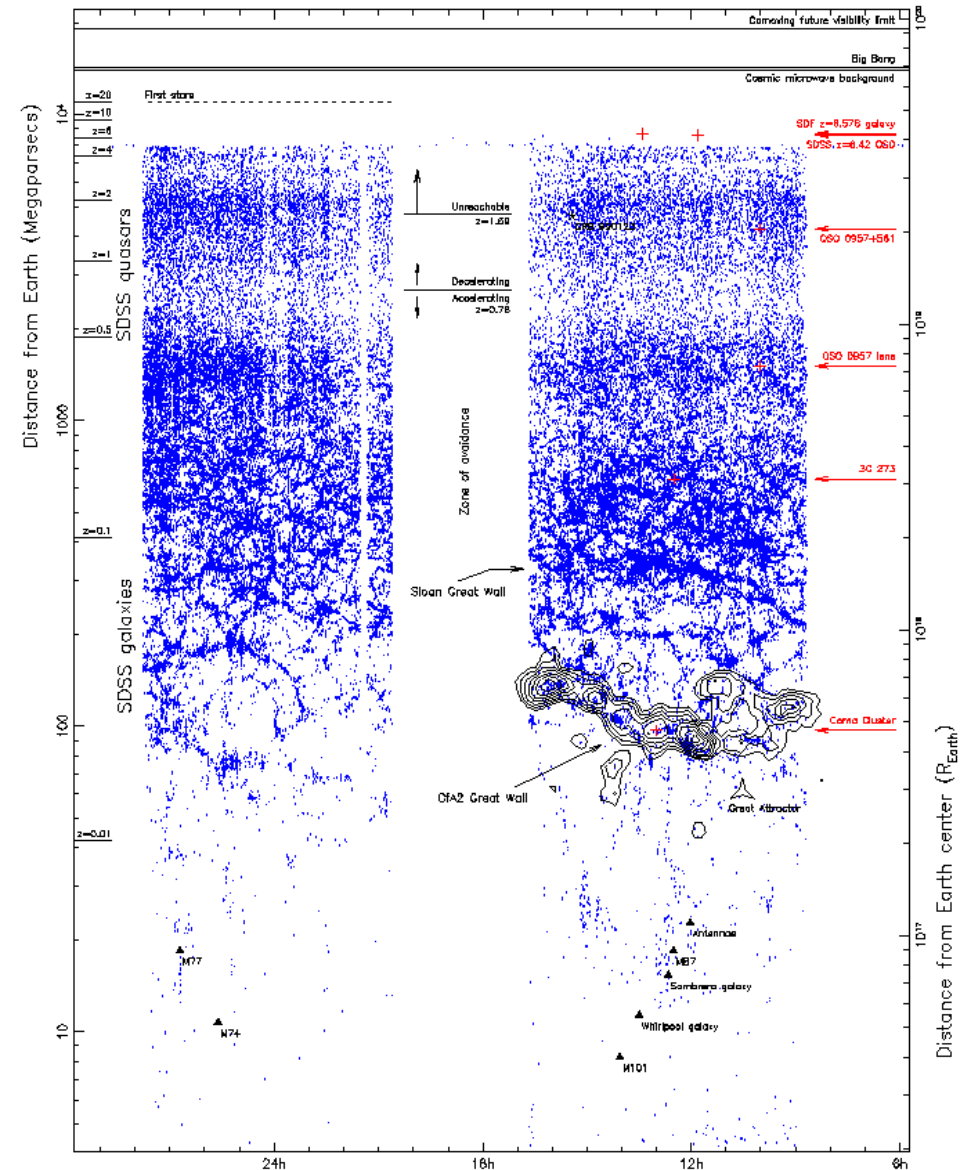
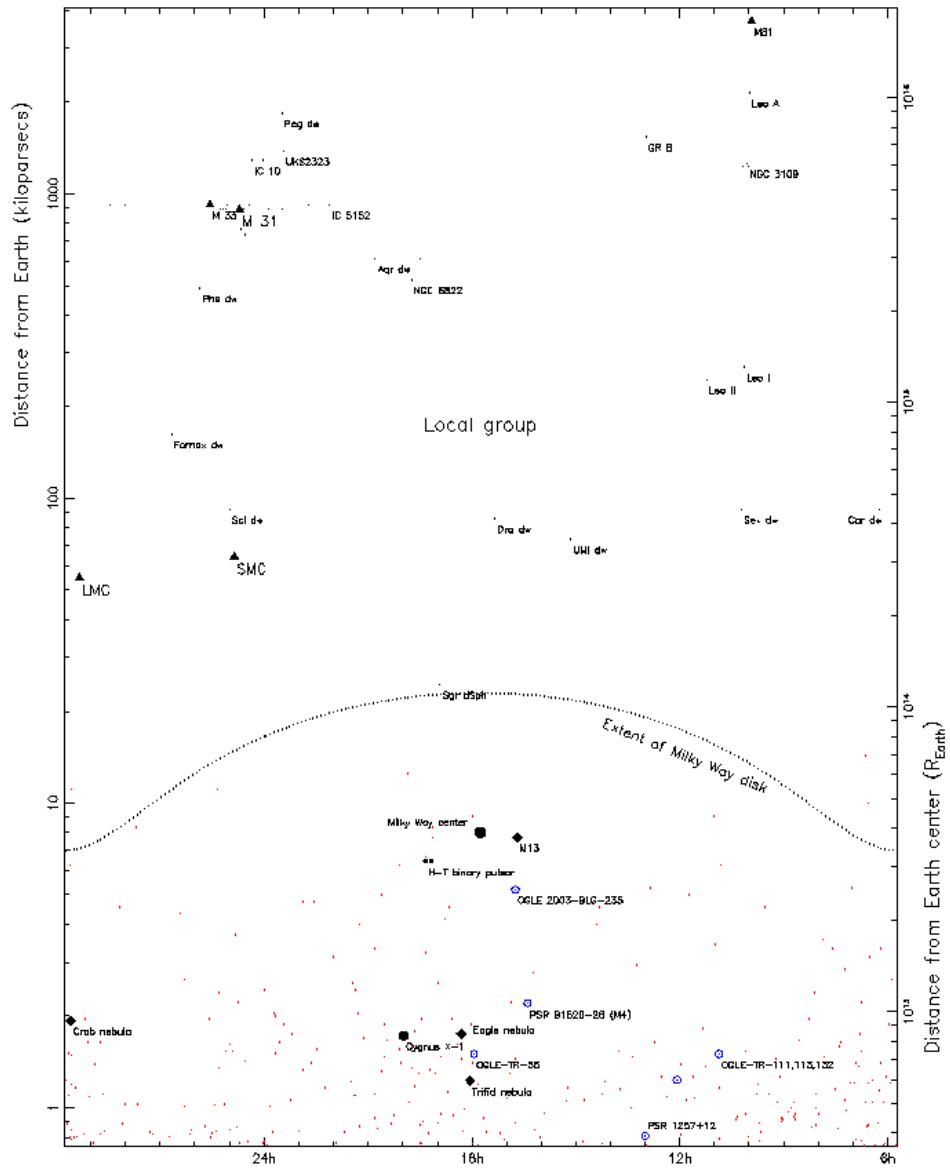
1980 - today



(CfA, 1980)



(SDSS, 2008)

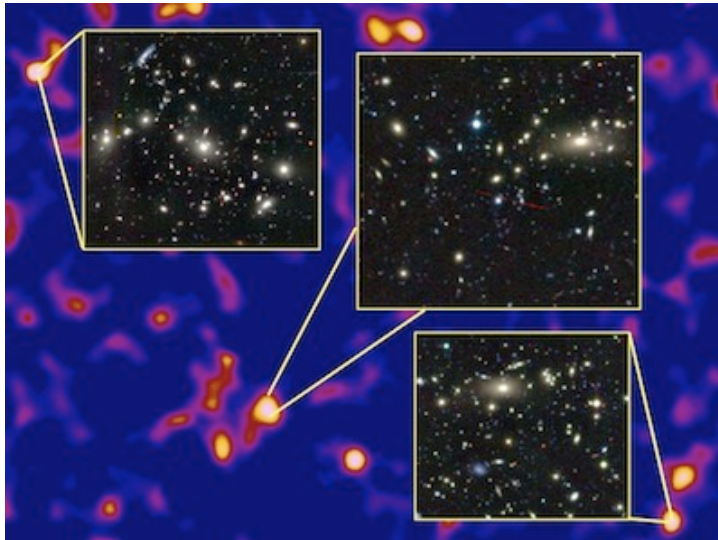


→ Homogeneity confirmed (on large scales)

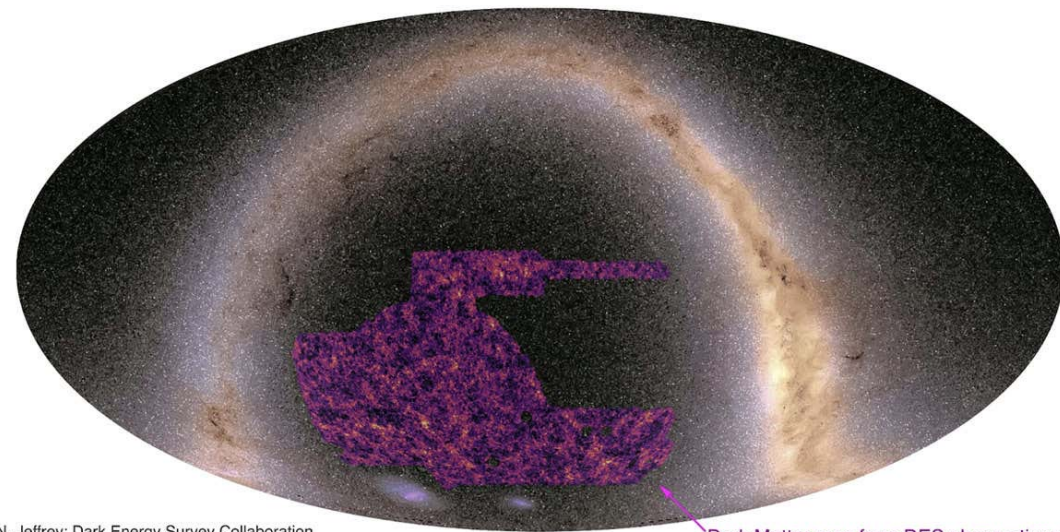
## + Observation of the LSS of dark matter in 2D and 3D

Mapping the galaxies shapes gives (less biased) information on the **cosmic web** – the DM **large-scale structure** of the Universe - by using **weak gravitational lensing** methods → find out the details of structure formation

2000 - today



(CFHTLenS, 2012)



N. Jeffrey; Dark Energy Survey Collaboration

Dark Matter map from DES observations

(DES, 2021)



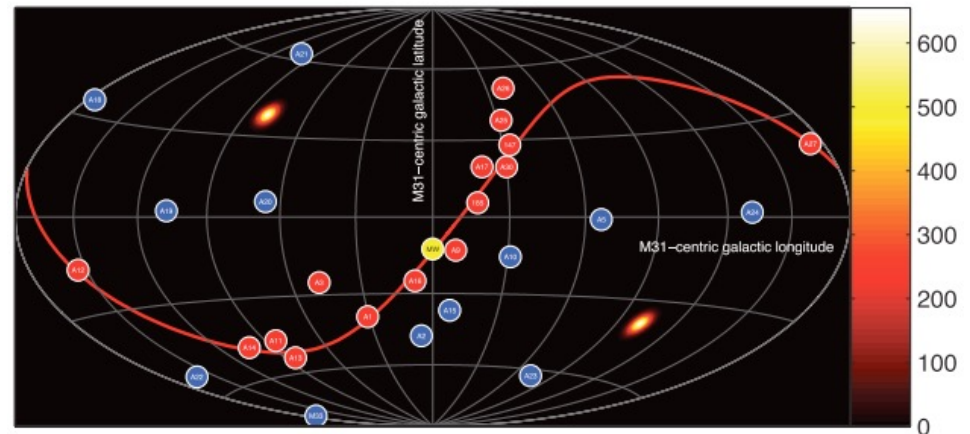
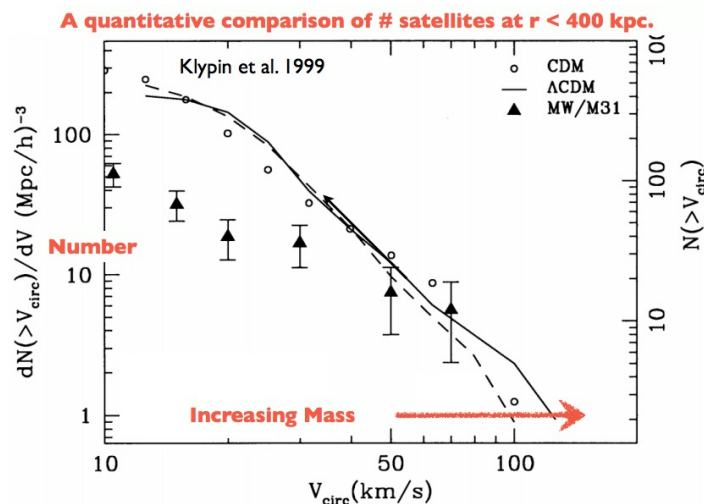
## + Observations of properties of small-scale structure (kpc)

→ Problem of the radial density profile of structures (**cusps/core**)

→ Problem of lack of structures (**satellite galaxies**)

→ Problem of the **satellite orbital plane** - possibly solved in 2022 with new simulations and Gaia 6-dim data (Sawalla et al, arXiv: 2205.02860)

Several problems not yet solved, leading to hypothesis of existence of other types of dark matter (Warm Dark Matter, Interacting DM), interacting DM/baryons in dense environments (Baryon feedback), hypothesis of modifications of GR on galactic scales (MOND)



## + Measurements of distances to SN

**Supernovae** at all redshifts are fainter (more distant?) than expected from the  $d_L(z)$  predicted by the CDM cosmological model

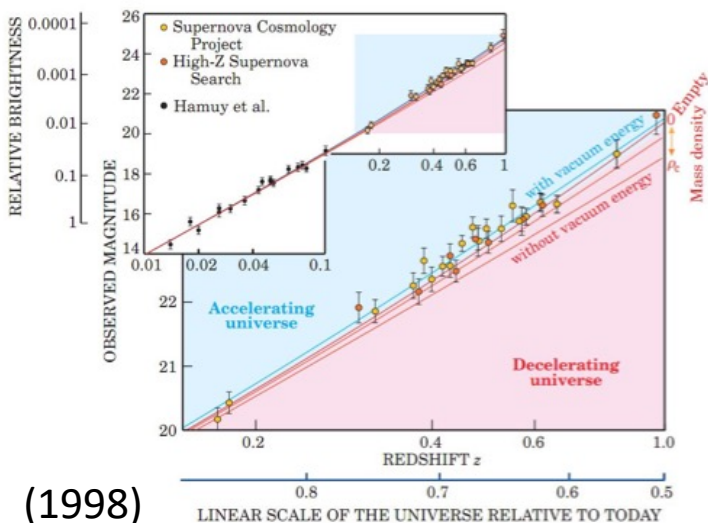
→ The Universe changed from a decelerated expansion to an accelerated one

Solved by assuming the existence of an extra component in the cosmological fluid - **Dark energy** →  **$\Lambda$ CDM model**

→ Alternatively, the Universe is not accelerating but the theory of gravitation on large scales is not GR, and the measured distances are compatible with that theory

New “**modified gravity**” theory not found yet

1998 - today



(1998)

Awarded to **Saul Perlmutter, Brian P. Schmidt** and **Adam G. Riess** "for the discovery of the accelerating expansion of the Universe through observations of distant supernovae." (1/2 + 1/4 + 1/4)

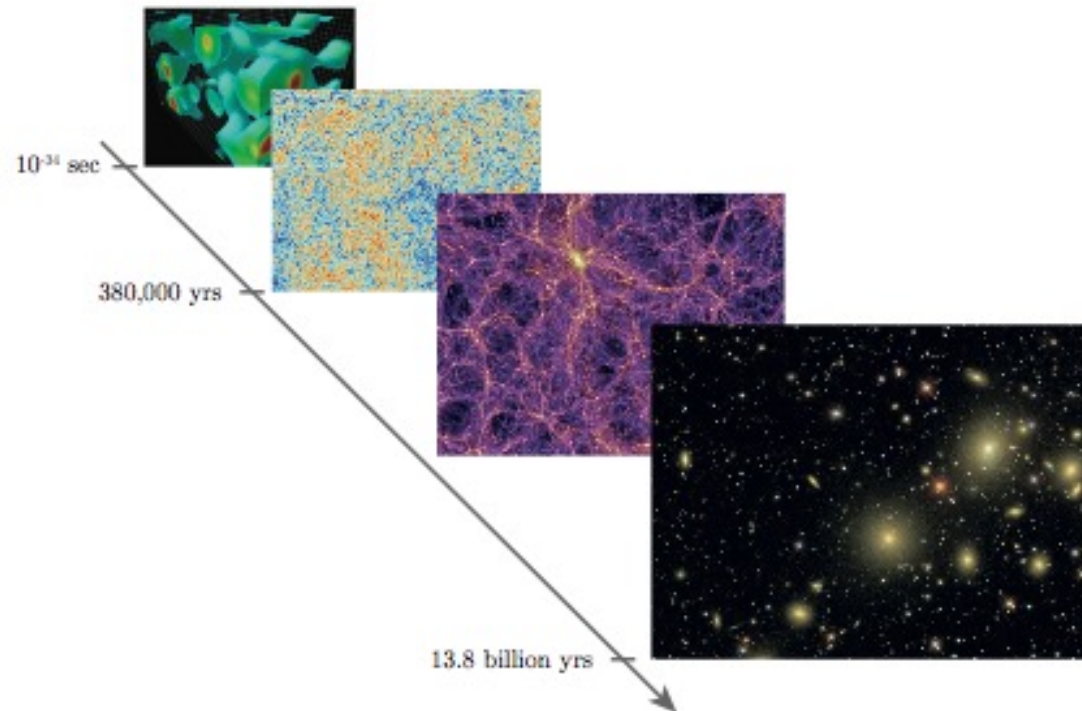


# $\Lambda$ CDM

the standard physical model of the Universe

General Relativity + Big Bang + Inflation + Gravitational clustering + cosmological fluid that includes dark matter of the type cold and dark energy of the type cosmological constant.

This physical model has been the standard model of the Universe since the beginning of the XXI<sup>st</sup> century and it is known as  $\Lambda$ CDM.



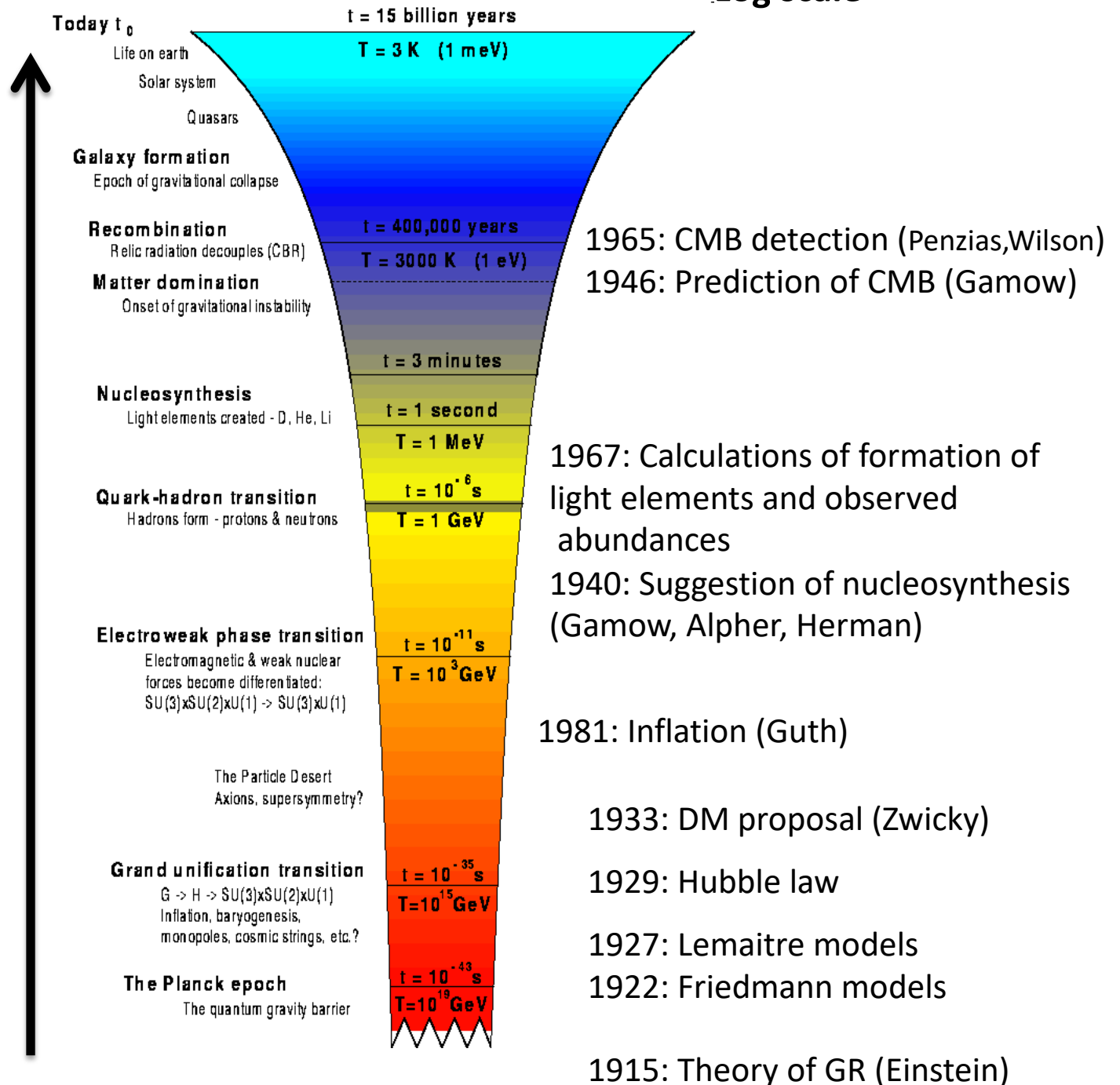
# Cosmic timeline

Log scale

Stable particles are the only ones left: photons, neutrinos, protons, neutrons, electrons, DM particles.

During the thermal history, the various species gradually decouple (leave the equilibrium) as their reaction rates become smaller than the expansion rate.

Inflation - mechanism introduced to solve some of the problems of the Big Bang model. It also provides the inhomogeneities initial conditions from quantum fluctuations.



# Linear scale

## History of the Universe



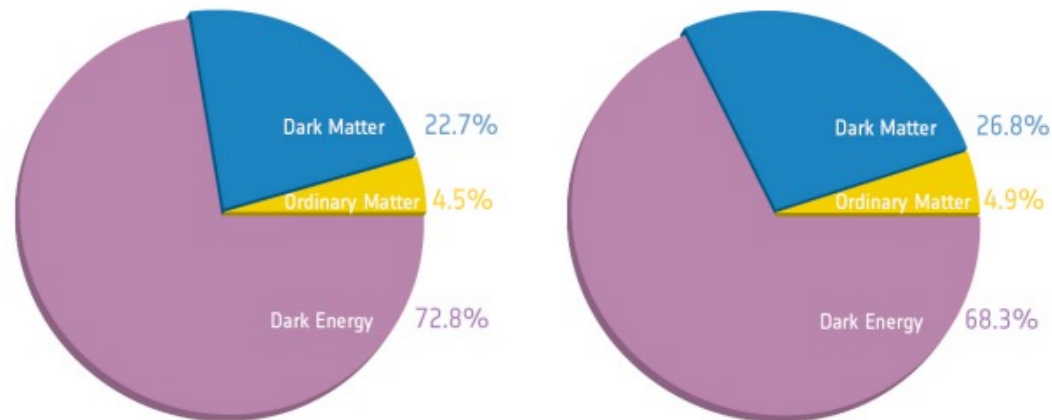
<p>2001: H<sub>0</sub> distance ladder (HST Key Project) (W. Freedman)</p> <p>1998: Accelerated expansion (SNIa)</p>	<p><b>Homogeneity</b></p>
<p>2005: Detection of the BAO peak (SDSS)</p> <p>2001: LSS map (SDSS, 2dFGRS) → SDSS IV (2019) → DESI (2024)</p> <p>2000: Weak lensing (LSS of DM) → DES (2021) → Euclid (2027)</p> <p>1986: The Great Wall (scale of homogeneity?)</p> <p>1970: Large-scale structure (first z-surveys of galaxies)</p>	<p><b>LSS</b></p>
<p>2006: Bullet Cluster (Chandra, Lensing) (DM observed?)</p> <p>1996: Nbody simulations (Virgo) (Universal profile NFW)</p> <p>1993: M<sub>b</sub> from clusters is 15% of M<sub>tot</sub> (S. White) (DE?)</p> <p>1982: X-ray cluster mass (Einstein satellite)</p> <p>1933: Cluster dynamics: DM needed (F. Zwicky)</p>	<p><b>Clusters</b></p>
<p>1996: z-evolution of Star-formation rate (HDF) (P. Madau)</p> <p>1986: First LSB galaxy</p> <p>1979: First gravitational lens system</p> <p>1974: Mass function (Press, Schechter) (NL collapse)</p> <p>1970: Rotation curves (DM also needed in galaxies) (V. Rubin)</p>	<p><b>Cosmic Noon</b></p>
<p>2024: Luminous early galaxies (record z=14.2) (JWST)</p> <p>2010: Cosmological HI 21cm (Pen) → SKA (&gt; 2027)</p> <p>1970s: Discovery of Ly-<math>\alpha</math> forest</p> <p>1965: Gunn-Peterson test (the universe is highly ionized)</p> <p>1963: Discovery of the first quasar (first high-z source)</p>	<p><b>Cosmic Dawn</b></p>
<p>2013: CMB high precision and polarization (Planck)</p> <p>2003: CMB small scales (WMAP)</p> <p>2000: CMB 1st peak (Boomerang, Maxima) (Universe flat)</p> <p>1992: Anisotropies of CMB (COBE) (DM also needed)</p> <p>1990: CMB Black-body (COBE) (Big Bang)</p>	<p><b>Dark ages</b></p>
<p>2016: Gravitational waves (LIGO) → LISA (2037)</p> <p>2002: Neutrino oscillations</p>	<p><b>Primordial</b></p>

## $\Lambda$ CDM parameters

$\Lambda$ CDM is a complex model. It is a theoretical construction supported by observations.

It includes a variety of physical processes that occur in a variety of epochs, in a variety of scales and contains a large number of free parameters – the **cosmological parameters** - that need to be fixed by the observations.

The values of the cosmological parameters determine the details of the expansion of the Universe and the evolution and formation of its large-scale structures → **they determine the "cosmology"**.



Before Planck

After Planck

Parameter	Planck+WP		Planck+WP+highL		Planck+lensing+WP+highL		Planck+WP+highL+BAO	
	Best fit	68% limits	Best fit	68% limits	Best fit	68% limits	Best fit	68% limits
$\Omega_b h^2$	0.022032	$0.02205 \pm 0.00028$	0.022069	$0.02207 \pm 0.00027$	0.022199	$0.02218 \pm 0.00026$	0.022161	$0.02214 \pm 0.00024$
$\Omega_c h^2$	0.12038	$0.1199 \pm 0.0027$	0.12025	$0.1198 \pm 0.0026$	0.11847	$0.1186 \pm 0.0022$	0.11889	$0.1187 \pm 0.0017$
$100\theta_{MC}$	1.04119	$1.04131 \pm 0.00063$	1.04130	$1.04132 \pm 0.00063$	1.04146	$1.04144 \pm 0.00061$	1.04148	$1.04147 \pm 0.00056$
$\tau$	0.0925	$0.089^{+0.012}_{-0.014}$	0.0927	$0.091^{+0.013}_{-0.014}$	0.0943	$0.090^{+0.013}_{-0.014}$	0.0952	$0.092 \pm 0.013$
$n_s$	0.9619	$0.9603 \pm 0.0073$	0.9582	$0.9585 \pm 0.0070$	0.9624	$0.9614 \pm 0.0063$	0.9611	$0.9608 \pm 0.0054$
$\ln(10^{10} A_s)$	3.0980	$3.089^{+0.024}_{-0.027}$	3.0959	$3.090 \pm 0.025$	3.0947	$3.087 \pm 0.024$	3.0973	$3.091 \pm 0.025$
$A_{100}^{PS}$	152	$171 \pm 60$	209	$212 \pm 50$	204	$213 \pm 50$	204	$212 \pm 50$
$A_{143}^{PS}$	63.3	$54 \pm 10$	72.6	$73 \pm 8$	72.2	$72 \pm 8$	71.8	$72.4 \pm 8.0$
$A_{217}^{PS}$	117.0	$107^{+20}_{-10}$	59.5	$59 \pm 10$	60.2	$58 \pm 10$	59.4	$59 \pm 10$
$A_{143}^{CIB}$	0.0	$< 10.7$	3.57	$3.24 \pm 0.83$	3.25	$3.24 \pm 0.83$	3.30	$3.25 \pm 0.83$
$A_{217}^{CIB}$	27.2	$29^{+6}_{-9}$	53.9	$49.6 \pm 5.0$	52.3	$50.0 \pm 4.9$	53.0	$49.7 \pm 5.0$
$A_{143}^{SZ}$	6.80	...	5.17	$2.54^{+1.1}_{-1.9}$	4.64	$2.51^{+1.2}_{-1.8}$	4.86	$2.54^{+1.2}_{-1.8}$
$r_{143 \times 217}^{PS}$	0.916	$> 0.850$	0.825	$0.823^{+0.069}_{-0.077}$	0.814	$0.825 \pm 0.071$	0.824	$0.823 \pm 0.070$
$r_{143 \times 217}^{CIB}$	0.406	$0.42 \pm 0.22$	1.0000	$> 0.930$	1.0000	$> 0.928$	1.0000	$> 0.930$
$\gamma^{CIB}$	0.601	$0.53^{+0.13}_{-0.12}$	0.674	$0.638 \pm 0.081$	0.656	$0.643 \pm 0.080$	0.667	$0.639 \pm 0.081$
$\xi^{tSZ \times CIB}$	0.03	...	0.000	$< 0.409$	0.000	$< 0.389$	0.000	$< 0.410$
$A^{kSZ}$	0.9	...	0.89	$5.34^{+2.8}_{-1.9}$	1.14	$4.74^{+2.6}_{-2.1}$	1.58	$5.34^{+2.8}_{-2.0}$
$\Omega_\Lambda$	0.6817	$0.685^{+0.018}_{-0.016}$	0.6830	$0.685^{+0.017}_{-0.016}$	0.6939	$0.693 \pm 0.013$	0.6914	$0.692 \pm 0.010$
$\sigma_8$	0.8347	$0.829 \pm 0.012$	0.8322	$0.828 \pm 0.012$	0.8271	$0.8233 \pm 0.0097$	0.8288	$0.826 \pm 0.012$
$z_{re}$	11.37	$11.1 \pm 1.1$	11.38	$11.1 \pm 1.1$	11.42	$11.1 \pm 1.1$	11.52	$11.3 \pm 1.1$
$H_0$	67.04	$67.3 \pm 1.2$	67.15	$67.3 \pm 1.2$	67.94	$67.9 \pm 1.0$	67.77	$67.80 \pm 0.77$
Age/Gyr	13.8242	$13.817 \pm 0.048$	13.8170	$13.813 \pm 0.047$	13.7914	$13.794 \pm 0.044$	13.7965	$13.798 \pm 0.037$
$100\theta_s$	1.04136	$1.04147 \pm 0.00062$	1.04146	$1.04148 \pm 0.00062$	1.04161	$1.04159 \pm 0.00060$	1.04163	$1.04162 \pm 0.00056$
$r_{drag}$	147.36	$147.49 \pm 0.59$	147.35	$147.47 \pm 0.59$	147.68	$147.67 \pm 0.50$	147.611	$147.68 \pm 0.45$

**fundamental  
cosmological  
parameters**

**nuisance  
parameters  
(of a  
particular  
cosmological  
probe)**

**derived  
cosmological  
parameters**

# $\Lambda$ CDM problems

**The description of the Universe is far from being finished!**

## **Theoretical development**

- Details of the non-linear structure formation are not well understood
- The LSS is not completely described yet (high-order correlations)
- Relativistic effects not completely studied (larger scales)

## **Observations and interpretation**

- Many observations suffer from systematic effects
- Different observations are well fitted by the model predictions but for different and inconsistent parameter values  $\rightarrow$  the Hubble tension
- Many alternative DE models also fit the data
- Test the assumptions (e.g. cosmological principle)

## **Fundamental concepts**

- Nature of dark matter still unknown
- Nature of dark energy still unknown



# Plan of the course: studying the physical model of the Universe

## The Homogeneous Universe

geometry, dynamics, age, distances, cosmological parameters, contents of the Universe (dark matter, dark energy, radiation, baryonic matter)

## Testing the Homogeneous Universe: *probes of geometry*

standard candles (SN), standard rulers (BAO), standard abundances, distance ladder ( $H_0$ ), densities (lensing, dark matter), estimators, biases, statistical inference (Fisher matrix, MCMC)

## The Inhomogeneous Universe

linear spatial perturbations, random fields, structure formation, power spectra of dark/baryonic matter, non-linear structure

## Testing the Inhomogeneous Universe: *probes of structure*

weak gravitational lensing (cosmic shear), galaxy clustering, CMB anisotropies

There is no single textbook covering all aspects of the course at the level intended. So, the **main resource** are the lecture notes:

I. Tereno - *Cosmologia Fisica lecture notes* -

**LECTURE NOTES** ~1000 slides

<https://fenix.ciencias.ulisboa.pt/courses/cfis-2254879305243175/lecture-notes>

Introduction

00: A physical model for the Universe

Fundamental concepts

01: The zeroth order Universe

02: The metric and its degrees of freedom

03: The cosmological fluid

04: The background evolution

05: The energy density budget

06: The density contrast random field

07: Statistical properties of the density contrast field

08: Parameterization of the density contrast field

Structure formation

09: Newtonian perturbed fluid equations

10: Dark matter linear clustering

11: Baryonic matter linear clustering

12: Non-linear clustering

13: Perturbations in general relativity

14: The Einstein-Boltzmann equations

Cosmological observations

15: Cosmological probes

16: Supernova surveys

17: Statistical inference

18: Cosmological parameter estimation

19: Cosmic microwave background

20: Galaxy clustering

21: Gravitational lensing

22: Weak gravitational lensing

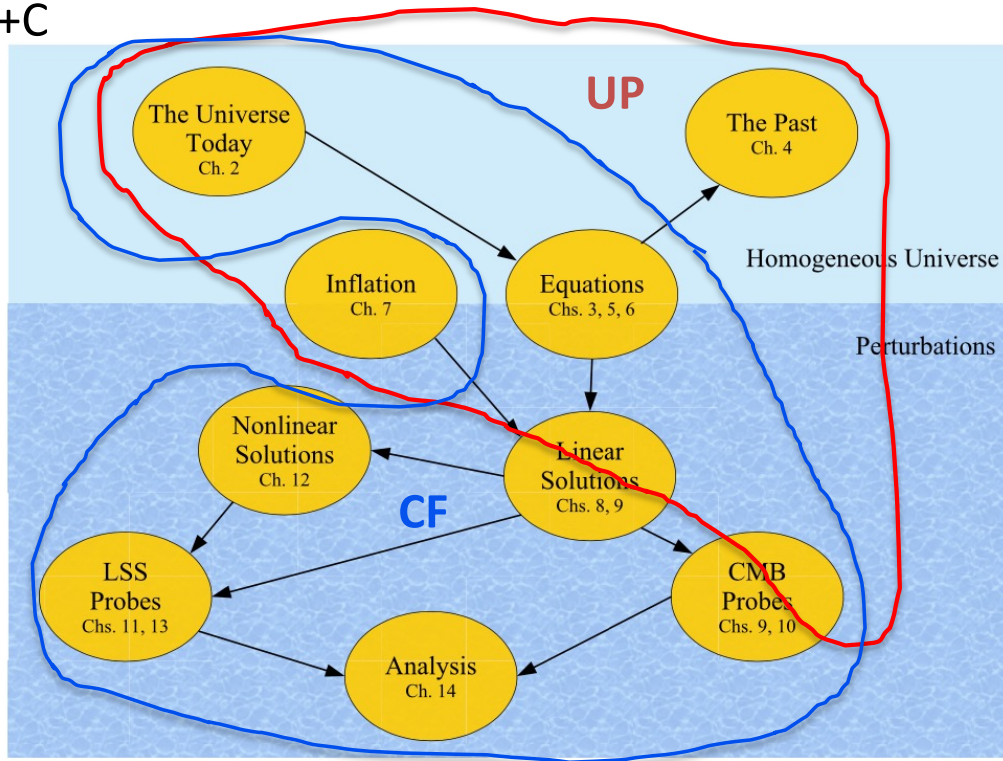
# Cosmology sub-divisions A, B, C and how different is this course from Primordial Universe

Time	Temperature (K)	Event
<b>The Quantum Gravity Era</b>		
$1 \times 10^{-43}$ s (Planck time)	$1 \times 10^{32}$	quantum limit of general relativity
<b>The Inflation Era</b>		
$1 \times 10^{-35}$ s	$1 \times 10^{28}$	grand unification symmetry breaking
$1 \times 10^{-34}$ s	$1 \times 10^{27}$	start of inflation
$1 \times 10^{-32}$ s	$1 \times 10^{27}$	start of reheating and end of inflation
$1 \times 10^{-11}$ s	$3 \times 10^{15}$	ew unification symmetry breaking
<b>The Quark-Lepton Era</b>		
$1 \times 10^{-5}$ s	$2 \times 10^{12}$	formation of hadrons from quarks
0.1 s	$3 \times 10^{10}$	neutrinos decouple
1 s	$1 \times 10^{10}$	neutron to proton ratio freezes out
10 s	$5 \times 10^9$	electron positron annihilation
<b>The Radiation Era</b>		
3 min	$1 \times 10^9$	nucleosynthesis begins
30 min	$4 \times 10^8$	nucleosynthesis ends
2000 anos	$6 \times 10^4$ ( $z \approx 10^4$ )	matter-radiation equivalence
<b>The Matter Era</b>		
10 mil anos (the plasma epoch)	$1 \times 10^4$	matter is fully ionized
300 mil anos	$3.5 \times 10^3$	electrons and protons recombine
400 mil anos	$3.0 \times 10^3$ ( $z \approx 1100$ )	photon decoupling (last scattering surface)
400 milhoes de anos	( $z \approx 15$ )	first bound structures form formation of intergalactic medium first dark halos of galaxies first stars (first heavy elements) clusters filaments and voids
<b>The Dark Energy Era</b>		
13.6 mil milhoes de anos	2.726	today

Primordial Universe

Physical Cosmology

B+C



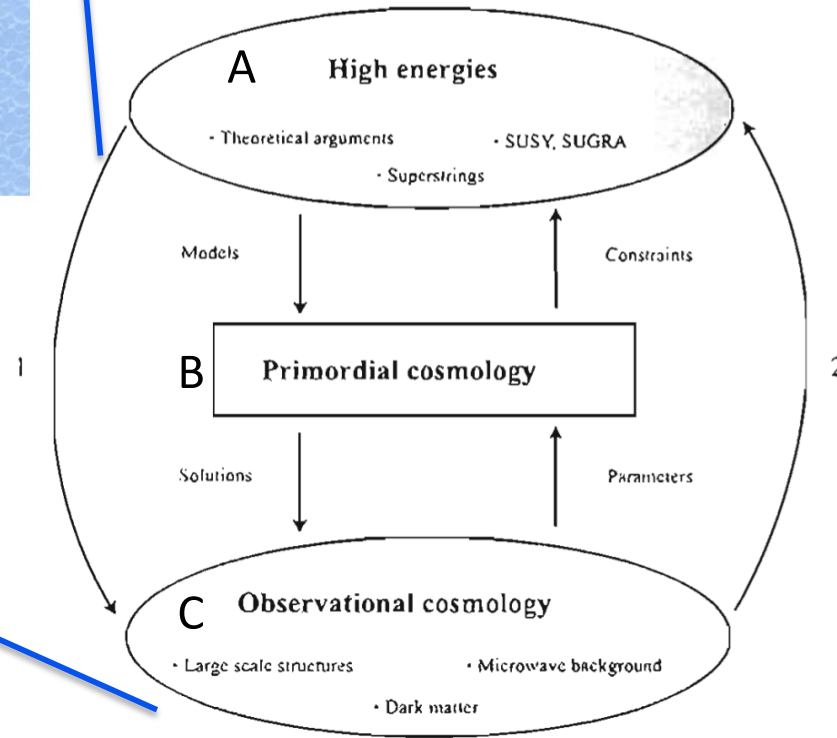
(from Dodelson and Schmidt)

B. Theoretical: B0: homogeneous universe (expansion), B1: inhomogeneous universe (structure formation, statistical description)

C. Theoretical: cosmological probes, statistical description, estimators, simulations

### The 3 sub-divisions of theoretical cosmology

A. Theoretical : field theory, particle physics, dark energy models, modified gravity



(from Peter and Uzan)

## Other bibliography

There are many good cosmology **textbooks** that provide good explanations of some aspects, or that go into greater depth in some topics.

- P. Peter and J.P. Uzan - *Primordial Cosmology* (2009) - Ch. 3,5 (homogeneous and inhomogeneous Universe -B-), Ch. 6,7 (cosmological probes -C-), other chapters focus on -A-

- L. Amendola and S. Tsujikawa - *Dark Energy* (2010), Ch. 2,3,4,12 (homogeneous and inhomogeneous Universe -B-), Ch 5,14 (cosmological probes -C-), Ch. 13 (statistical methods -C-), other chapters focus on -A-

- Y. Wang - *Dark Energy* (2010) - Ch. 1,2 (a quick summary of relevant aspects of -B-), Ch. 4-7 (details on the main cosmological probes -C-)

- S. Dodelson and F. Schmidt - *Modern Cosmology* 2<sup>nd</sup> ed. (2021), the full book gives a very detailed and complete coverage of the inhomogeneous Universe and the theoretical aspects of observational cosmology (more advanced level -B,C-)

- P. Schneider - *Extragalactic Astronomy and Cosmology - an introduction* (2006), Ch. 4,7,8 give a rigorous but less advanced description of the homogeneous Univ, inhomogeneous Univ and cosmological probes (more introductory level -B,C-)

- P. Coles and F. Lucchin - *Cosmology* 2<sup>nd</sup> ed. (2002), Ch. 1,2,4,10-19 covers most aspects of the course at a less advanced and also more outdated level (-B,C-)

There are also many good **lecture notes** from cosmology courses from universities around the world, that can be found on-line.

- Luca Amendola (B,C)
- Daniel Baumann – detailed calculations (B, some A)
- Tobias Baldauf – theory of observational cosmology (a good resource for the theoretical aspects of C)
- Julien Lesgourgues – detailed description of inhomogeneous Universe (B)
- Hannu Kurki-Suonio - detailed description of inhomogeneous Universe (B)
- Matthias Bartelmann – less advanced level
- Michael Hudson – less advanced level