



#### Dark matter

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#### Dark Matter, Phase transitions and Gravitational Waves



#### Brief history of the universe

#### The early years

In the "beginning" the was a hot and dense universe. The interactions between particles were frequent and energetic. Then, the primordial plasma cooled and the light elements were formed (hydrogen, helium and lithium).

With the drop in energy the first stable atoms appeared. This is also the moment when photons started to roam freely.

What we see today is the microwave radiation from this afterglow. The radiation is nearly uniform (about 2.7 K) in all directions.

There are however small variations in the cosmic microwave background in temperature at a level of 1 part in 10 000. These fluctuations reflect tiny variations in the primordial density of matter.

Over time, and under the influence of gravity, these matter fluctuations grew. Dense regions were getting denser. Eventually, galaxies, stars and planets formed.

However what we "see" today as matter and energy is barely what we have access to in experiments on earth. Most of the universe today consists of forms of strange matter and energy.

Dark matter is required to explain the <u>stability of galaxies</u> and the <u>rate of formation of the</u> <u>large-scale structure of the universe</u>. Dark energy is required to rationalise the striking fact that the <u>expansion of the universe started to accelerate recently</u> (meaning a few billion years ago). What dark matter and dark energy are is still a mystery.

Finally, there is growing evidence that the primordial density perturbations originated from microscopic quantum fluctuations, stretched to cosmic sizes during a period of inflationary expansion. The physical origin of inflation is still a topic of active research.

#### So what now?

**Missing ingredients:** 

Dark matter - no good dark matter candidates in the SM

Mater-antimatter asymmetry - more CP violation is needed

Neutrino masses...

Unexplained experimental results:

Muon magnetic moment

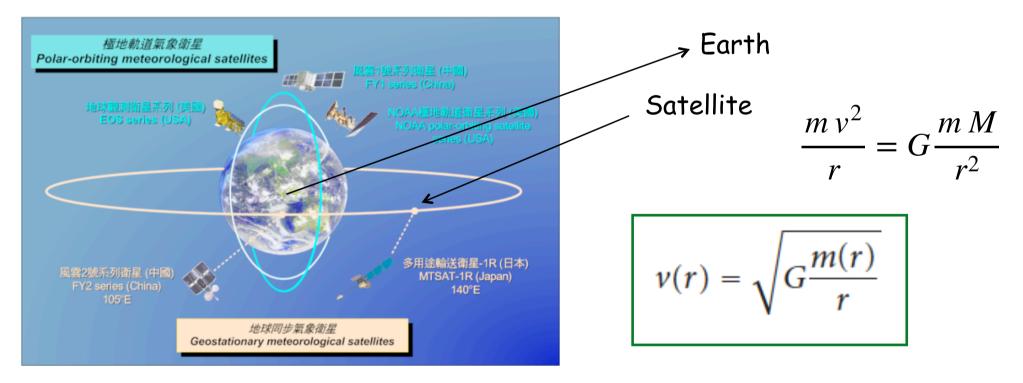


There is also gravity and dark energy

#### The early years

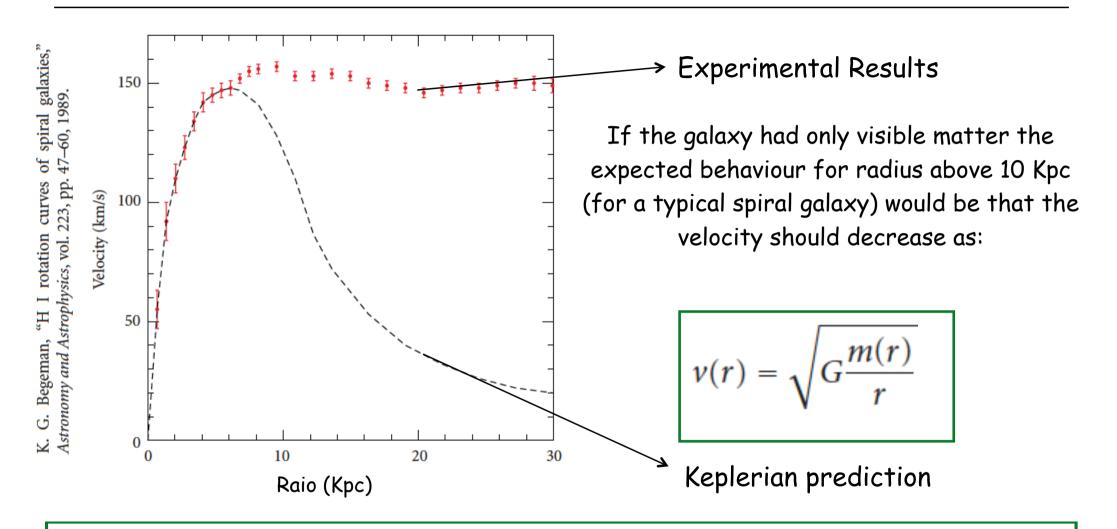
Fritz Zwicky (1930) When discussing the discrepancy between the observed and the expected rotation velocity of galaxies.

"Should this turn out to be true, the surprising result would follow that <u>dark matter</u> is present in a much higher density than radiating matter."



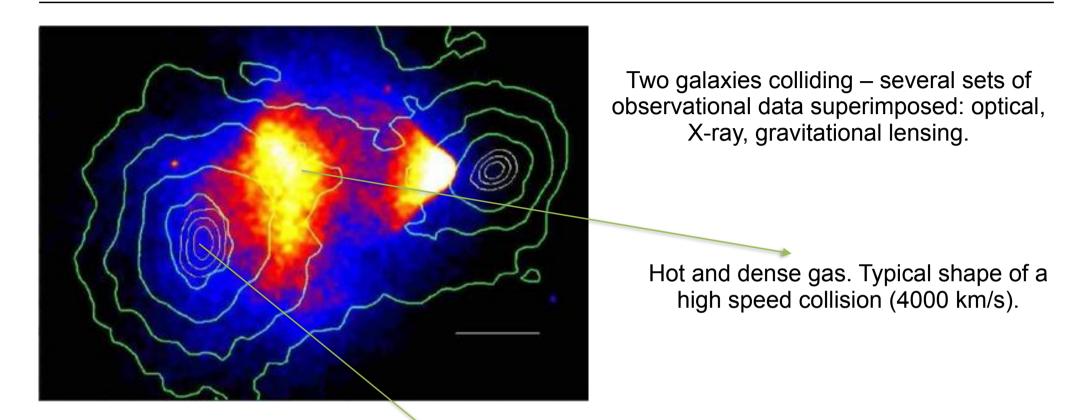
At a distance of 640 Km, the satellite has a velocity of 27000 Km/h.

#### Rotation curves of galaxies



Contrary to luminosity, mass is not concentrated close to centre of spiral galaxies. The distribution of light does not match the distribution of mass.

#### The Bullet Cluster



Lines of gravitation potential – from gravitational lensing show that the dark matter is concentrated around the galaxies and that it is not affected by the collisions.

Dark matter interacts very weakly!

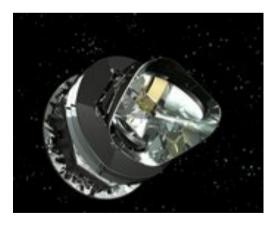
#### The Cosmic Microwave Background

In the Standard Model of Cosmology, it is assumed that just after the Big Bang the Universe was extremely hot, it then inflated (very rapidly) and cooled down. One effect of the rapid cooling was predicted to be a very low temperature radiation that would populate all space until today.

In 1965, astronomers Arno Penzias e Robert Wilson found (by accident – or so they say) an isotropic radiation of 2.725 Kelvin (- 270° C) (Nobel Prize 1978).

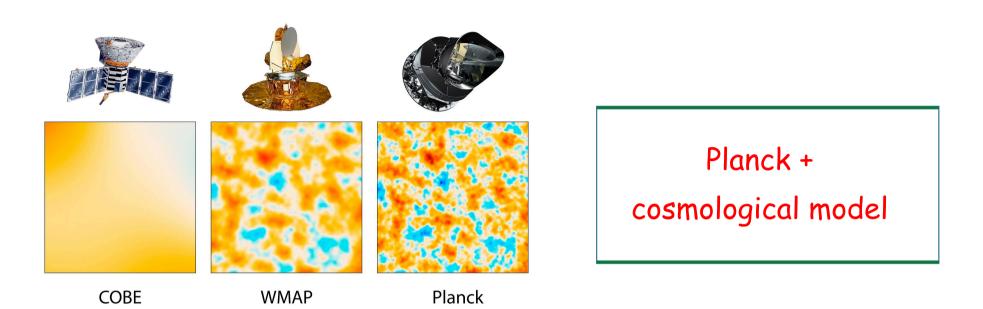


### What can we learn from the CMB?



Planck

#### The Cosmic Microwave Background



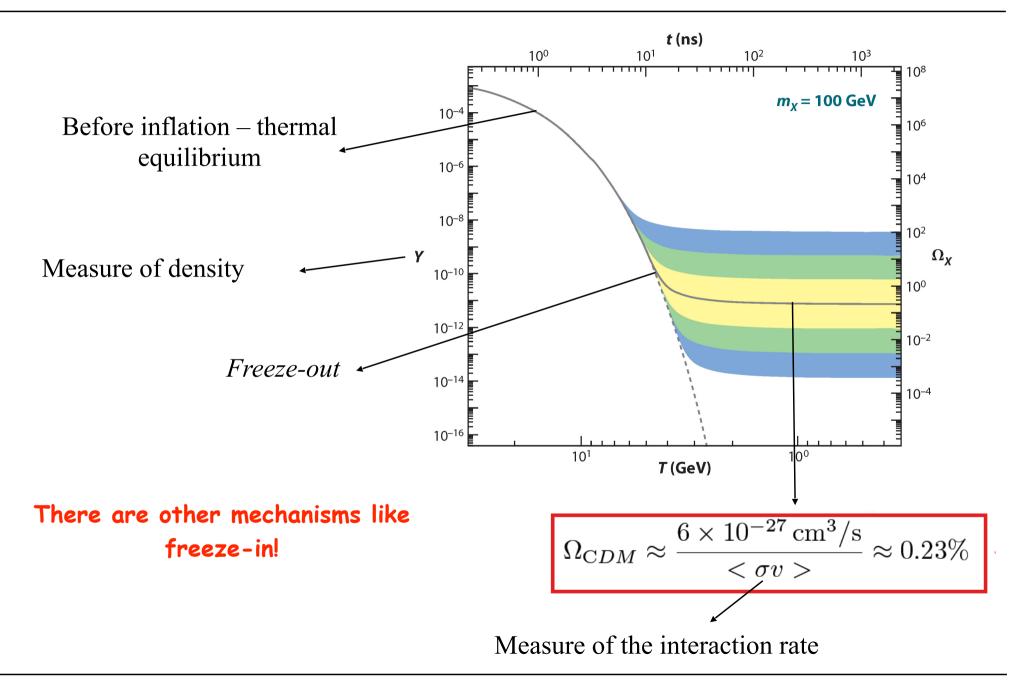
## Fluctuation in the Cosmic Background Radiation are due to the matter density fluctuations in the early Universe.

Once upon a time all particles were in thermal equilibrium.

As the Universe expanded and cooled, the rate of interactions was not enough to maintain thermal equilibrium (freeze out).

The unstable particles disappeared (decayed); number of stable particles reached a constant (thermal relic density) which has still approximately the same value today.

#### What happened to dark matter?



• It completely changes our perception of the universe. Just a while ago we thought all matter was made of essentially the same stuff.

• It is the most interdisciplinary (inside physics) subject as it needs general relativity, nuclear physics, particle physics, cosmology, classical physics (thermodynamics and mechanics...)

• Mystery - "we know" it exists, "we know where it is", we have some hints on how it behaves but we do not know what it is ...

Why is dark matter so interesting?

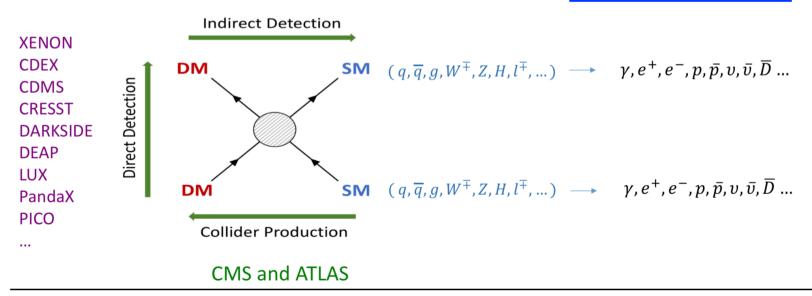
#### • Massive, stable, neutral, weak (or none) interaction with SM



WIMP - weakly interacting massive particles/ Many other possibilities - essentially no mass limits/ all spins possible

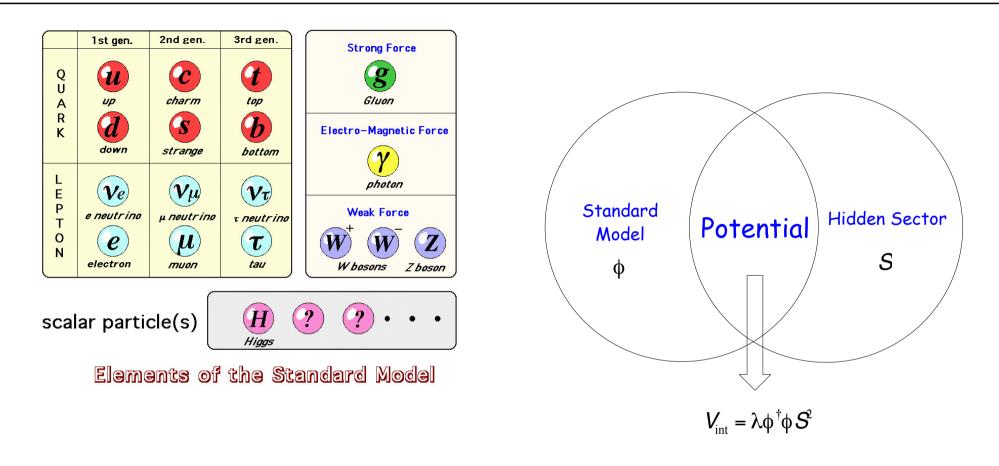
#### HESS, HAWC, VERITAS, MAGIC, IceCube,... PAMELA, FERMI, CALET, DAMPE, AMS, ...

Searches for DM



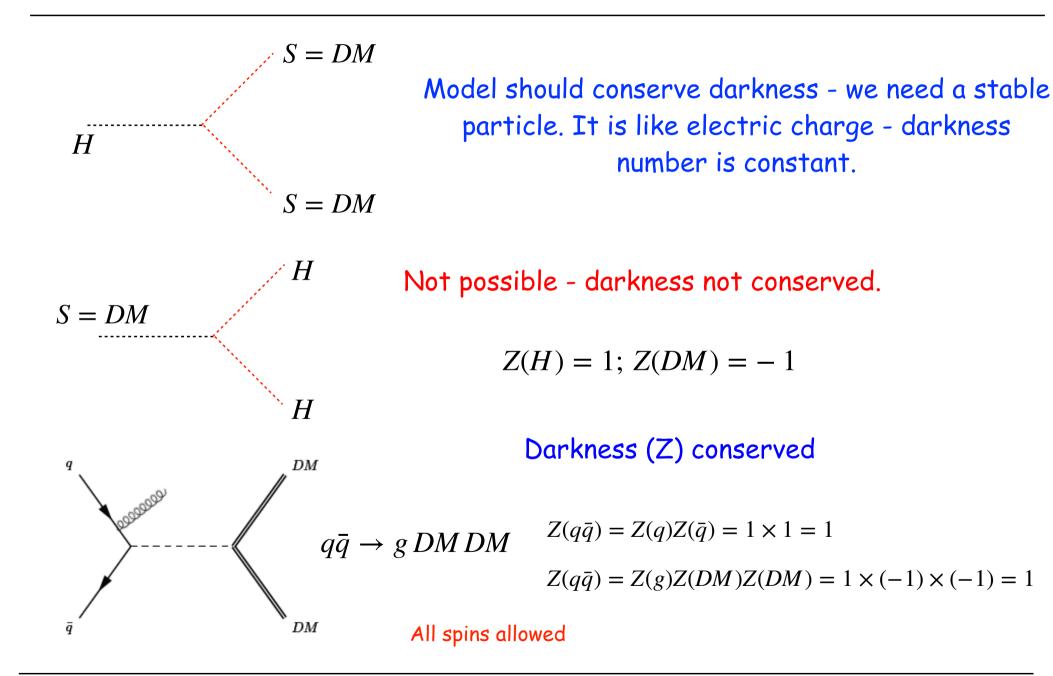
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#### Extensions of the SM - a new model is needed

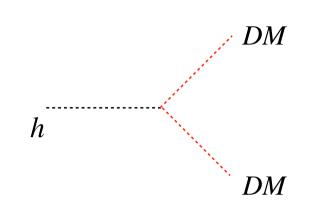


Lagrangian term that links the SM with the hidden sector. Dark Matter particle has to be stable. Can be done with a new quantum number.

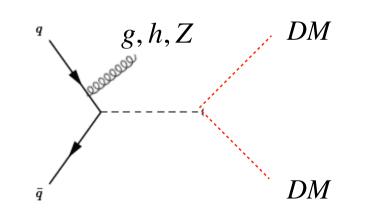
#### Conserved quantities - <u>darkness</u>



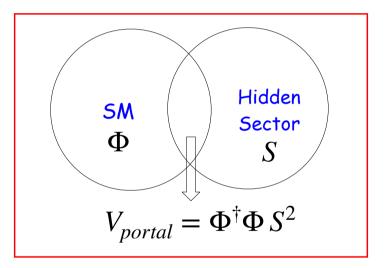
#### Dark Matter (IDM)



Searches need some kind of handle



Model should conserve "darkness" - we need a stable particle. The invisible width of the Higgs and the dark matter direct detection experiments set a bound on the so-called portal coupling(s).

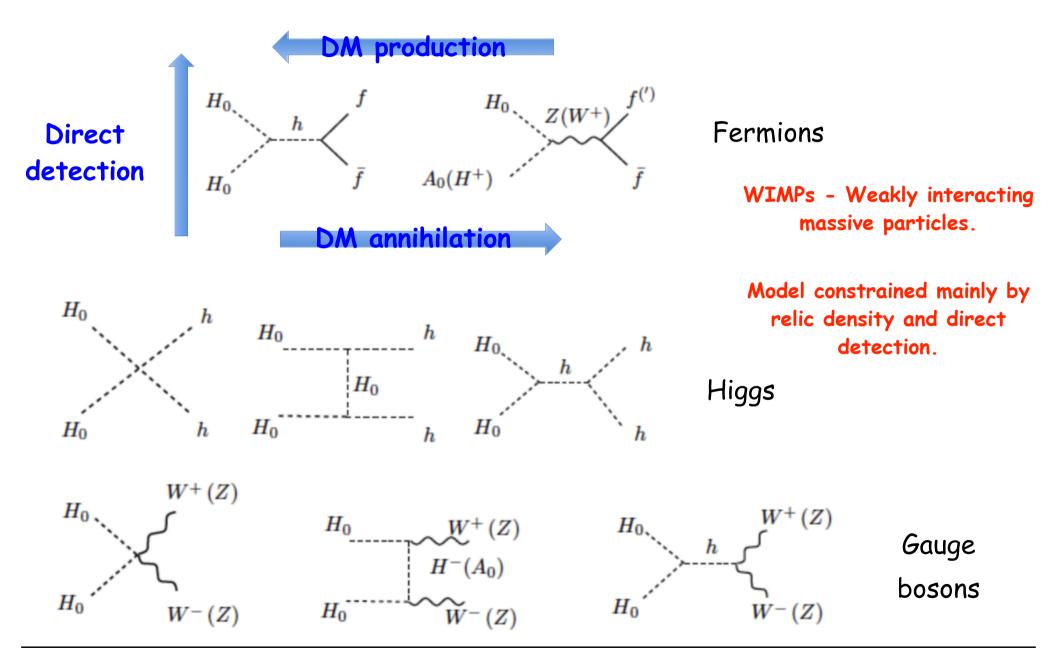


 $q\bar{q} \rightarrow (g, h, Z, \dots) DMDM$ 

 $Z(q\bar{q}) = Z(q)Z(\bar{q}) = 1 \times 1 = 1$ 

 $Z(q\bar{q}) = Z(H)Z(DM)Z(DM) = 1 \times (-1) \times (-1) = 1$ 

#### Dark Matter (IDM)



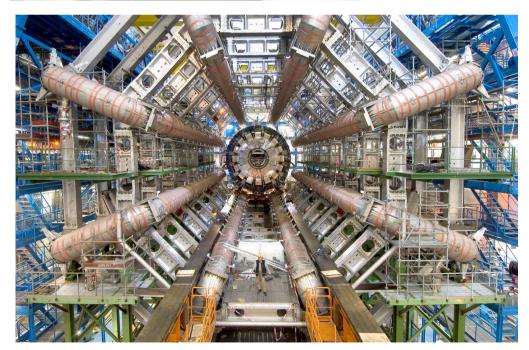
#### A collider is useful

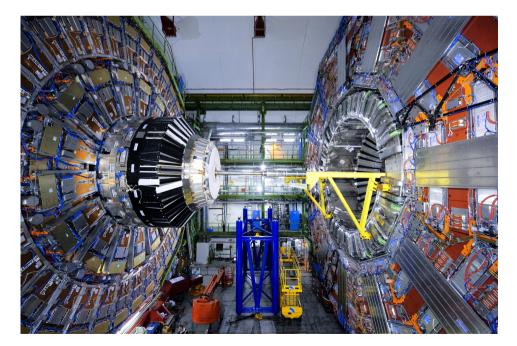
#### Where the protons travel



People





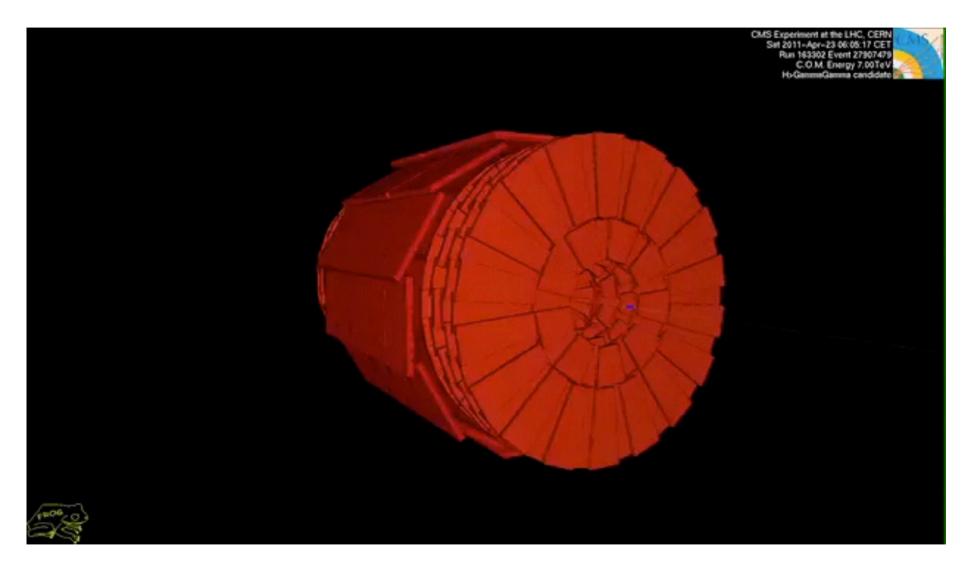


ATLAS

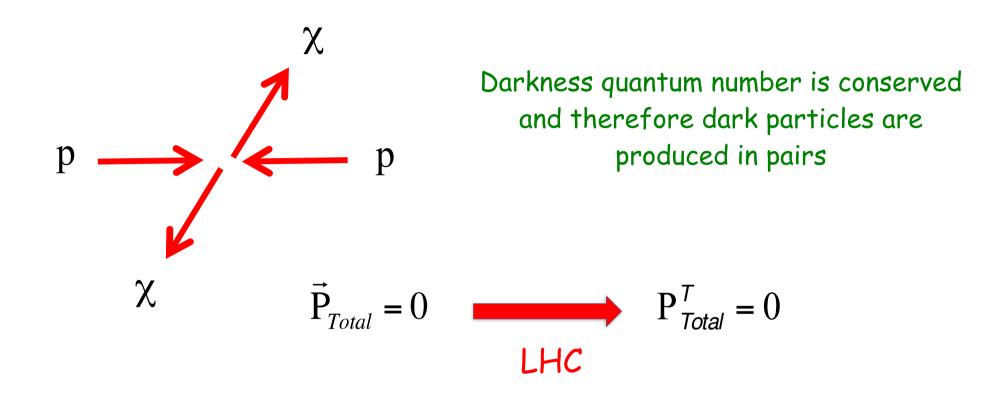
CMS

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#### Particles collide...



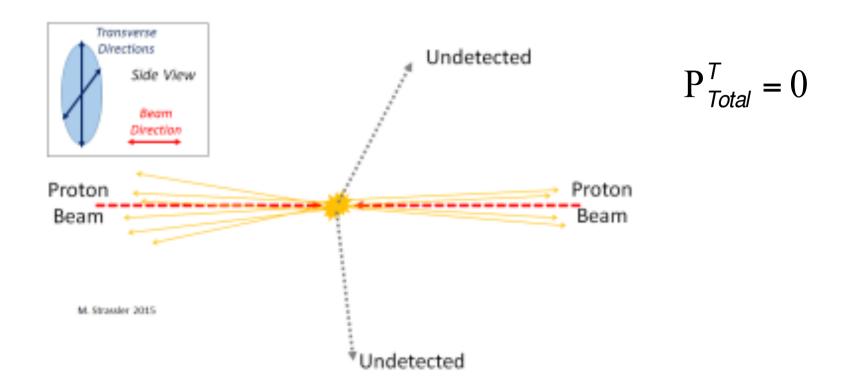
#### Back to the LHC - Dark matter production



But dark matter does not interact (or it does but very weakly) with the SM particles. We see nothing!

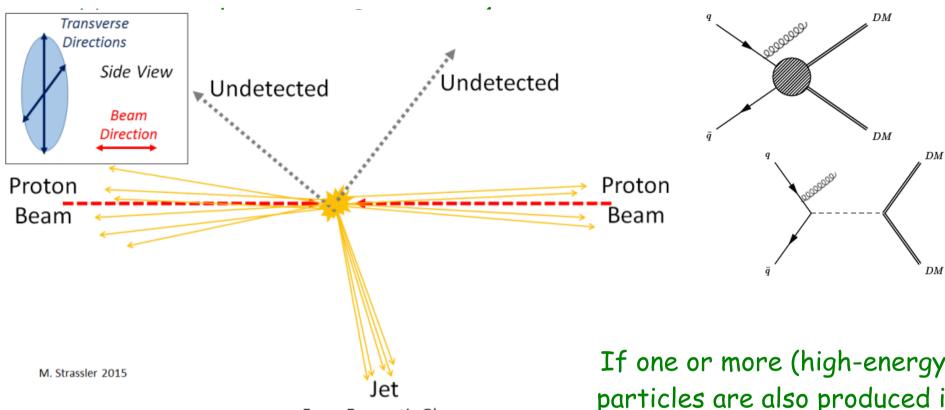
There will be MET - but still we see nothing!

#### Back to the LHC - Dark matter production



# So the scenario where only dark matter is produced cannot simply be probed at any level.

Mono-X (X = Z, jet, Higgs...)

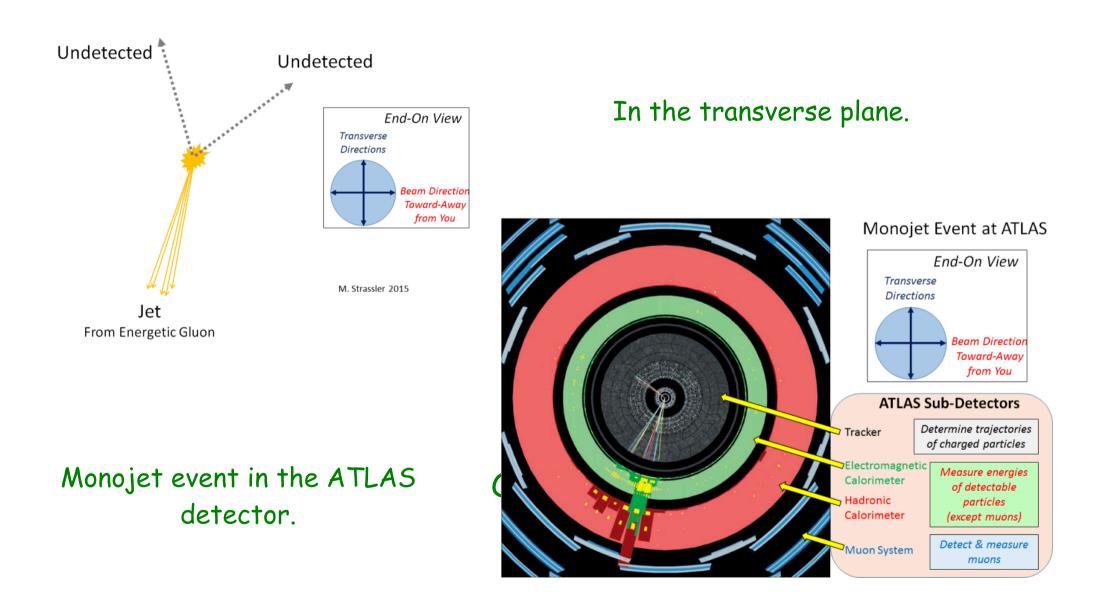


From Energetic Gluon

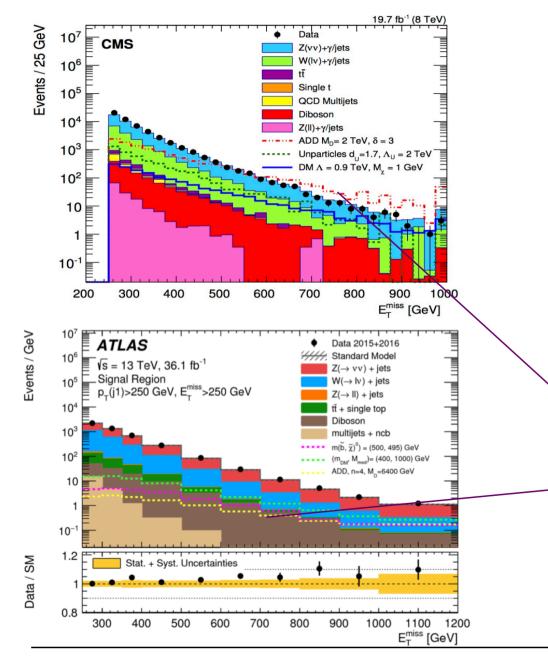
# However, this can also be MET from neutrinos.

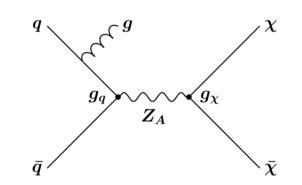
If one or more (high-energy) particles are also produced in the process then we have a mono-X (multi-X - still called mono-X) event! The X (for instance a jet) has a very large pT.

#### A monojet in ATLAS



#### Mono-jet model interpretation in CMS



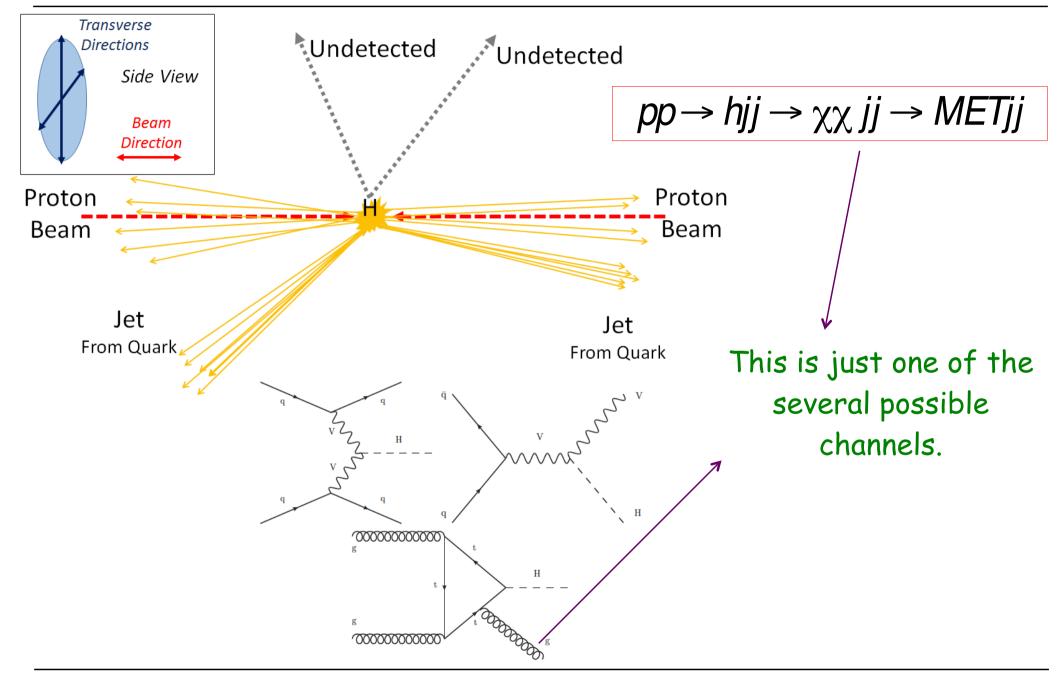


We know the SM background. This particular case is for an effective vertex with gluons.

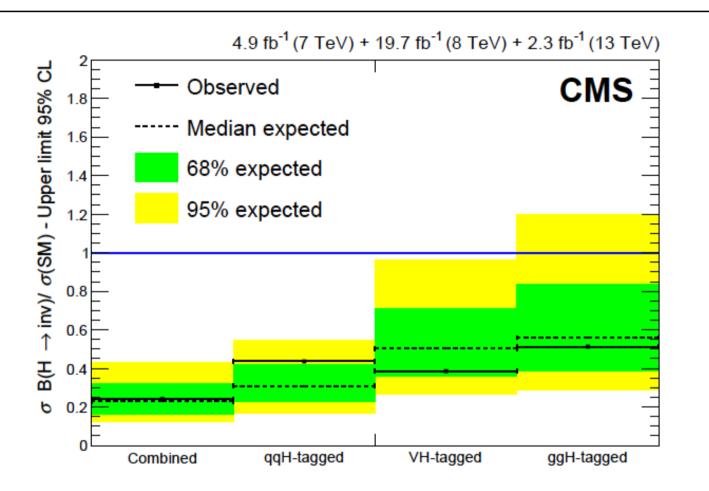
Dark matter line for a given cross section and mass of dark matter.

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#### Another possibility



#### Invisible decays

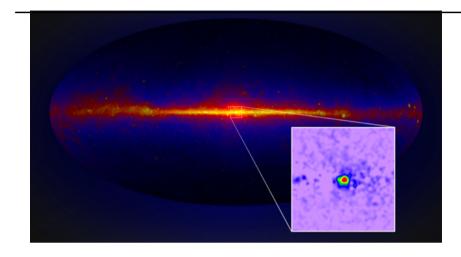


CMS results for the exclusion in the different channels

Assuming a SM production cross section for the Higgs boson, CMS obtains a limit

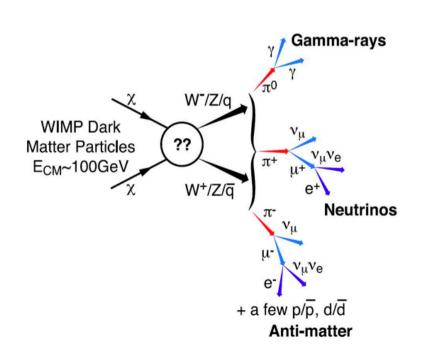
 $\mathcal{B}(H \rightarrow inv) < 0.24 \ (0.23)$  at the 95% CL

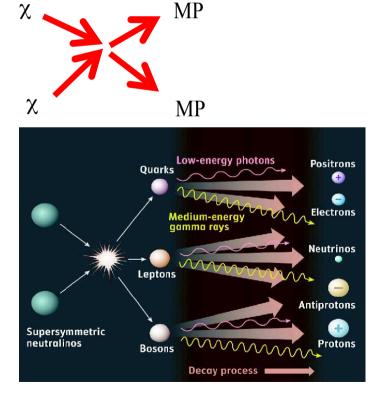
#### Indirect detection



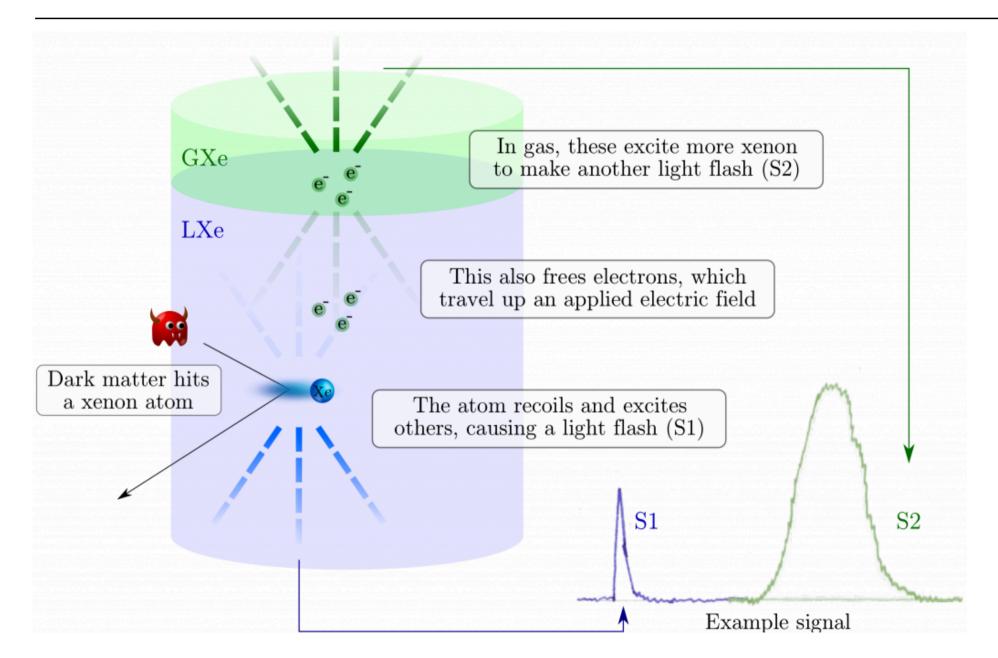
The Fermi Large Area Telescope (LAT) detects gamma radiation with energies between 0.3 and 300 GeV. It also detects electrons and positrons.

WIMPs collide producing either photons or particle anti-particle pairs.

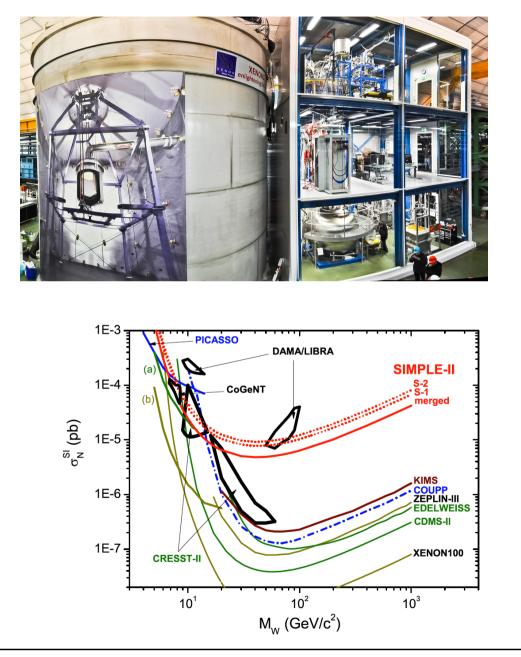


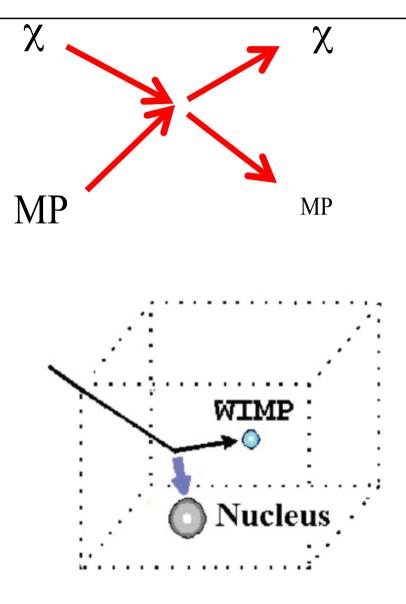


#### **Direct detection**



#### **Direct detection**

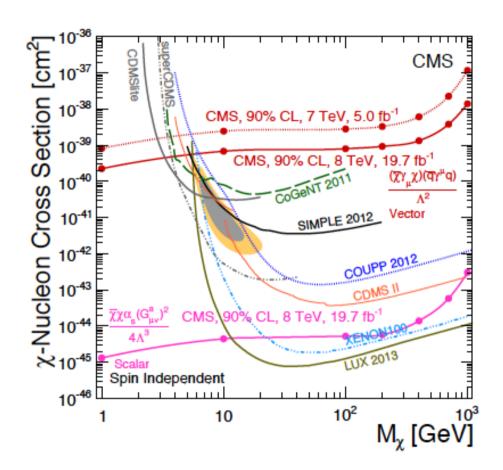


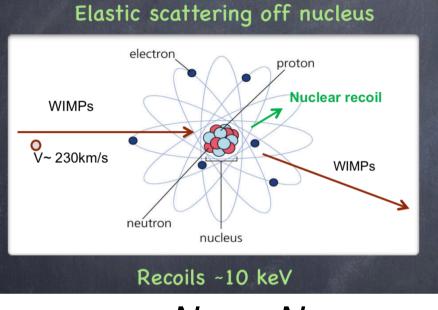


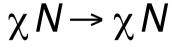
WIMP collides with nucleus - recoil energy can be measured.

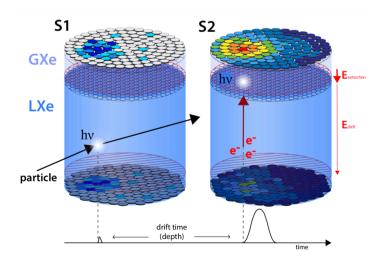
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#### Direct detection vs. LHC



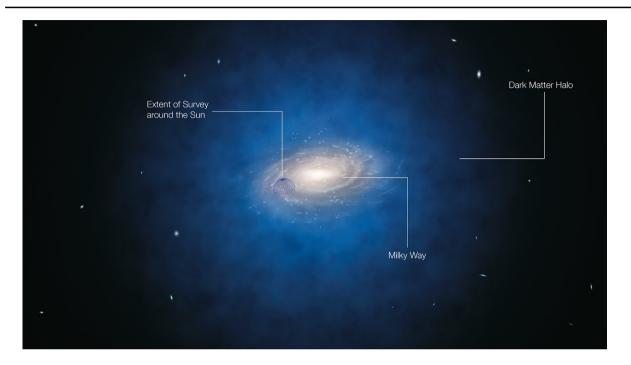






Xenon

#### Halos

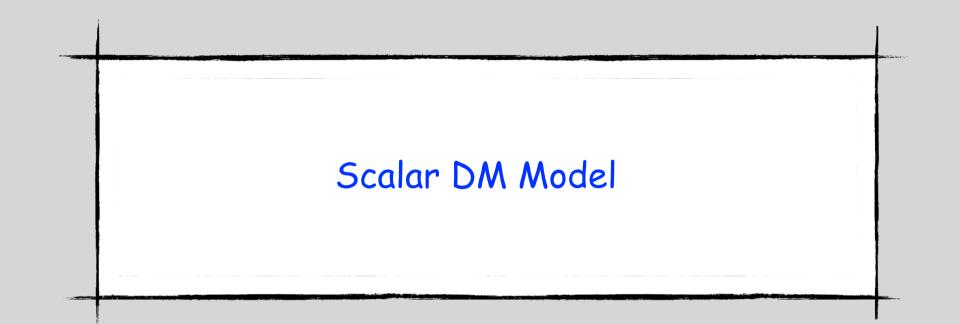


The visible disk of the Milky Way Galaxy is thought to be embedded in a much larger, roughly spherical halo of dark matter. The dark matter density drops off with distance from the galactic center.

It is now believed that about 95% of the galaxy is composed of dark matter. The luminous matter makes up approximately 9×10<sup>10</sup> solar masses. The dark matter halo is likely to include around 6×10<sup>11</sup> to 3×10<sup>12</sup> solar masses of dark matter. A 2014 analysis of stellar motions calculated the dark matter density (at the sun's distance from the galactic centre) = 0.0088 (+0.0024 -0.0018) solar masses/parsec^3.

The radial velocity dispersion shows an almost constant value of 120 km/s out to 30 kpc and then continuously declines down to 50 km/s at about 120 kpc. This fall-off puts important constraints on the density profile and total mass of the dark matter halo of the Milky Way.

# The simplest DM models



#### The spin 0 extension - real

The SM is extended by an extra real scalar singlet S. The most general Lagrangian we can write is

$$\mathscr{L} = \mathscr{L}_{SM} + \frac{1}{2} (\partial_{\mu} S) (\partial^{\mu} S) - aS - bS^2 - cS^3 - dS^4 - \kappa_1 SH^{\dagger}H - \kappa_2 SH^{\dagger}H - \mu^2 H^{\dagger}H - \lambda (H^{\dagger}H)^2$$

with (in the unitary gauge)

$$H = \begin{pmatrix} 0 \\ h \end{pmatrix}$$

If we include the  $Z_2$  symmetry  $S \rightarrow -S$ , the potential reduces to

$$V_N = bS^2 + dS^4 + \kappa_1 S^2 H^{\dagger} H + \mu^2 H^{\dagger} H + \lambda (H^{\dagger} H)^2$$

The minimum conditions for the potential are

$$\begin{cases} \frac{\partial V}{\partial S} = 2bS + 4dS^3 + 2\kappa_1 Sh^2 = 0\\ \frac{\partial V}{\partial h} = 2h\mu^2 + 4\lambda h^3 + 2\kappa_1 S^2 h = 0 \end{cases}$$

This set equation has four solutions

1) S = 0; h = 0; 2) S = -b/(2d); h = 0; 3)  $S = 0; h^2 = -\mu^2/(2\lambda);$  4)  $S \neq 0; h \neq 0$ 

The first is the symmetric solution. So SSB does not occur. This is also true for solution 2. Solution 3 is the DM + SM one. In solution 4 the dark symmetry is broken by the vacuum.

P: Show that solution 3) has a DM candidate

P: Why doesn't SSB occur is scenario 2)?

P: Find solution 4) explicitly; find the mass eigenstates in this scenario; is there a DM candidate?

# The spin 0 extension - complex

Let us now consider the extension by a complex singlet S. The most general Lagrangian we can write is

$$\mathscr{L} = \mathscr{L}_{SM} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} - \lambda_{S} \left| \mathbb{S} \right|^{4} - \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H + \mu^{2} (\mathbb{S}^{2} + \mathbb{S}^{*2}) \qquad \mathbb{S} = \frac{1}{\sqrt{2}} (v_{S} + S + iA)$$

Model	Phase	VEVs at global minimum	
$\mathbb{U}(1)$	Higgs+2 degenerate dark	$\langle \mathbb{S}  angle = 0$	
	2  mixed + 1  Goldstone	$\langle A \rangle = 0 \ (\mathbb{M}(1) \to \mathbb{Z}_2')$	
$\mathbb{Z}_2 \times \mathbb{Z}'_2$	Higgs + 2 dark	$\langle \mathbb{S}  angle = 0$	
	$2 \operatorname{mixed} + 1 \operatorname{dark}$	$\langle A \rangle = 0 \ (\mathbb{Z}_2 \times \mathbb{Z}'_2 \to \mathbb{Z}'_2)$	
$\mathbb{Z}_2'$	$2 \operatorname{mixed} + 1 \operatorname{dark}$	$\langle A \rangle = 0$	
	3 mixed	$\langle \mathbb{S}  angle  eq 0 \ (\mathbb{Z}_2')$	

# The spin 0 extension - complex

One particular case: black Lagrangian is U(1) symmetric. Black plus red

$$\mathcal{L} = \mathcal{L}_{SM} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} - \lambda_{S} \left| \mathbb{S} \right|^{4} - \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H + \mu^{2} (\mathbb{S}^{2} + \mathbb{S}^{*2}) \qquad \mathbb{S} \to \mathbb{S}^{*}$$

SM + dark matter candidate A + a new scalar that mixes with the CP-even field in the doublet such that

$$m_{\pm} = \lambda_H v_H^2 + \lambda_S v_S^2 \pm \sqrt{\lambda_H^2 v_H^4 + \lambda_S^2 v_S^4 + \kappa v_H^2 v_S^2 - 2\lambda_H \lambda_S v_H^2 v_S^2}$$

The mass eigenstates fields  $h_1$  and  $h_2$  are obtained from h and S via

$$\binom{h_1}{h_2} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \binom{h}{S}$$

The conditions for the potential to be bounded from below are the same for the two models

$$\lambda_H > 0, \qquad \lambda_S > 0, \qquad \kappa > -2\sqrt{\lambda_H \lambda_S}$$

The scalar mass matrix is



# A vector DM model

Dark U(1)<sub>X</sub> gauge symmetry: all SM particles are U(1)<sub>X</sub> neutral. New complex scalar field - scalar under the SM gauge group but has unit charge under U(1)<sub>X</sub>. Lagrangian invariant under

$$X_{\mu} \to -X_{\mu}, \quad \mathbb{S} \to \mathbb{S}^*$$

Forbids kinetic mixing between the SM gauge boson from  $U(1)_y$  and the dark one from  $U(1)_x$ . The Lagrangian is

$$\mathscr{L} = \mathscr{L}_{SM} - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) - \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{4} + \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) - \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{4} + \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) - \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{4} + \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{4} + \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{4} + \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X^{\mu\nu} + \mu_{S} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} + \lambda_$$

with

$$H = \begin{pmatrix} G^{\pm} \\ \frac{1}{\sqrt{2}}(v_H + h + iG_0) \end{pmatrix} \qquad \mathbb{S} = \frac{1}{\sqrt{2}}(v_S + S + iA)$$

h is the real doublet component, S is the new real scalar component and A is the Goldstone boson related with  $U(1)_X$ .

### P: Find the mass of the new gauge boson.

# A vector DM model

With the previous definitions, the masses of the gauge bosons are

$$m_W = \frac{1}{2}gv_H; m_Z = \frac{1}{2}\sqrt{g^2 + g^2}v_H; m_{DM} = g_X v_S$$

and the masses of the two scalars are

$$m_{\pm} = \lambda_{H} v_{H}^{2} + \lambda_{S} v_{S}^{2} \pm \sqrt{\lambda_{H}^{2} v_{H}^{4} + \lambda_{S}^{2} v_{S}^{4} + \kappa v_{H}^{2} v_{S}^{2} - 2\lambda_{H} \lambda_{S} v_{H}^{2} v_{S}^{2}}$$

The mass eigenstates fields  $h_1$  and  $h_2$  are obtained from h and S via (and the Goldstone is eaten by the vector DM)

$$\binom{h_1}{h_2} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \binom{h}{S}$$

I will come back to this model later.



# A fermion DM model

Let us now build a model with a DM fermion. The Lagrangian is

$$\mathscr{L} = \mathscr{L}_{SM} + V_{SM} - V_{New} + \bar{\chi}(\gamma_{\mu}\partial^{\mu} - m_{\chi})\chi - iy_{\chi}P\bar{\chi}\gamma_{5}\chi + \text{scalar kinetic terms}$$

where  $\chi$  is the new DM fermion for which we impose a  $Z_2$  symmetry  $\chi \to -\chi$  that is combined with  $P \to P$  and  $\phi_2 \to -\phi_2$  leading to the following new potential with two complex scalar doublets and one real singlet.

$$\begin{split} V_{New} &= m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^{\dagger} \Phi_2 + h \cdot c.) + \frac{m_s^2}{2} P^2 + \kappa (P \Phi_1^{\dagger} \Phi_2 + h \cdot c.) \\ &+ \frac{\lambda_1}{2} (\Phi_1^{\dagger} \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^{\dagger} \Phi_2)^2 + \lambda_3 (\Phi_1^{\dagger} \Phi_1) (\Phi_2^{\dagger} \Phi_2) + \lambda_4 (\Phi_1^{\dagger} \Phi_2) (\Phi_2^{\dagger} \Phi_1) \\ &+ \frac{\lambda_5}{2} \left[ (\Phi_1^{\dagger} \Phi_2)^2 + h \cdot c \cdot \right] + \frac{\lambda_6}{4} P^4 + \frac{\lambda_7}{2} (\Phi_1^{\dagger} \Phi_1) P^2 + \frac{\lambda_8}{2} (\Phi_2^{\dagger} \Phi_2) P^2 \end{split}$$

We will need and extra  $Z_2$  symmetry  $\chi \to -\chi$ , to make sure that no other Yukawa terms can be built with the SM fermions.

### P: Try to build one of these terms

# A fermion DM model

The new dark fermion  $\chi$  couples to two new fields, that come from the rotation of P and the CP-odd field from the doublet.

 $(a\cos\theta + A\sin\theta)\bar{\chi}\gamma_5\chi$ 

In turn, a and A provide the link to the remaining SM particles. So the pseudo scalar acts here as the portal.

P: Could we do this with a scalar instead of a pseudoscalar?

P: If a pseudo scalar is indeed needed, could we do this with one doublet only?

P: What are the diagrams for  $pp \rightarrow \chi \chi j$ ? What is the background?

# The spin 0 extension - complex

Let us now go back to 5th model on the list

$$\mathscr{L} = \mathscr{L}_{SM} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} - \lambda_{S} \left| \mathbb{S} \right|^{4} - \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H + \mu^{2} (\mathbb{S}^{2} + \mathbb{S}^{*2}) \qquad \mathbb{S} = \frac{1}{\sqrt{2}} (v_{S} + S + iA)$$

Model	Phase	VEVs at global minimum	
$\mathbb{U}(1)$	Higgs+2 degenerate dark	$\langle \mathbb{S} \rangle = 0$	
	2  mixed + 1  Goldstone	$\langle A \rangle = 0 \ (\mathbb{M}(1) \to \mathbb{Z}_2')$	
$\mathbb{Z}_2  imes \mathbb{Z}'_2$	Higgs + 2 dark	$\langle \mathbb{S} \rangle = 0$	
	$2 \operatorname{mixed} + 1 \operatorname{dark}$	$\langle A \rangle = 0 \ (\mathbb{Z}_2 \times \mathbb{Z}'_2 \to \mathbb{Z}'_2 \ )$	
$\mathbb{Z}_2'$	$2 \operatorname{mixed} + 1 \operatorname{dark}$	$\langle A \rangle = 0$	
	3 mixed	$\langle \mathbb{S} \rangle \neq 0 \ (\mathbb{Z}_2')$	

P: What are the diagrams for  $pp \rightarrow \chi \chi j$ ? What is the background?

P: What are the diagrams for  $\chi u \rightarrow \chi u$ ? And for  $\chi g \rightarrow \chi g$ ?

P: What are the diagrams for  $\chi\chi \rightarrow hh$ ? And for  $\chi\chi \rightarrow \gamma\gamma$ ?

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# Rules for extended sectors

# Extended scalar sectors

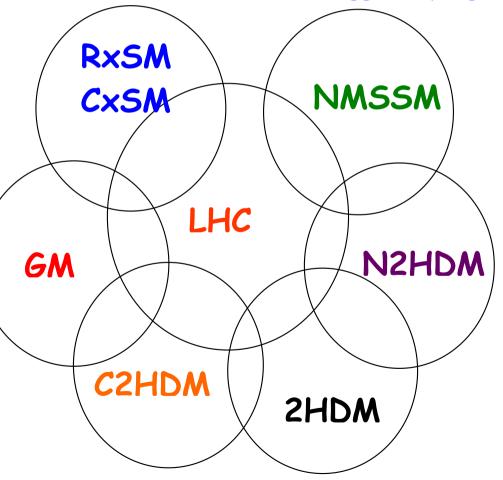
1. <u>Direct detection of new physics</u> - Motivate searches at the LHC in simple extensions of the scalar sector - benchmark models for searches.

2. Indirect detection of new physics (via measurements of the 125 GeV Higgs couplings)

a) Mixing effects with other Higgs bosons, e.g. singlet, doublet, CP admixtures.

b) How efficiently can the parameter space of these simple extensions
be constrained through measurements
of Higgs properties? Focus on CP.

c) What are higher order EW corrections (of extended models) good for?



# Many simple model with new and interesting physics

	CxSM (RxSM)	2HDM	C2HDM	N2HDM
Model	SM+Singlet	SM+Doublet	SM+Doublet	2HDM+Singlet
Scalars	$h_{1,2,(3)}$ (CP even)	$H, h, A, H^{\pm}$	$H_{1,2,3}$ (no CP), $H^{\pm}$	$h_{1,2,3}$ (CP-even), A, $H^{\pm}$
Motivation	DM, Baryogenesis	$+ H^{\pm}$	+ CP violation	+

### Similar neutral Higgs sector but different underlying symmetries

- Final There is a 125 GeV Higgs (other scalars can be lighter and/or heavier).
- From the 2HDM on, tan  $\beta = v_2/v_1$ . Also charged Higgs are present.
- Models (except singlet extensions) can be CP-violating.
- Final the p=1 at tree-level.
- You get a few more scalars (CP-odd or CP-even or with no definite CP)
- Fin case all neutral scalars mix there will be three mixing angles
- They can have dark matter candidates (or not)

# Potential(s)

Potential 
$$V = m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^{\dagger} \Phi_2 + h \cdot c.) + \frac{m_s^2}{2} \Phi_s^2$$
  
 $+ \frac{\lambda_1}{2} (\Phi_1^{\dagger} \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^{\dagger} \Phi_2)^2 + \lambda_3 (\Phi_1^{\dagger} \Phi_1) (\Phi_2^{\dagger} \Phi_2) + \lambda_4 (\Phi_1^{\dagger} \Phi_2) (\Phi_2^{\dagger} \Phi_1)$   
 $+ \frac{\lambda_5}{2} \left[ (\Phi_1^{\dagger} \Phi_2) + h \cdot c. \right] + \frac{\lambda_6}{4} \Phi_8^4 + \frac{\lambda_7}{2} (\Phi_1^{\dagger} \Phi_1) \Phi_s^2 + \frac{\lambda_8}{2} (\Phi_2^{\dagger} \Phi_2) \Phi_s^2$   
with fields  
 $\Phi_1 = \begin{pmatrix} \phi_1^{\dagger} \\ \frac{1}{\sqrt{2}} (v_1 + \rho_1 + i\eta_1) \end{pmatrix} \Phi_2 = \begin{pmatrix} \phi_2^{\dagger} \\ \frac{1}{\sqrt{2}} (v_2 + \rho_2 + i\eta_2) \end{pmatrix} \Phi_s = v_s + \rho_s$   
magenta  $\Rightarrow$  SM  
magenta + black  $\Rightarrow$  2HDM (also C2HDM)  
magenta + black + blue + red  $\Rightarrow$  N2HDM  
 $\star m_{12}$  and  $\lambda_5$  real  $2HDM$   
 $\star m_{12}$  and  $\lambda_5$  real  $2HDM$   
 $\star m_{12}$  and  $\lambda_5$  real  $2HDM$   
 $\star m_{12}$  and  $\lambda_5$  complex C2HDM  
 $\star m_{12}$  and  $\lambda_5$  compl

or

4

# Constraints

- Should contain a SM-like Higgs boson
- Electroweak p parameter should be close to 1 (relation between W and Z mass)

$$\rho_{exp} = 1.0004^{+0.0003}_{-0.0004}$$

$$\rho = \frac{m_W^2}{m_Z^2 \cos \theta_W^2} = \frac{\sum_i \left[ 4T_i(T_i + 1) - Y_i^2 \right] |v_i|^2 c_i}{\sum_i 2Y_i^2 |v_i|^2}$$

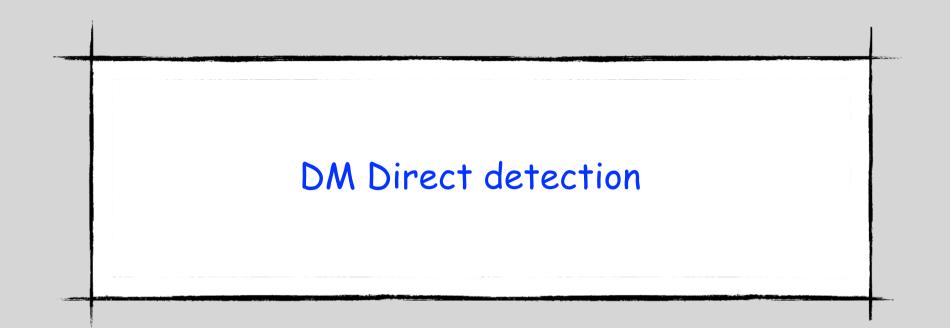
$$\sum_i (2Y_i^2) |v_i|^2$$

$$Q = T_3 + Y/2$$

 $SU(2)_L$  Isospin

- VEV
- 1(1/2) for complex (real) representations

- Perturbative unitarity
- Boundness from below



# Distribution of Dark Matter in the galaxy

Hard problem - there are only averages over long volumes. There are attempts to measure locally and globally the shape of the Milky Way DM halo.

But what we really need is the kinematic distribution of DM in our solar system.

We assume the Standard Halo Model (SHM) with a density profile of  $\rho(r) \sim r^{-2}$ . The velocities obey a Boltzmann-Maxwell distribution. The local circular speed of DM is (218-246) Km/s. The velocity distribution is cut at the escape velocity, which is about 530 Km/s.

The prediction for the direct detection of DM on the Earth is separated into a kinematical part involving the velocity distribution and one part that deals with the collision. This allows us to compare different experiments independently of the local DM distribution.

MB distribution - system containing a large number of identical non-interacting, non-relativistic classical particles in thermodynamic equilibrium, the fraction of the particles within an infinitesimal element of the three-dimensional velocity space, cantered on a velocity vector of magnitude v, is

$$f(v) \; d^3 v = \left(rac{m}{2\pi kT}
ight)^{3/2} e^{-rac{mv^2}{2kT}} \; d^3 v,$$

# **Direct detection**

We assume we have a WIMP that has an electroweak interaction that comes via some portal. Since the DM is coupled to a mediator (in the case of the scalar extension is the Higgs) and the mediator is coupled to the remaining SM particles, there will be an effective DM-SM interaction.

Also, we assume there is a local DM density  $\rho_0$  in which the earth is traveling. The DM stream may interact with a nucleus and transfer a small amount of energy (recoil energy). So far no event was recorded and bounds were set on coupling vs. mass. The differential scattering can be written as

$$\frac{dR(E_R,t)}{dE_R} = N_T \frac{\rho}{m_{\chi}} \int_{v > v_{min}} v f(\vec{v} + \vec{v}_E(t)) \frac{d\sigma(E_R,v)}{dE_R} d^3v \qquad [\sigma vn] = m^2 \frac{m}{s} \frac{1}{m^3} = \frac{1}{s}$$

where  $E_R$  is the recoil energy,  $N_T$  is the number of nuclei, v is the velocity in the rest frame of the experiment, f is the velocity distribution function and  $v_{min}$  is the minimum velocity of DM causing a recoil energy. The minimum velocity for elastic scattering is

$$v_{min} = \sqrt{\frac{m_N E_R}{2\mu^2}}, \qquad \mu = \frac{m_N m_\chi}{m_N + m_\chi}$$

where  $m_N$  is the nucleon mass.

1

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# **Direct detection**

The differential rate can further be divided in a spin-dependent (SD) and a spin-independent (SI) part. The time integrated differential cross section is then written as

$$\frac{\sigma(E_R, v)}{dE_R} = \frac{m_N}{2\mu^2 v^2} \left(\sigma^{SI} F_{SI}^2(E_R) + \sigma^{SD} F_{SD}^2(E_R)\right)$$

where F are nuclear form factors. The DM velocity is non-relativistic,  $v/c \approx 10^{-3}$ , and therefore the recoil energies are low (order KeV) and the momentum transfer is of order GeV. This in turn means that nuclei cannot be treated as point-like in the scattering process with DM. The cross section with a target nucleus is

$$\sigma_i^{SI} = \frac{\mu_i}{\pi} |Z_i g_p^{SI} + (A_i - Z_i) g_n^{SI}|^2 |F_i(q)|^2$$

where i indicates the material and Z and A are the proton and mass numbers, respectively.

Now we need to find a way to link the quarks to the nucleons.

Let us see how exactly we can do this.

Let us go back to the Fermi theory of weak interactions, with Lagrangian

$$\mathscr{L}_{int} = \frac{G_F}{\sqrt{2}} \sum_{i,j} \bar{\psi}_i \gamma_\mu (1 - \gamma_5) \psi_i \ \bar{\psi}_i \gamma_\mu (1 - \gamma_5) \psi_i$$

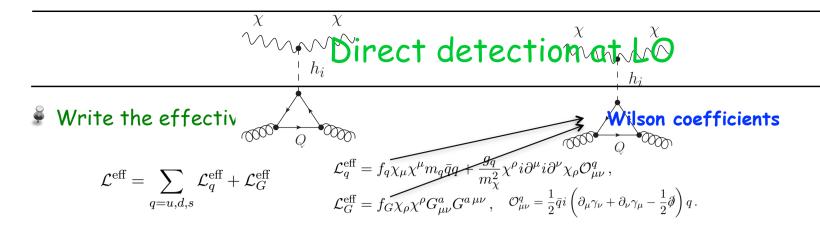
In the electroweak theory this interaction would have been written as

$$\mathscr{L}_{int} = \frac{g^2}{8} \sum_{i,j} \bar{\psi}_i \gamma_\mu (1 - \gamma_5) \psi_i \ \frac{-1}{q^2 - m_W^2} \bar{\psi}_i \gamma_\mu (1 - \gamma_5) \psi_i$$

And in the limit  $q^2 \ll m_W^2$  we can write

$$\mathscr{L}_{int} \approx \frac{g^2}{8m_W^2} \sum_{i,j} \bar{\psi}_i \gamma_\mu (1 - \gamma_5) \psi_i \ \bar{\psi}_i \gamma_\mu (1 - \gamma_5) \psi_i \quad (q^2 \ll m_W^2) \qquad \qquad \frac{G_F}{\sqrt{2}} = \frac{g^2}{8m_W^2}$$

We say that we have matched the Wilson coefficient  $G_F/\sqrt{2}$  to the coefficient of the actual model. This yields  $G_F = 1.17 \times 10^{-5} \text{ GeV}^{-2}$ . Theory works well for and energy well below the W boson mass. At higher energies one should use the proper electroweak theory.



Define the nucleon matrix elements

And calculate the cross section

fraction of the nucleon momentum carried by the quarks (PDFs)

$$\sigma_N = \frac{1}{\pi} \left( \frac{m_N}{m_\chi + m_N} \right)^2 \left| f_N \right|^2. \qquad f_N/m_N = \sum_{q=u,d,s} f_q f_{T_q}^N + \sum_{q=u,d,s,c,b} \frac{3}{4} \left( q^N(2) + \bar{q}^N(2) \right) g_q - \frac{8\pi}{9\alpha_S} f_{T_G}^N f_G.$$

And now we need to get all the Wilson coefficients  $f_q, g_q, f_G$  at the order we are working at

Write the effective Lagrangian

$$\mathcal{L}_{\text{eff}} = \sum_{q} C_{S}^{q} \mathcal{O}_{S}^{q} + C_{S}^{g} \mathcal{O}_{S}^{g} + \sum_{q} C_{T}^{q} \mathcal{O}_{T}^{q}$$

$$\begin{split} \mathcal{O}^q_S &= m_q \chi^2 \bar{q} q \,, \\ \mathcal{O}^g_S &= \frac{\alpha_s}{\pi} \chi^2 G^a_{\mu\nu} G^{a\mu\nu} \,, \\ \mathcal{O}^q_T &= \frac{1}{m_\chi^2} \chi i \partial^\mu i \partial^\nu \chi \mathcal{O}^q_{\mu\nu} \,. \end{split}$$

Quark contributions

$$\mathcal{A}_{\text{gen}} = \sum_{i} C_{\chi\chi h_i} C_{qqh_i} \frac{1}{q^2 - m_{h_i}^2} \bar{u}(\mathbf{p}) u(\mathbf{p} + \mathbf{q}) \xrightarrow{q^2 \to 0} -\sum_{i} C_{\chi\chi h_i} C_{qqh_i} \frac{1}{m_{h_i}^2} \bar{u}(\mathbf{p}) u(\mathbf{p})$$

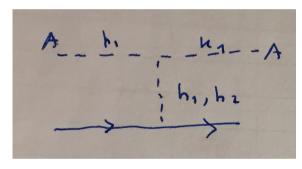
### Assuming scalar-like couplings we can write

$$\mathcal{L}_{ ext{eff}} \supset -\sum_{i} rac{C_{\chi\chi h_i} C_{qqh_i}}{2m_{h_i}^2} \chi \chi \bar{q} q$$
 Term in the effective Lagrangian

And so the Wilson coefficient is

$$C_S^q \supset -\sum_i \frac{C_{\chi\chi h_i} C_{qqh_i}}{2m_q m_{h_i}^2}$$

### Exchanged momentum very small



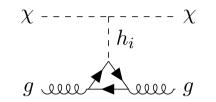
There can be additional contributions to the quark operators generated through other diagrams, even though at tree level the t-channel exchange is the only topology contributing to this operator in the models under investigation.

# Direct detection at LO for scalars

Gluon contributions

$$m_Q \bar{Q} Q \to -\frac{\alpha_s}{12\pi} G^a_{\mu\nu} G^{a\mu\nu}$$

Finis transformation can be used to units  $\frac{f_N^{\text{LO}}}{m_N} = f_q^{\text{LO}} \left[ \sum_{q=u,d,s} f_{T_q}^N - \underbrace{\frac{h_i}{q}}_{q} \right]$ 



### And so the final cross section is

$$\sigma_N = \frac{1}{\pi} \left( \frac{m_N}{m_{\chi} + m_N} \right)^2 \left| f_N \right|^2.$$

And for normalisation the Wilson coefficient in a model with two scalars is

$$f_q = \frac{1}{2} \frac{gg_{\chi}}{m_W} \frac{\sin(2\alpha)}{2} \frac{m_{h_1}^2 - m_{h_2}^2}{m_{h_1}^2 m_{h_2}^2} m_{\chi}, \quad q = u, d, s, c, b, t$$

# Nuclear form factors

We here present the numerical values for the nuclear form factors defined in Eq. (4.59). The values of the form factors for light quarks are taken from micrOmegas [75]

$$f_{T_u}^p = 0.01513, \quad f_{T_d}^p = 0.0.0191, \quad f_{T_s}^p = 0.0447,$$
 (A.99a)

$$f_{T_u}^n = 0.0110, \quad f_{T_d}^n = 0.0273, \quad f_{T_s}^n = 0.0447,$$
 (A.99b)

which can be related to the gluon form factors as

$$f_{T_G}^p = 1 - \sum_{q=u,d,s} f_{T_q}^p, \qquad f_{T_G}^n = 1 - \sum_{q=u,d,s} f_{T_q}^n.$$
(A.100)

The needed second momenta in Eq. (4.59) are defined at the scale  $\mu = m_Z$  by using the CTEQ parton distribution functions [76],

 $u^p(2) = 0.22, \qquad \bar{u}^p(2) = 0.034, \qquad (A.101a)$ 

$$d^p(2) = 0.11, \qquad \bar{d}^p(2) = 0.036, \qquad (A.101b)$$

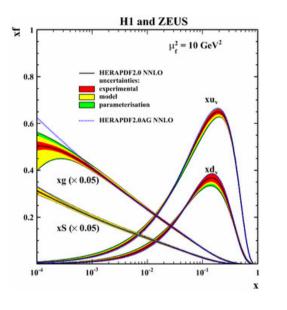
$$s^{p}(2) = 0.026$$
,  $\bar{s}^{p}(2) = 0.026$ , (A.101c)

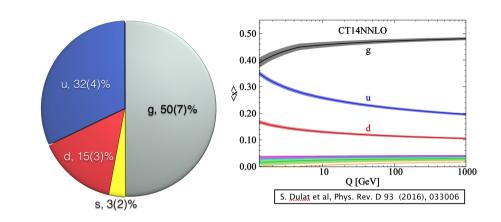
$$c^{p}(2) = 0.019, \qquad \bar{c}^{p}(2) = 0.019, \qquad (A.101d)$$

$$b^p(2) = 0.012, \qquad \bar{b}^p(2) = 0.012, \qquad (A.101e)$$

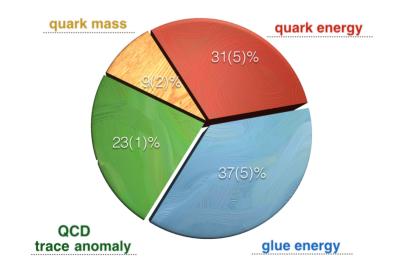
where the respective second momenta for the neutron can be obtained by interchanging up- and down-quark values.

# Nuclear form factors





**Figure 1.** The contributions of different quark flavors and glue to the proton momentum fraction. The left panel shows the lattice results renormalized in the  $\overline{\text{MS}}$  scheme at 2 GeV with 1-loop perturbative calculation and proper normalization of the glue. The experimental values are illustrated in the right panel, as a function of the  $\overline{\text{MS}}$  scale. Our results agree with the experimental values at 2 GeV.



YANG ET AL., ARXIV:1710.09011V1 (2018)

Figure 2. The pie chart of the proton mass decomposition, in terms of the quark mass, quark energy, glue field energy and trace anomaly.

# The spin 0 extension - real

The SM is extended by an extra real scalar singlet S. The most general Lagrangian we can write is

$$\mathscr{L} = \mathscr{L}_{SM} + \frac{1}{2} (\partial_{\mu} S) (\partial^{\mu} S) - aS - bS^2 - cS^3 - dS^4 - \kappa_1 SH^{\dagger}H - \kappa_2 SH^{\dagger}H - \mu^2 H^{\dagger}H - \lambda (H^{\dagger}H)^2$$

And with a  $Z_2$  symmetry  $S \rightarrow -S$ , the potential reduces to

$$V_N = bS^2 + dS^4 + \kappa_1 S^2 H^\dagger H + \mu^2 H^\dagger H + \lambda (H^\dagger H)^2$$

Let us consider the solution (for the minimum)

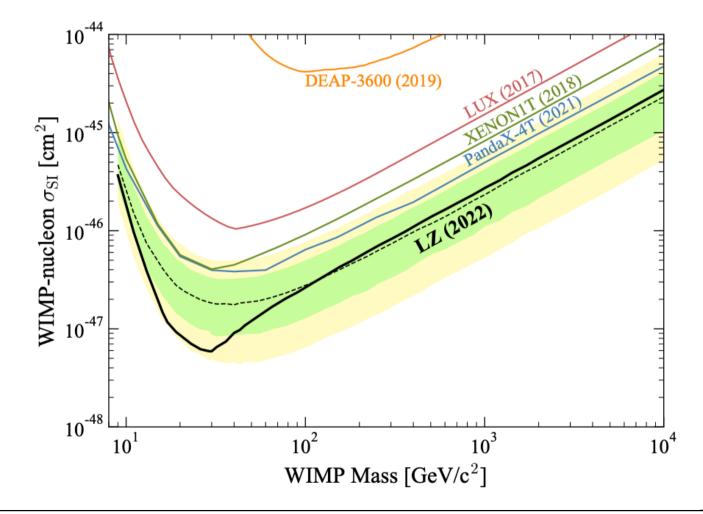
$$S = 0; h^2 = -\mu^2/(2\lambda);$$

P: Collect the relevant couplings for direct detection.

P: Calculate the amplitude.

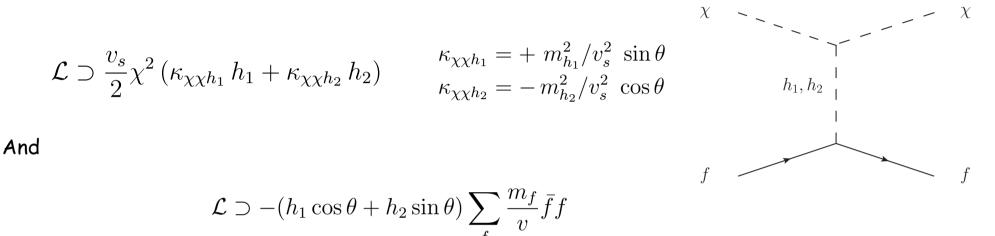
# DD measurements

This is what we have to compare to.

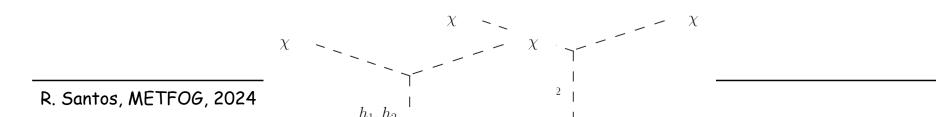


# Back to the complex spin zero extension

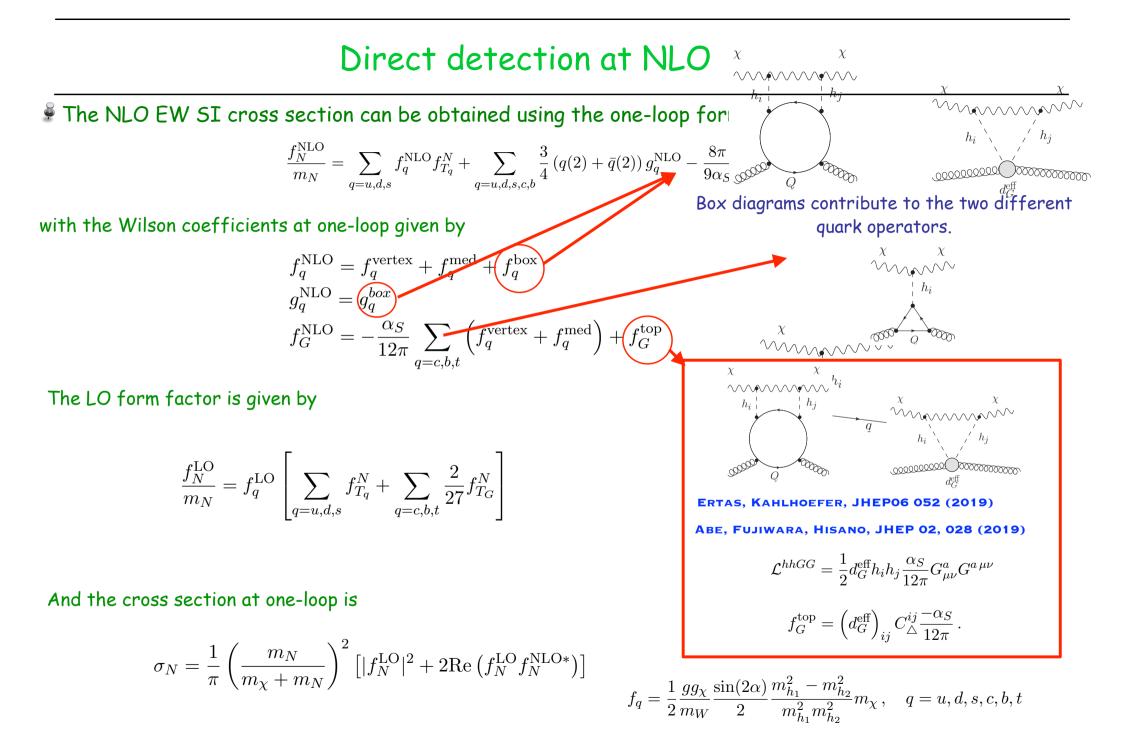
Let us now consider the same process but in the complex extension. The relevant pieces of the Lagrangian are



### P: What is now the amplitude in the limit of zero exchanged momentum?



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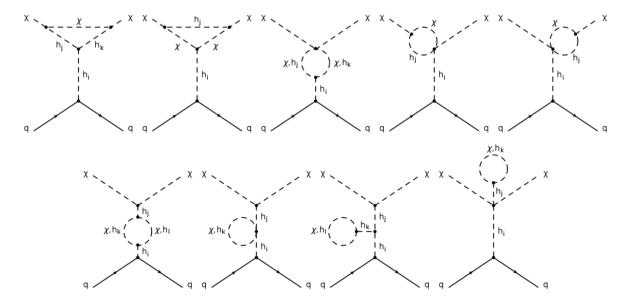
# Direct detection at NLO

S2HDM - Now the SM is extended by one doublet and a complex singlet. There is an extra doublet compared to the previous model.

$$\mathcal{V} = \sum_{ij} m_{ij}^2 \phi_i^{\dagger} \phi_j + \sum_{ijkl} \lambda_{ijkl} \phi_i^{\dagger} \phi_j \phi_k^{\dagger} \phi_l + \sum_{ij} \kappa_{ij} \left| \mathbb{S} \right|^2 \phi_i^{\dagger} \phi_j - \mu_S^2 \left| \mathbb{S} \right|^2 + \lambda_S \left| \mathbb{S} \right|^4 + \mu^2 (\mathbb{S}^2 + \mathbb{S}^{*2})$$

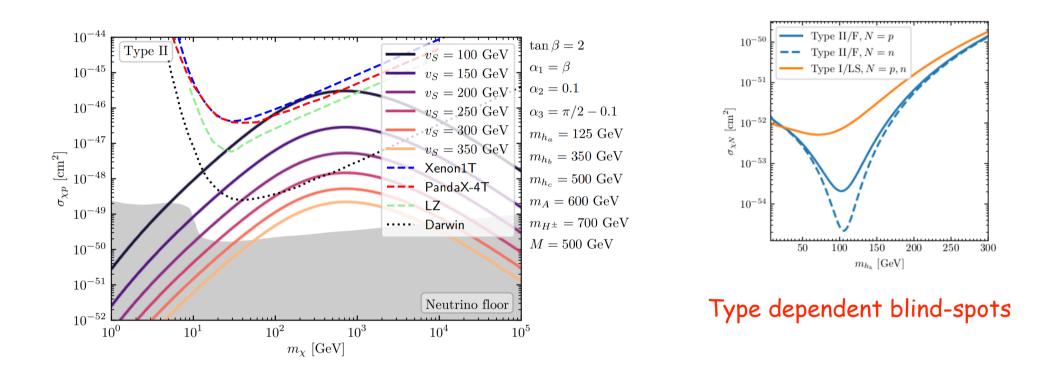
<u>Extra particles</u>: 2 CP-even scalars, 2 charged scalars and 1 CP-odd scalar and a DM particle. Free parameters  $m_{h_{1,2,3}}$ ,  $m_A$ ,  $m_{\chi}$ ,  $\alpha_{1,2,3}$ ,  $\tan \beta$ ,  $m_{12}^2$ ,  $v_S$ .

These models can lead to tree-level flavour changing neutral currents. These are very constrained by experiment. To solve this problem one usually forces the Yukawa Lagrangian to be invariant under a  $Z_2$  symmetry. This leads to 4 possible Yukawa Lagrangians (the way scalars are combined with fermions).



Diagrams that survive. Same type of diagrams as for the CxSM but with more particles in the loop.

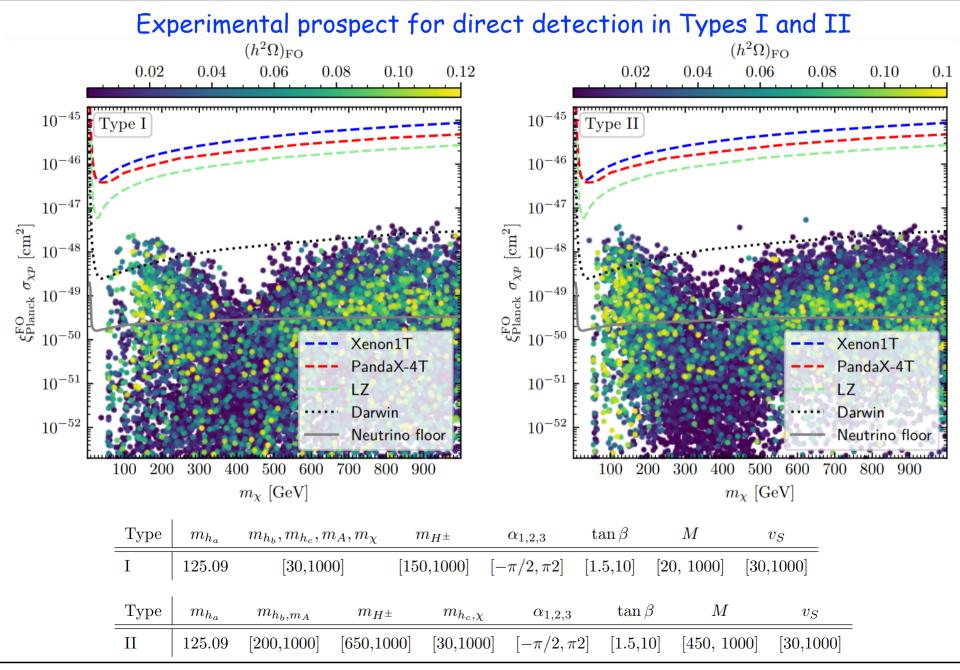
# Direct detection at NLO



Here we just fixed all input parameters except for the VEV of the singlet. The behaviour is similar for all values of the singlet VEV but as the VEV gets smaller a larger mass region in the WIMP region is excluded.

We also show Darwin as an example of some future projection. This is the total cross section.

# Direct detection at NLO



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# Scalar DM but more interesting

# Peculiar Scalar extensions of the SM

Some models have negligible dark matter direct detection (DD) cross section at zero momentum transfer (at leading order). Barely affected by direct detection bounds.

True for models with a pNG dark matter candidate with origin in a potential of the form

$$\mathcal{V} = \sum_{ij} m_{ij}^2 \phi_i^{\dagger} \phi_j + \sum_{ijkl} \lambda_{ijkl} \phi_i^{\dagger} \phi_j \phi_k^{\dagger} \phi_l + \sum_{ij} \kappa_{ij} \left| \mathbb{S} \right|^2 \phi_i^{\dagger} \phi_j - \mu_S^2 \left| \mathbb{S} \right|^2 + \lambda_S \left| \mathbb{S} \right|^4 + \mu^2 (\mathbb{S}^2 + \mathbb{S}^{*2})$$

with

$$\phi_i = \begin{pmatrix} c^{\pm} \\ \frac{1}{\sqrt{2}}(v_i + a_i + ib_i) \end{pmatrix} \qquad \qquad \mathbb{S} = \frac{1}{\sqrt{2}}(v_s + s + iA)$$

which is a model with N Higgs Doublet Model plus a complex singlet.

The potential is invariant under

 $S \rightarrow S^*$  Stabilises A

and without the red term it is also invariant under

$$\mathbb{S} \to e^{i\alpha} \mathbb{S}$$

The soft breaking term gives mass to the pNG dark matter.

R. Santos, METFOG, 2024

# One doublet and one complex singlet (CxSM)

The SM is extended by an extra complex scalar singlet  $\mathbb{S}$  which has a global U(1) symmetry

 $\mathbb{S} \to e^{i\alpha} \mathbb{S}$ 

Softly break dark U(1) symmetry to the residual  $Z_2$  symmetry in one of the singlet components

SM + dark matter candidate A + a new scalar that mixes with the CP-even field in the doublet such that

$$m_{\pm} = \lambda_{H} v_{H}^{2} + \lambda_{S} v_{S}^{2} \pm \sqrt{\lambda_{H}^{2} v_{H}^{4} + \lambda_{S}^{2} v_{S}^{4} + \kappa v_{H}^{2} v_{S}^{2} - 2\lambda_{H} \lambda_{S} v_{H}^{2} v_{S}^{2}}$$

The mass eigenstates fields  $h_1$  and  $h_2$  are obtained from h and S via

$$\binom{h_1}{h_2} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \binom{h}{S}$$

The conditions for the potential to be bounded from below are the same for the two models

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# One doublet and one complex singlet (CxSM)

The amplitude for the DM direct detection cross section

$$i\mathcal{M} \sim \sin\alpha \cos\alpha \left(\frac{im_{h_2}^2}{t - m_{h_2}^2} - \frac{im_{h_1}^2}{t - m_{h_1}^2}\right) \left(\frac{-im_f}{v}\right) \bar{u}_f(k_2) u_f(p_2) \sim 0 \qquad (t \to 0)$$

And it vanishes for zero momentum transfer. Why? Going back to the Lagrangian,

Writing

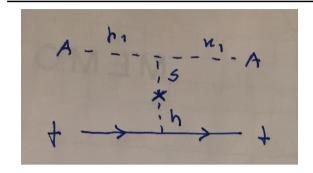
$$\mathbb{S} = \frac{v_S + S}{\sqrt{2}} e^{i\frac{A}{v_S}} \quad \Rightarrow \quad V_{soft} = -\mu^2 (v_S + S)^2 \cos\left(\frac{2A}{v_S}\right) = -\mu^2 (v_S + S)^2 \left(1 - \frac{2A^2}{v_S^2}\right) + \dots$$

Including the kinetic term leads to the following Lagrangian interaction

$$\mathscr{L}_{SA^2} = = \frac{1}{2v_S} (\partial^2 S) A^2 - \frac{1}{v_S} SA(\partial^2 + m_A^2) A$$

First term proportional to  $p^2$  of S and the second term vanishes when the DM particle is on-shell. Amplitude is proportional to  $p^2$  with A on-shell.

# One doublet and one complex singlet (CxSM)



$$i\mathcal{M} \sim \left(\frac{-it}{v_S}\right) \frac{i}{t - m_S^2} (-i2\lambda_{SH}vv_S) \frac{i}{t - m_h^2} \left(\frac{-im_f}{v}\right) \bar{u}_f(k_2) u_f(p_2)$$

Which vanishes when t = 0

Note however if other soft breaking terms are added

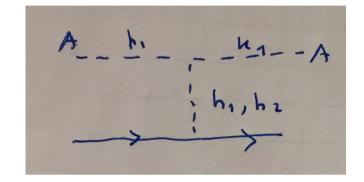
$$V'_{soft} = -\kappa_1^3(\mathbb{S} + \mathbb{S}^*) - \kappa_2 |\mathbb{S}|^2(\mathbb{S} + \mathbb{S}^*) - \kappa_3(\mathbb{S}^3 + \mathbb{S}^{*3})$$

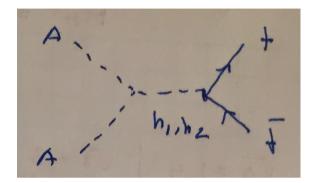
the cancellation is lost except for fine-tuned values of the couplings

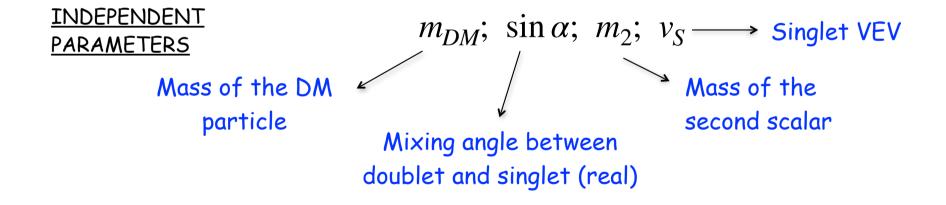
$$\kappa_1^3 = \frac{1}{2}(\kappa_2 + 9\kappa_3)v_S^2$$

# One doublet and one complex singlet (CxSM)

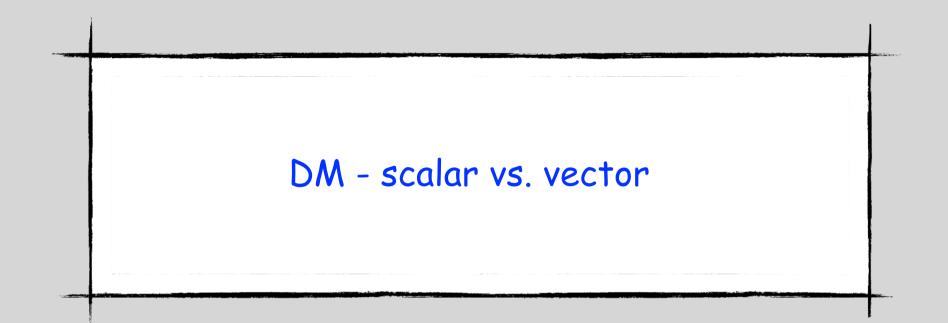
Note that the cancellation does not happen in scattering







There is obviously a 125 GeV Higgs (other scalar can be lighter or heavier). Experimental and theoretical constraints included.

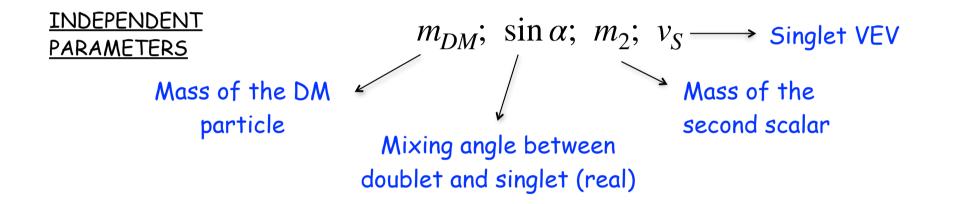


### Scalar vs. vector



### PARTICLE CONTENT

SDM: SM + <u>scalar dark matter</u> + new scalar



Parameter	Range
SM-Higgs— $m_1$	125.09 GeV
Second Higgs— $m_2$	[1,1000] GeV
DM— <i>m</i> <sub>DM</sub>	[1,1000] GeV
Singlet VEV— $v_s$	[1,10 <sup>7</sup> ] GeV
Mixing angle— $\alpha$	$\left[-\frac{\pi}{4},\frac{\pi}{4}\right]$

There is obviously a 125 GeV Higgs (other scalar can be lighter and heavier). Experimental and theoretical constraints to be discussed next Theoretical and collider constraints:

Points generated with Scanners requiring

- absolute minimum
- boundedness from below
- that perturbative unitarity holds
- S,T and U

<u>Signal strength</u>: gives a constraint on  $\cos \alpha$ 

<u>Searches</u>: BR of Higgs to invisible below 24%

<u>Searches</u>: for extra scalars imposed via HiggsBounds which gives a bound that is a function of the new scalar mass and  $\cos \alpha$ 

### Cosmological constraints:

<u>DM abundance</u>: we require

 $(\Omega h^2)_{DM} < 0.1186$  [Calculated with MicroOmegas]

or to be in the  $5\sigma$  allowed interval from the Planck collaboration measurement

 $(\Omega h^2)_{DM}^{obs} = 0.1186 \pm 0.0020$ 

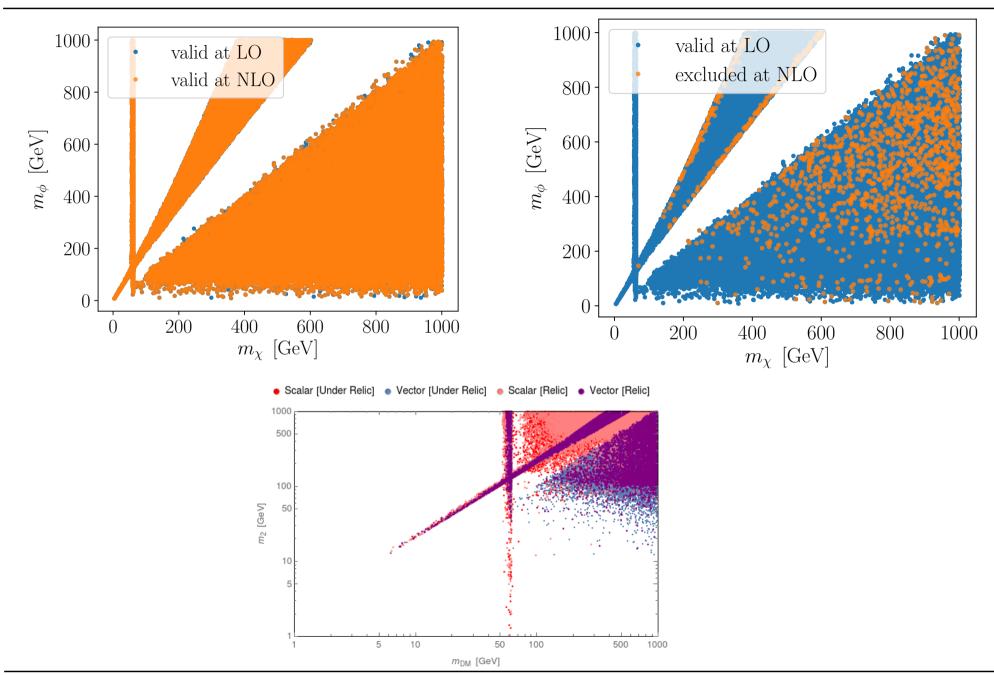
Direct detection: we apply the latest XENON1T bounds

$$\sigma_{DM,N}^{eff} = f_{DM} \, \sigma_{DM,N} \quad \text{with} \quad f_{DM} = \frac{(\Omega h^2)_{DM}}{(\Omega h^2)_{DM}^{obs}}$$

[Fraction contributing to the scattering]

<u>Indirect detection</u>: for the DM range of interest, the Fermi-LAT upper bound on the dark matter annihilation from dwarfs is the most stringent. We use the Fermi-LAT bound on bb.

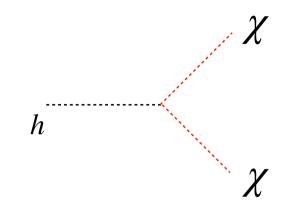
### Scalar vs. vector



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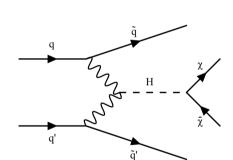
Back to colliders - the Higgs invisible width

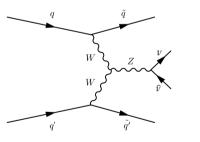
## Back to colliders - Higgs invisible width

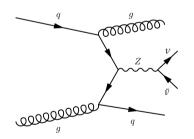


If the dark matter particle has a mass that is below half of Higgs mass, the Higgs can decay to a dark matter pair.

One of the many on-going searches is







The result gives us a bound on the BR of the Higgs to invisible

$$BR(h \to \chi\chi) = \frac{\Gamma(h \to \chi\chi)}{\Gamma_T(h)} \qquad \Gamma_T(h) \approx 4.6 \ MeV$$

### The width is calculated using

49.4.2 Two-body decays

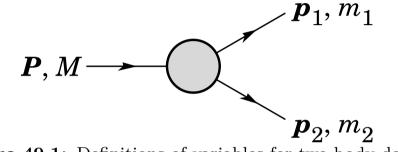


Figure 49.1: Definitions of variables for two-body decays.

In the rest frame of a particle of mass M, decaying into 2 particles labeled 1 and 2,

$$E_1 = \frac{M^2 - m_2^2 + m_1^2}{2M} , \qquad (49.16)$$

$$|\mathbf{p}_1| = |\mathbf{p}_2| = \frac{1}{2M} \sqrt{\lambda(M^2, m_1^2, m_2^2)}$$
, (49.17)

and

$$d\Gamma = \frac{1}{32\pi^2} |\mathscr{M}|^2 \frac{|\mathbf{p}_1|}{M^2} d\Omega , \qquad (49.18)$$

where  $\lambda(\alpha, \beta, \gamma) = \alpha^2 + \beta^2 + \gamma^2 - 2\alpha\beta - 2\alpha\gamma - 2\beta\gamma$  is the Källén function and  $d\Omega = d\phi_1 d(\cos \theta_1)$  is the solid angle of particle 1. The invariant mass M can be determined from the energies and momenta using Eq. (49.2) with  $M = E_{\rm cm}$ . Now calculate the invisible BR for the three models

<u>Scalar</u> - The SM is extended by an extra real scalar singlet S, with a  $Z_2$  symmetry  $S \rightarrow -S$ 

$$\mathscr{L} = \mathscr{L}_{SM} + \frac{1}{2} (\partial_{\mu} S)(\partial^{\mu} S) - V_N + V_{SM} \qquad V_N = bS^2 + dS^4 + \kappa_1 S^2 H^{\dagger} H + \mu^2 H^{\dagger} H + \lambda (H^{\dagger} H)^2$$

Let us consider the solution (for the minimum)

$$S = 0; h^2 = -\mu^2/(2\lambda);$$

<u>Vector</u> - Dark  $U(1)_X$  gauge symmetry: all SM particles are  $U(1)_X$  neutral.

$$\mathscr{L} = \mathscr{L}_{SM} - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} - \lambda_{S} \left| \mathbb{S} \right|^{4} - \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} - \lambda_{S} \left| \mathbb{S} \right|^{4} - \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} - \lambda_{S} \left| \mathbb{S} \right|^{4} - \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} - \lambda_{S} \left| \mathbb{S} \right|^{4} - \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} - \lambda_{S} \left| \mathbb{S} \right|^{4} - \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X_{\mu\nu} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \lambda_{S} \left| \mathbb{S} \right|^{2} + \kappa \left| \mathbb{S} \right|^{2} H^{\dagger} H \qquad D_{\mu} = \partial_{\mu} + ig_{X} X^{\mu\nu} + (D_{\mu} \mathbb{S})^{\dagger} (D^{\mu} \mathbb{S}) + \mu_{S}^{2} \left| \mathbb{S} \right|^{2} + \kappa \left| \mathbb{S} \right|^{2}$$

with

$$H = \begin{pmatrix} G^{\pm} \\ \frac{1}{\sqrt{2}}(v_H + h + iG_0) \end{pmatrix} \qquad S = \frac{1}{\sqrt{2}}(v_S + S + iA) \\ \begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} h \\ S \end{pmatrix}$$

### Back to colliders - Higgs invisible width

Now choose a DM mass of 40 GeV and calculate the bound on the portal coupling

$$BR(h \to \chi \chi) = \frac{\Gamma(h \to \chi \chi)}{\Gamma_T(h)} \qquad \qquad \Gamma_T(h) \approx 4.6 \ MeV$$

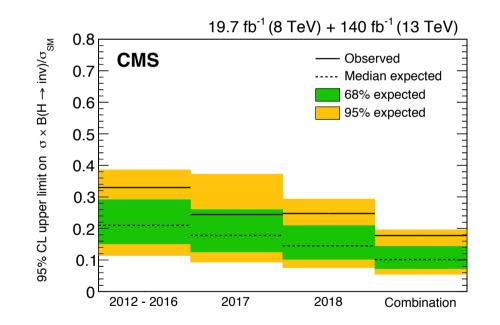


Figure 11: Observed and expected 95% CL upper limits on  $(\sigma_H / \sigma_H^{SM}) \mathcal{B}(H \to inv)$  for all datataking years considered, as well as their combination, assuming an SM Higgs boson with a mass of 125.38 GeV.

Relic density, WIMP miracle and thermal DM generation

### Temperature fluctuations in the CMB

CMB are photons that decoupled from the thermal bath. The <u>surface of last scattering is the one</u> <u>defined by the photons that could come freely to reach us today</u>.

 $T_0 = (2.72548 \pm 0.00057)$ 

The value of the variations is of the order  $\delta T/T \leq 10^{-5}$  in the <u>sphere of last scattering</u>. If we study these variations in detail we can understand better the temperature fluctuations at that time. Temperature fluctuations on the sphere can be described via spherical harmonics, with the usual polar and azimuthal angles

$$\frac{\delta T(\theta,\phi)}{T_0} = \frac{T(\theta,\phi) - T_0}{T_0} = \sum_{l=0}^{\infty} \sum_{m=-l}^{l} a_{lm} Y_{ml}(\theta,\phi)$$

In order to analyse temperature fluctuations, the relevant measure is the variance of the temperature distribution

$$\frac{1}{4\pi} \int d\Omega \left( \frac{\delta T(\theta, \phi)}{T_0} \right)^2 = \frac{1}{4\pi} \sum_{m,l} |a_{lm}|^2$$

# Temperature fluctuations in the CMB

The index m describes the angular momentum in a particular direction, but because there is no special direction in the sphere of last scattering the  $a_{lm}$  coefficients do not depend on m. Thus, the sum over m yields 21+1 identical terms. The average of  $|a_{lm}|^2$  over m will be defined as the observed power spectrum

$$C_{l} = \frac{1}{2l+1} \sum_{m=-l} |a_{lm}|^{2}$$

The values of the coefficients  $C_l$  can be determined using

$$\frac{1}{4\pi} \int d\Omega \left(\frac{\delta T(\theta, \phi)}{T_0}\right)^2 = \frac{1}{4\pi} \sum_{l=0}^{\infty} \frac{2l+1}{4\pi} C_l$$

Temperature fluctuations measured by PLANCK allows to calculate  $C_l$ .

The peaks are generated by acoustic oscillations which occur in the baryon-photon fluid at the time of photon decoupling.

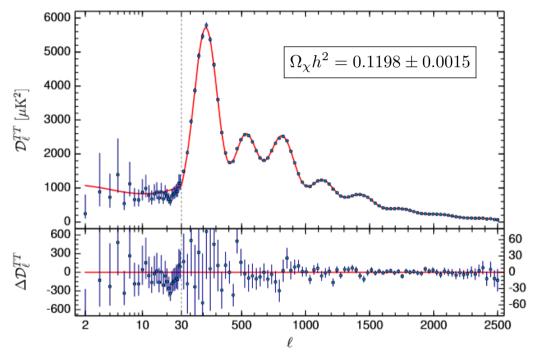
Regions with a large accumulation of DM form gravitational wells, which pull the baryon-photon fluid inside it resulting in a compression of the fluid.

At the same time the relativistic photons exert a pressure that counteracts the gravitational pull, which results in a rarefaction of the fluid.

These counteracting forces create oscillations in the baryon-photon fluid and lead to temperature fluctuations in the photon spectrum during decoupling.

### Temperature fluctuations in the CMB

The odd numbered peaks correspond to the decoupling of photons during a compression phase, while even numbered peaks correspond to a decoupling during a rarefaction phase.



To fit the data points given in a model with 6 independent cosmological parameters is used under the assumption of a flat universe. This model is referred to as the "base  $\Lambda CDM$ ", which includes the Hubble constant H, and the baryon and DM fraction The first peak corresponds to the time of last scattering where the fluid compressed once. Determining its position gives information about the curvature of the universe.

The second peak corresponds to one compression and one rarefaction of the fluid. A large relative baryon content in the baryon-photon fluid would lead to an increase in amplitude of the compression peaks and at the same time to a decrease of the rarefaction peaks. Therefore, by measuring the ratio between the first and the second peak, the <u>baryon content of the universe</u> can be obtained.

<u>The height of the third peak determines the</u> <u>amount of DM in the universe.</u> Since, DM does not interact with photons, it only contributes to the strength of the compression peaks. Therefore, a large third peak is a sign of a sizeable DM component in the universe.

The relic density is calculated using the Boltzmann equation which describes the change of a number density n(t) with time. If a(t) is the linear dimension of the universe,

$$0 = \frac{d}{dt} [n(t) a(t)^3] = \dot{n}(t)a(t)^3 + 3n(t)a(t)^2 \dot{a}(t) \implies \dot{n}(t) + 3H(t)n(t) = 0$$

Where H is the Hubble constant. This would be <u>the equation that would hold if the density of all</u> <u>particles would be constant with time</u>. The evolution of the density of DM is also related to the production or annihilation of DM

$$\dot{n}(t) = -3H(t)n(t) - \langle \sigma v \rangle_{\chi\chi} (n^{2}(t) - n_{eq}^{2})$$

where  $\langle \sigma v \rangle_{\chi\chi}$  is the thermal averaged cross section (luminosity), and  $n_{eq}$  is the equilibrium density. Note that

$$[\sigma vn] = m^2 \frac{m}{s} \frac{1}{m^3} = \frac{1}{s}$$

The thermal averaged cross section is given by

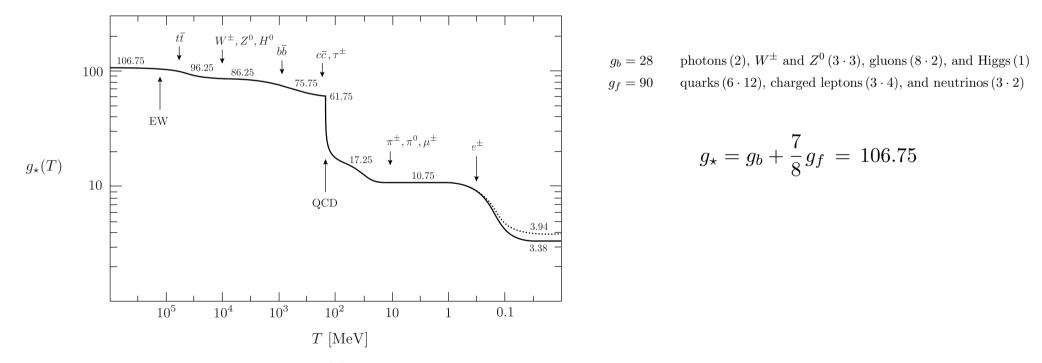
$$<\sigma v>_{\chi\chi} = \frac{\int d^3 p_{\chi,1} \int d^3 p_{\chi,2} e^{-(E_{\chi,1} + E_{\chi,2})/T} \sigma_{\chi\chi} v}{\int d^3 p_{\chi,1} \int d^3 p_{\chi,2} e^{-(E_{\chi,1} + E_{\chi,2})/T}}$$

$$v = \frac{\sqrt{(p_{\chi,1} \, p_{\chi,2}) - m_{\chi}^4}}{E_{\chi,1} \, E_{\chi,2}}$$

The equation is usually simplified with a change of variables Y = ns, leading to

$$\frac{dY}{dx} = -\sqrt{\frac{\pi}{45G}} \frac{g_*^{1/2} m_{\chi}}{x^2} \langle \sigma v \rangle_{\chi\chi} (Y^2 - Y_{\text{eq}}^2)$$

Where  $x = m_{\chi}/T$ , G is the gravitational constant and  $g_*$  are the relativistic degrees of freedom (that evolve over time). We have assumed that the total entropy on the universe remains constant with time.



**Figure 3.4:** Evolution of relativistic degrees of freedom  $g_*(T)$  assuming the Standard Model particle content. The dotted line stands for the number of effective degrees of freedom in entropy  $g_{*S}(T)$ .

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Going back to the Boltzmann equation in the form

$$\frac{dY}{dx} = -\sqrt{\frac{\pi}{45G}} \frac{g_*^{1/2} m_{\chi}}{x^2} \langle \sigma v \rangle_{\chi\chi} (Y^2 - Y_{\rm eq}^2) \qquad s' = h_{\rm eff}(T) \frac{2\pi^2}{45} T^3 , \quad \rho = g_{\rm eff}(T) \frac{\pi^2}{30} T^4$$

We can now integrate the equation to get the value of the Yield today.

The relic density can be calculated via

$$\Omega_{\chi} = \frac{\rho_{\chi,0}}{\rho_{\rm c}} = \frac{m_{\chi}n_0}{\rho_{\rm c}} = \frac{m_{\chi}s_0Y_0}{\rho_{\rm c}}$$

where  $s_0$  is the entropy density today and  $\rho_c = 3H^2/(8\pi G)$  is the critical density that separates a expanding from a collapsing universe. To match the definition of the observed relic density we need to multiply the above equation by

$$h^2 = \left(\frac{H}{100\frac{\mathrm{km}}{\mathrm{s\,Mpc}}}\right)^2$$

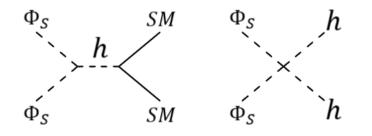
Introducing numerical values we get the following expression

$$\Omega_{\chi}h^2 = m_{\chi}s_0Y_o\frac{8\pi G}{3H^2} \approx 2.742 \times 10^8\frac{m_{\chi}}{GeV}Y_0$$

Experimental value  $\Omega_{\chi}h^2 = 0.1198 \pm 0.0015$ 

Now we just need to calculate  $Y_0$ . And we start with our favourite model

$$V = \mu^2 \Phi^{\dagger} \Phi + \lambda \left( \Phi^{\dagger} \Phi \right)^2 + \mu_S^2 \Phi_S^2 + \lambda_S \Phi_S^4 + \lambda_3 \Phi^{\dagger} \Phi \Phi_S^2$$



Note that the notation keeps changing!

We need to calculate the cross section for all possible processes, multiply by the relative velocity and find the thermal average.

But before that, the WIMP miracle.

## The WIMP miracle

We assume that DM is in thermal equilibrium with the SM particles, and is able to annihilate. At the point of thermal decoupling DM freezes-out with a density that is approximate the one that we measure today. The process of annihilation is

### $\chi\chi \to SMSM$

The interaction rate corresponding to the scattering process just compensates the increasing scale factor at the point of decoupling

### $\Gamma(T_{dec}) = H(T_{dec})$

If we assume that the interaction rate is set by the electroweak interactions and use the Z-boson coupling and mass, the cross section of the above process is of the order

$$\sigma_{\chi\chi} = \frac{\pi \alpha^2 m_{\chi}^2}{c_w^2 m_Z^4}$$

And after assuming a lot of other stuff (that could change the order of magnitude but not by much) we reach the conclusion

$$\Omega_{\chi} h^2 \approx 0.12 \left( \frac{13 \, {\rm GeV}}{m_{\chi}} \right)^2 \ . \label{eq:Glambda}$$

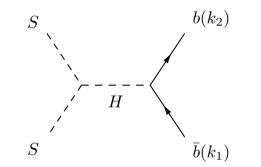
known as the WIMP miracle.

<u>Scalar</u> - The SM is extended by an extra real scalar singlet S, with a  $Z_2$  symmetry  $S \rightarrow -S$ 

$$\mathscr{L} = \mathscr{L}_{SM} + \frac{1}{2}(\partial_{\mu}S)(\partial^{\mu}S) - V_{N} + V_{SM}$$

Let us consider the solution (for the minimum) S = 0;  $h^2 = -\mu^2/(2\lambda)$ ;

And now let us calculate a specific process of DM annihilation to a b-quark pair



First we calculate the cross section. After that we make an approximation of averaging over a constant. Then we calculate Y today by approximating whatever we can to constants.

### What do we need?

$$v = 2\sqrt{\frac{s}{4m_{\chi}^2} - 1} \qquad \Omega_{\chi}h^2 = m_{\chi}s_0Y_o\frac{8\pi G}{3H^2} \approx 2.742 \times 10^8\frac{m_{\chi}}{GeV}Y_0 \qquad m_P = \sqrt{\frac{hc}{2\pi G}} = 1.22 \times 10^{19}\,GeV$$

Now we integrate from  $x_f$  (at freeze-out) to infinity

$$\frac{dY}{dx} = -\lambda \frac{Y^2}{x^2} \qquad \qquad x = \frac{m_{\chi}}{T} \qquad \qquad \lambda = \sqrt{\frac{\pi}{45G}} g_*^{1/2} m_{\chi} < \sigma v >_{\chi\chi}$$

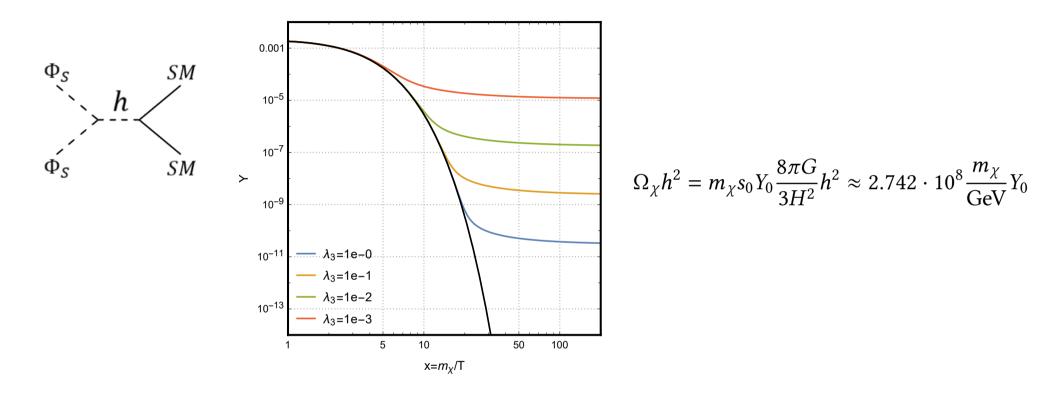
The result is

$$Y_0 = Y_\infty \approx \frac{x_f}{\lambda}$$

Considering  $x_f$  = 10 calculate the coupling for a DM of 100 GeV.

$$\Omega_{\chi}h^2 = m_{\chi}s_0Y_o\frac{8\pi G}{3H^2} \approx 2.742 \times 10^8\frac{m_{\chi}}{GeV}Y_0$$

Back to the complex singlet and considering only the final state with b quarks



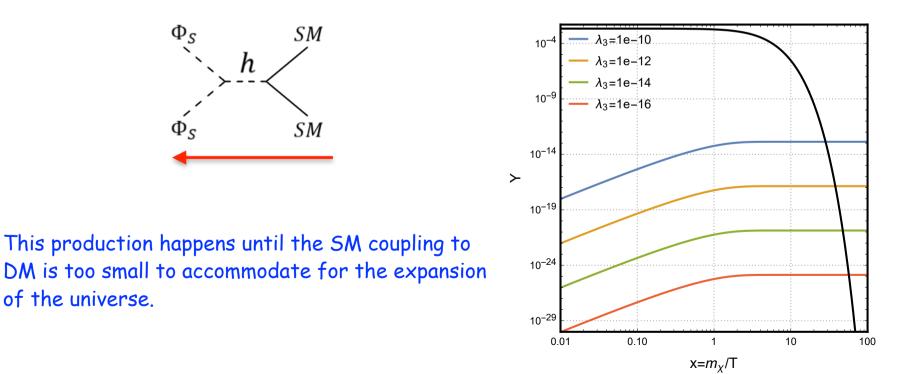
The figure shows the evolution of Y(x) as a function of x for different cross sections, that is, for different portal couplings. The larger the coupling the smaller the yield. The reason is that the thermal averaged cross section is a measure of how strongly the SM and the DM bath are coupled. A larger coupling means a more efficient interaction rate. This in turn means a smaller temperature and a larger x.

## Mechanisms of DM generation - freeze-in

Freeze-out may not happen if the portal coupling is too small. In that case the DM annihilation channels are not efficient enough to produce the current relic density.

In this regime of very weakly interacting massive particles, also called Feebly Interacting Massive Particles (FIMPs) the mechanism of freeze-in may come to the rescue.

In contrast to freeze- out, the DM particles do not start in thermal equilibrium with the SM and have a low initial abundance. Processes favour the direction of DM production from SM particles instead of annihilation of DM particles into SM particles.



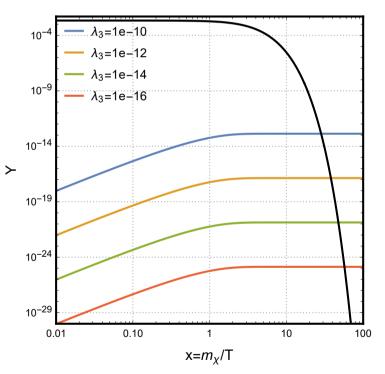
The calculation of the relic density via freeze-in is in general more involved than for freeze-out. Due to the fact that during freeze-in the DM particles are not in thermal equilibrium with the SM particles, the newly produced heavy DM particles have in general less kinetic energy than at equilibrium.

In terms of Y and x the Boltzmann equation now is

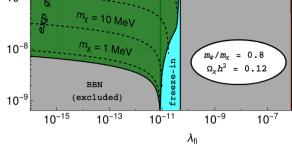
$$\frac{dY}{dx} = \sqrt{\frac{\pi}{45G}} \frac{g_*^{1/2} m_{\chi}}{x^2} \sum_{i,j=1}^N \langle \sigma v \rangle_{ij} (Y_{i,eq} Y_{j,eq} - Y_i Y_j)$$

The figure shows the relation between the coupling  $\lambda_3$ from the potential and the evolution of Y. As for to freeze-out a higher value of  $\lambda_3$  results in a larger TAC. In contrast to freeze-out though, a larger TAC results in a larger yield (and therefore relic density), because the annihilation of SM particles into DM is more efficient.

At temperatures lower than the dark matter mass, the bath no longer has enough energy to produce dark matter. At this point, the amount of dark matter has "frozen-in," there are no other ways to produce more dark matter.





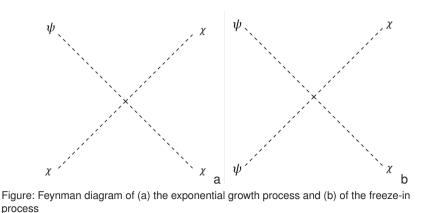


This is a mechanism that complements freeze-in and freeze-out production in a new parameter space to explain the observed DM abundance.

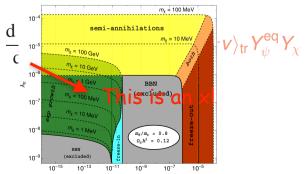
To make this work we need at least two DM particles  $(\chi, \psi)$ .  $\psi$  is already in thermal equilibrium with the SM bath in the early universe.  $\chi$  has a small initial value abundance created by freeze-in. Interaction between  $\psi$  and  $\chi$  leads to an exponential growth of  $\chi$  that shuts down at some point.

In this scenario we extend the SM with two real singlet scalar fields  $\chi, \psi$  that are odd under  $Z_2$  and all SM particles are even. The most general renormalisable Lagrangian is

$$\begin{split} \mathcal{L}_{\text{scalar,int}} &= - \, m_{11}^2 \Phi_1^{\dagger} \Phi_1 + m_{22}^2 \Phi_2^2 + m_{33}^2 \Phi_3^2 + m_{23} \Phi_2 \Phi_3 \\ &+ \lambda_1 (\Phi^{\dagger} \Phi)^2 + \lambda_2 \Phi_2^4 + \lambda_3 \Phi_3^4 + \lambda_{12} (\Phi_1^{\dagger} \Phi_1) \Phi_2^2 + \lambda_{13} (\Phi_1^{\dagger} \Phi_1) \Phi_3^2 \\ &+ \lambda_{23} \Phi_2^2 \Phi_3^2 + \lambda_{123} (\Phi_1^{\dagger} \Phi_1) \Phi_2 \Phi_3 + \lambda_{223} \Phi_2^3 \Phi_3 + \lambda_{332} \Phi_3^3 \Phi_2. \end{split}$$

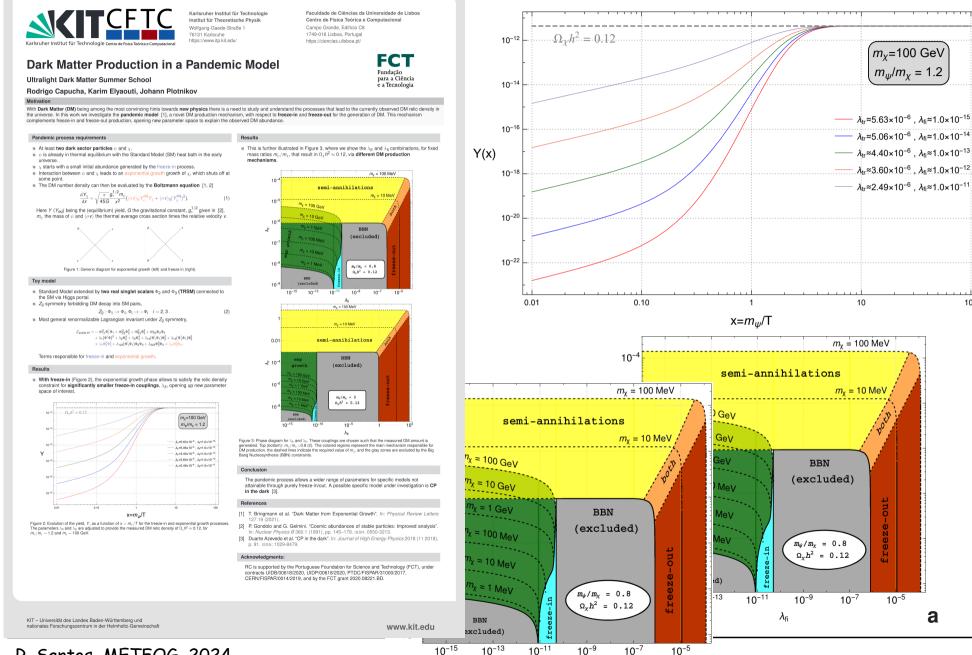


Here the terms which leads to freeze-in and exponential growth are highlighted.



$$\langle \mathbf{Y}_{\psi}^{\mathsf{eq}} \mathbf{Y}_{\chi} - \langle \sigma \mathbf{v} \rangle_{\mathsf{fi}} (\mathbf{Y}_{\psi}^{\mathsf{eq}})^2 ).$$

### Mechanisms of DM generation - pandemic



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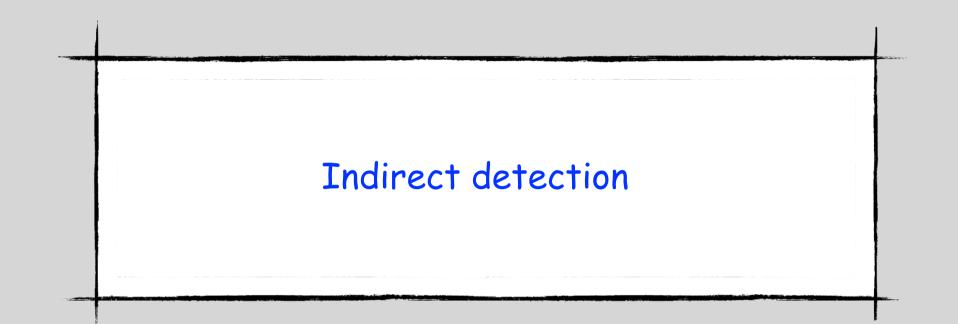
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$$\mathcal{M} = \bar{u}(k_2) \, \frac{-im_f}{v_H} \, v(k_1) \, \frac{-i}{(k_1 + k_2)^2 - m_H^2 + im_H \Gamma_H} \, \left(-2i\lambda_3 v_H\right)$$

$$\begin{split} \sum_{\text{spin}} |\mathcal{M}|^2 &= 4\lambda_3^2 m_f^2 \left( \sum_{\text{spin}} v(k_1) \bar{v}(k_1) \right) \left( \sum_{\text{spin}} u(k_2) \bar{u}(k_2) \right) \frac{1}{\left| (k_1 + k_2)^2 - m_H^2 + i m_H \Gamma_H \right|^2} \\ &= 4\lambda_3^2 m_f^2 \, \operatorname{Tr} \left[ (\mathbf{k}_1 - m_f \mathbf{1}) \, (\mathbf{k}_2 + m_f \mathbf{1}) \right] \frac{1}{\left[ (k_1 + k_2)^2 - m_H^2 \right]^2 + m_H^2 \Gamma_H^2} \\ &= 4\lambda_3^2 m_f^2 \, 4 \left[ k_1 k_2 - m_f^2 \right] \, \frac{1}{\left[ (k_1 + k_2)^2 - m_H^2 \right]^2 + m_H^2 \Gamma_H^2} \\ &= 8\lambda_3^2 m_f^2 \, \frac{(k_1 + k_2)^2 - 4m_f^2}{\left[ (k_1 + k_2)^2 - m_H^2 \right]^2 + m_H^2 \Gamma_H^2} \,. \end{split}$$

$$\begin{split} \overline{\sum_{\text{spin,color}} |\mathcal{M}|^2} &= N_c \; 8\lambda_3^2 m_b^2 \; \frac{s - 4m_b^2}{\left(s - m_H^2\right)^2 + m_H^2 \Gamma_H^2} \\ \sigma(SS \to b\bar{b}) &= \frac{1}{16\pi s} \; \sqrt{\frac{1 - 4m_b^2/s}{1 - 4m_S^2/s}} \; \overline{\sum |\mathcal{M}|^2} \\ &= \frac{N_c}{2\pi\sqrt{s}} \; \lambda_3^2 m_b^2 \; \sqrt{\frac{1 - 4m_b^2/s}{s - 4m_S^2}} \; \frac{s - 4m_b^2}{\left(s - m_H^2\right)^2 + m_H^2 \Gamma_H^2} \end{split}$$

$$\begin{split} \left< \sigma v \right> \left|_{SS \to b\bar{b}} \equiv \sigma v \right|_{SS \to b\bar{b}} \overset{\text{Eq.(3.19)}}{=} v \; \frac{N_c \lambda_3^2 m_b^2}{2\pi \sqrt{s}} \; \frac{\sqrt{1 - 4m_b^2/s}}{m_S v} \; \frac{s - 4m_b^2}{\left(s - m_H^2\right)^2 + m_H^2 \Gamma_H^2} \\ \overset{\text{threshold}}{=} \frac{N_c \lambda_3^2 m_b^2}{4\pi m_S^2} \; \sqrt{1 - \frac{m_b^2}{m_S^2}} \; \frac{4m_S^2 - 4m_b^2}{\left(4m_S^2 - m_H^2\right)^2 + m_H^2 \Gamma_H^2} \\ \overset{m_S \gtrless}{=} m_b \; \frac{N_c \lambda_3^2 m_b^2}{\pi} \; \frac{1}{\left(4m_S^2 - m_H^2\right)^2 + m_H^2 \Gamma_H^2} \; . \end{split}$$



There are many on-going experiments with the goal of detecting the products of DM annihilation in our Galaxy, or beyond.

We assume that DM annihilation is strongly suppressed after thermal freeze-out. However, it can still occur today and the chances of discovery can be maximised by searching in regions of very high DM density.

For most extensions of the SM, DM can annihilate to most of the SM particles.

We will just focus on <u>photon final states</u>. Depending on the model, DM can annihilate directly into a pair of photons, or into other SM states that then produce photons. The gamma-rays propagate essentially unperturbed, and can be detected by a satellite or ground-based telescope on Earth.

Let us consider that there are multiple DM annihilation channels, each with velocity-averaged cross section  $\langle \sigma_i v \rangle$ . The annihilation rate per particle is

$$\sum_{i} \frac{\rho\left[r(\ell,\psi)\right]}{m_{\chi}} \times \langle \sigma_{i} v \rangle$$

where r is the radial distance between the annihilation event and the Galactic Center—it is a function of the line-of-sight (l.o.s.) distance, l, which is oriented an angle  $\psi$  away from the Galactic plane.

The total annihilation rate in the volume dV =  $I^2 dI d\Omega$  is obtained by multiplying the previous equation by the total number of particles in the volume

$$\left(\sum_{i} \frac{\rho\left[r(\ell,\psi)\right]}{m_{\chi}} \left\langle \sigma_{i}v \right\rangle\right) \times \left(\frac{\rho\left[r(\ell,\psi)\right]}{2 m_{\chi}} dV\right) \quad \text{Factor of 2 because we need to DM particles to annihilate}$$

The photon flux is the annihilation rate multiplied by  $dN_i/dE_\gamma$ , that is, the number of photons at a given energy  $E_\gamma$  produced in the i<sup>th</sup> annihilation channel. The differential photon flux  $d\Phi/dE_\gamma$  in the observational volume oriented in the direction  $\psi$  is

$$\frac{d\Phi}{dE_{\gamma}}\left(E_{\gamma},\psi\right) = \frac{1}{4\pi} \int_{\Delta\Omega} d\Omega \int_{\text{l.o.s.}} d\ell \,\rho \left[r(\ell,\psi)\right]^2 \sum_{i} \frac{\langle\sigma_i v\rangle}{2m_{\chi}^2} \frac{dN_i}{dE_{\gamma}}$$

All the astrophysical uncertainties in the determination of the flux are absorbed by the J-factor

$$J = \frac{1}{\Delta\Omega} \int d\Omega \int_{\text{l.o.s.}} d\ell \, \rho \, [r(\ell, \psi)]^2$$

The larger the J-factor, the more interesting the astrophysical target is for DM annihilation. The J-factors for dwarf galaxies are roughly J ~  $10^{19-20} \text{ GeV}^2/\text{cm}^5$ . For our nearest neighbour, the Andromeda galaxy, J ~  $10^{20} \text{ GeV}^2/\text{cm}^5$ . For our own Galactic Center, J ~  $10^{22-25} \text{ GeV}^2/\text{cm}^5$  ( $10^{22-24}$ ) within 0.1°(1°).

The final state particles are stable leptons or protons propagating large distances in the Universe. While the leptons or protons can come from many sources, the anti-particles appear much less frequently. One key experimental task in many indirect dark matter searches is therefore the ability to measure the charge of a lepton, typically with the help of a magnetic field. For example, we can study the energy dependence of the antiproton–proton ratio or the

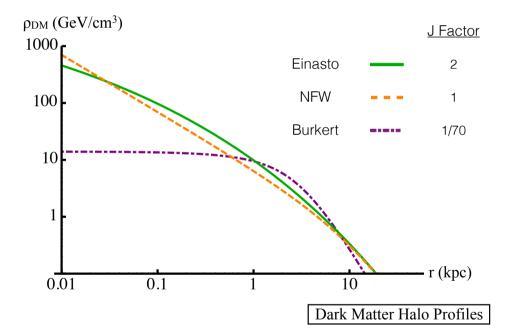


Figure 14: Dark matter galactic halo profiles, including standard Einasto and NFW profiles along with a Burkert profile with a 3 kpc core. J factors are obtained assuming a spherical dark matter distribution and integrating over the radius from the galactic center from  $r \simeq 0.05$  to 0.15 kpc. J factors are normalized so that  $J(\rho_{\text{NFW}}) = 1$ . Figure from Ref.[12]

However, when we choose a good target, there is a balance between the size of the J-factor and the potential backgrounds that has to be taken into account.

As an example, dwarf galaxies are DM-dominated and therefore some of the cleanest systems to search for DM because they contain very few stars and little gas. In contrast, a signal from the center of the Galaxy, while enhanced due to the DM density and proximity, has to contend with large systematic uncertainties on the astrophysical backgrounds.

The particle physics input to the flux is the factor (in most cases the velocity-averaged cross section can be pulled out of the integral)

$$\frac{\langle \sigma v \rangle_{\chi\chi}}{m_{\chi}^2} \frac{dN}{dE_{\gamma}}$$

The kinematics of the annihilation event determine the basic properties of the photon energy spectrum. Consider, first, the case where the DM annihilates directly into one or two photons:  $\chi \chi \rightarrow \gamma X$ , where X =  $\gamma$ , Z, H or some other neutral state. In the non-relativistic limit, energy conservation gives

$$2 m_{\chi} = E_{\gamma} + \sqrt{E_{\gamma}^2 + m_X^2} \longrightarrow E_{\gamma} \approx m_{\chi} \left( 1 - \frac{m_X^2}{4m_{\chi}^2} \right) \qquad \begin{array}{l} \mathsf{E}_{\mathsf{v}} \text{ is the energy of the outgoing photon in the} \\ \mathsf{CM} \text{ frame and } \mathsf{m}_{\mathsf{X}} \text{ is the mass of the X state.} \end{array}$$

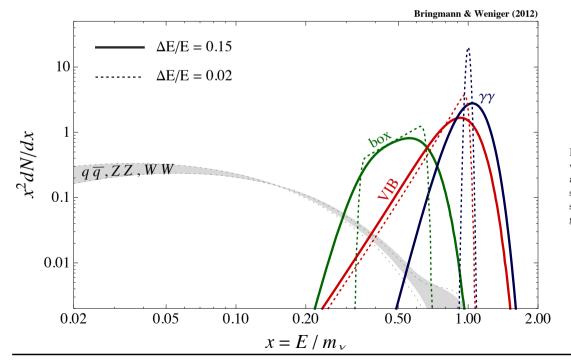
The  $\gamma\gamma$  final state results in a monochromatic energy line at the DM mass. For a  $\gamma Z$  final state, the gamma line is still monochromatic, but is shifted to lower energies.

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Blue lines - energy spectrum for a  $\gamma\gamma$  final state where the measured energy resolution is  $\Delta E/E = 0.15$  (solid) or 0.02 (dotted). The observation of such a gamma-ray 'line' would be spectacular evidence for DM annihilation. However, the production of a pair of gamma-rays is typically loop-suppressed (and therefore sub-dominant) in many theories.

Red lines - how the spectrum changes if photons are radiated off of virtual charged particles in the loop.

Green lines - illustrate the box spectrum, which arises when the DM annihilates to a new state  $\varphi$  (e.g.,  $\chi\chi \rightarrow \varphi\varphi$ ) that then decays to a photon pair ( $\varphi \rightarrow \gamma\gamma$ ).





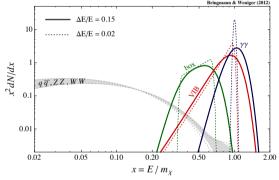


Figure 10: Illustration of the photon energy spectrum for the  $\gamma\gamma$  final state without (blue) and Figure 1: Various gamma-ray spectra expected from DM annihilation, all normalized to V(x > 0, 1) = 0 with (ref.) spectra had stable physical busics and share the spectra in the spectra in the spectra is an initiation of the photon of the

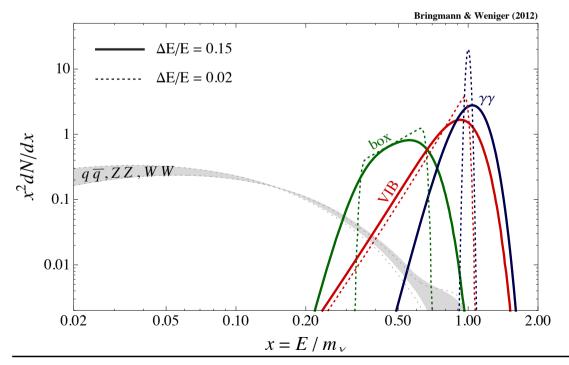
### 2.1. Lines

The direct annihilation of DM pairs into  $\gamma X$  – where  $X = \gamma, Z, H$  or some new neutral state – leads to *monochromatic* gamma rays with  $E_{\gamma} = m_{\chi} \left[ 1 - m_{\chi}^2 / 4m_{\chi}^2 \right]$ , providing a striking signature which is essentially impossible to mimic by astrophysical contributions [51]. Unfortunately, these processes are loop-suppressed with  $O(\alpha_{em}^2)$  and thus usually subdominant, i.e. not actually visible against the continuous (both astrophysical and DM induced) background when taking into account realistic detector resolutions; however, examples of particularly strong line signals exist [32, 33, 52–56]. A space-based detector with resolution  $\Delta E/E = 0.1$  (0.01) could, e.g., start to discriminate be-

tween  $\gamma\gamma$  and  $\gamma Z$  lines for DM masses of roughly  $m_{\chi} \lesssim 150 \text{ GeV}$  ( $m_{\chi} \lesssim 400 \text{ GeV}$ ) if at least one of the lines has a statistical significance of  $\gtrsim 5\sigma$  [57]. This would, in princip**105** open the fascinating possibility of doing 'DM spectroscopy' (see also Section 5).

Another possibility is that the DM annihilates to leptons, gauge bosons, or quarks, which may produce <u>secondary photons</u> either through final-state radiation or in the shower of their decay products. The photon energy spectrum  $dN/dE_{\gamma}$  depends on the exact details of the final-state radiation, and must be determined with Monte Carlo tools like Pythia.

In the case of secondary photon production, the energy spectrum does not have a very distinctive shape, and one must search for a continuum excess over the background. The grey band in shows an example of the spectrum for annihilation to quarks or gauge bosons.



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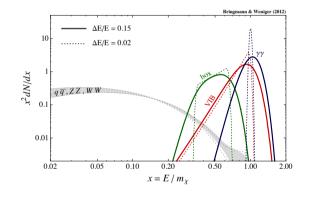


Figure 10: Illustration of the photon energy spectrum for the  $\gamma \gamma_1$  final state without (blue) and with (ref.) spectra high state spectral from DM annihilation, all normalized to V(x > 0, 1) = 0annihilation state are was the state of the state of the spectra state of the spec

#### 2.1. Lines

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The details of the annihilation mechanism are in the velocity-averaged cross section  $\langle \sigma v \rangle$ . This cross section is the same in many simple models as what appears in the relic density calculation.

In addition, we automatically have an interesting target scale for the cross section:  $3 \times 10^{-26}$  cm<sup>3</sup> s<sup>-1</sup>. This regime was probed by the best gamma-ray observatories. For example, the Fermi Large Area Telescope has searched for signals of DM annihilation in the Milky Way's dwarf galaxies.

Figure show the results for DM annihilation (from FermiLAT) to bb (left) and tau tau (right)

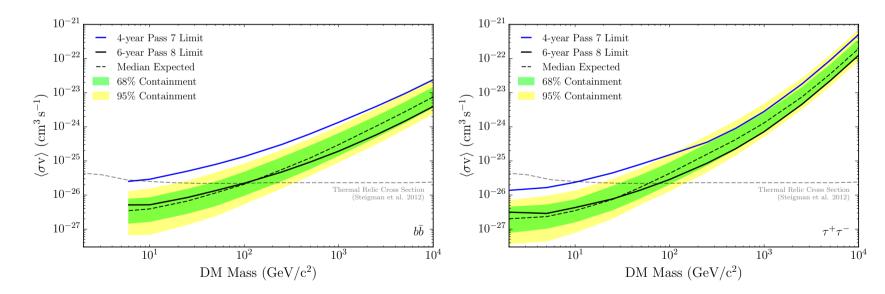
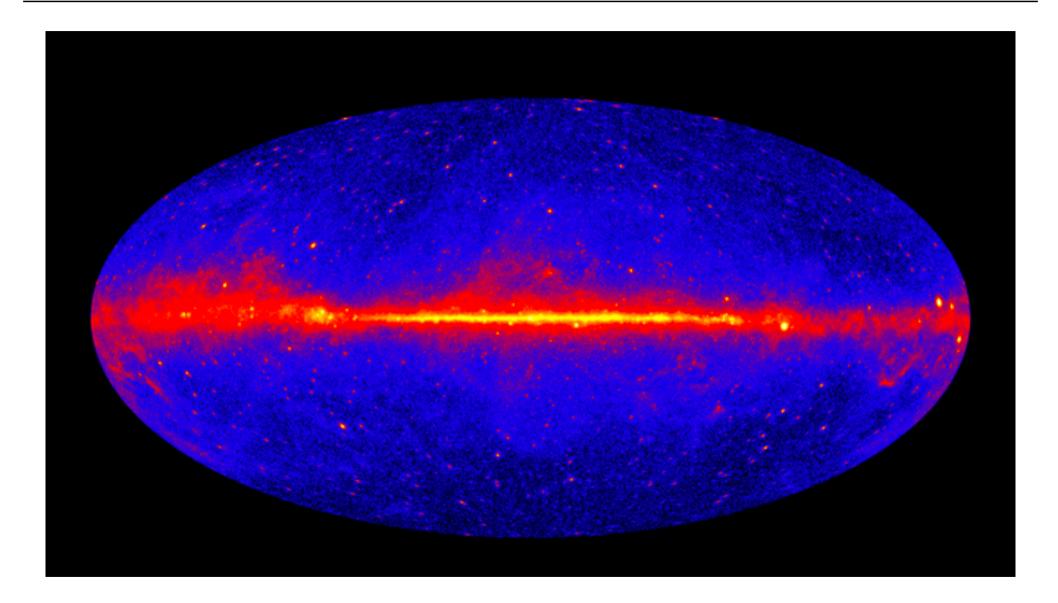


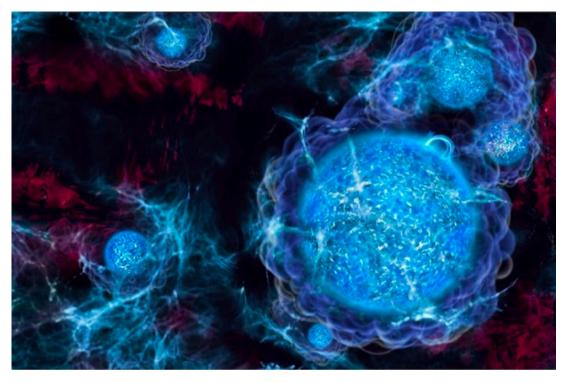
Figure 11: Fermi LAT limits on DM annihilation into bb (left) and  $\tau^+\tau^-$  (right) final states. The dashed black line is the expected bound with 68% and 95% contours shown in green and yellow, respectively. The solid black line is the observation with six-year Pass 8 data. Figure from [99].





# Ultralight DM

Dark matter can be ultra-light. If DM is in the mass range of  $10^{-20} - 10^{-10}$  eV, it can produce compact objects that in turn may produce Gravitational Waves (GW) that can be probed by current and future experiments. These objects are known as boson stars.



The production mechanisms in this case are: the misalignment mechanism, decay of thermal relics, freeze-out and decay of topological defects (Domain Walls and Cosmic Strings).

An ultralight DM thermally produced is hard, because it behaves as hot dark matter and it can jeopardise the period of structure formation.

However, if the pNGB has an extremely small coupling with the SM particles, it ensures it will not be thermally produced.

We can use the same extension of the SM that we have used for the scalar DM. This DM candidate has can be ultralight dark matter.

# Ultralight DM

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Using the exact same potential for a complex scalar field invariant under U(1) with a soft breaking term we can describe such a light particle.

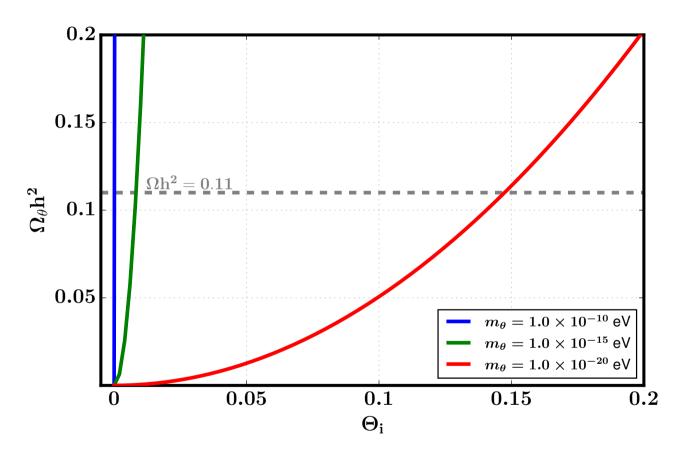
$$V(H,\phi) = V_0(H) + \mu_{\phi}^2 \phi \phi^* + \frac{1}{2} \lambda_{\phi} |\phi \phi^*|^2 + \lambda_{H\phi} H^{\dagger} H \phi \phi^* + V_{\text{soft}},$$
$$V_0(H) = \mu_H^2 H^{\dagger} H + \frac{1}{2} \lambda_H \left( H^{\dagger} H \right)^2 \qquad V_{\text{soft}} = \frac{1}{2} \mu_s^2 \left( \phi^2 + \phi^{*2} \right)$$

Resulting in a very small self-interaction

$$\phi = \frac{1}{\sqrt{2}} \left( \sigma + \nu_{\sigma} \right) e^{i\theta/\nu_{\sigma}} \qquad \qquad \lambda_{\theta\theta\theta\theta} = -\frac{m_{\theta}^2}{6\nu_{\sigma}^2}$$

# Ultralight DM

Ultralight non-thermal DM produced via the misalignment mechanism.



 $V_{\rm soft} = \frac{\mu_s^2}{2} \left(\sigma + \nu_\sigma\right)^2 \cos\left(2\frac{\theta}{\nu_\sigma}\right)$ 

Figure 1: Abundance of ultralight DM for the case where the SSB occurs before the end of inflation, for  $m_{\theta} = 10^{-10}$  eV,  $10^{-15}$  eV and  $10^{-20}$  eV for blue, green and red curves, respectively. Here, we fixed  $\nu_{\sigma} = 10^{17}$  GeV.